



Exclusive $|V_{ub}|$ and $|V_{cb}|$

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Outline

Introduction

$|V_{cb}|$ from $B \rightarrow D^* l \nu$

Study of D^{**} states in $B \rightarrow D^{**} l \nu$ decay

$|V_{ub}|$ from $B \rightarrow \pi l \nu$ (and other exclusive charmless SL decays)

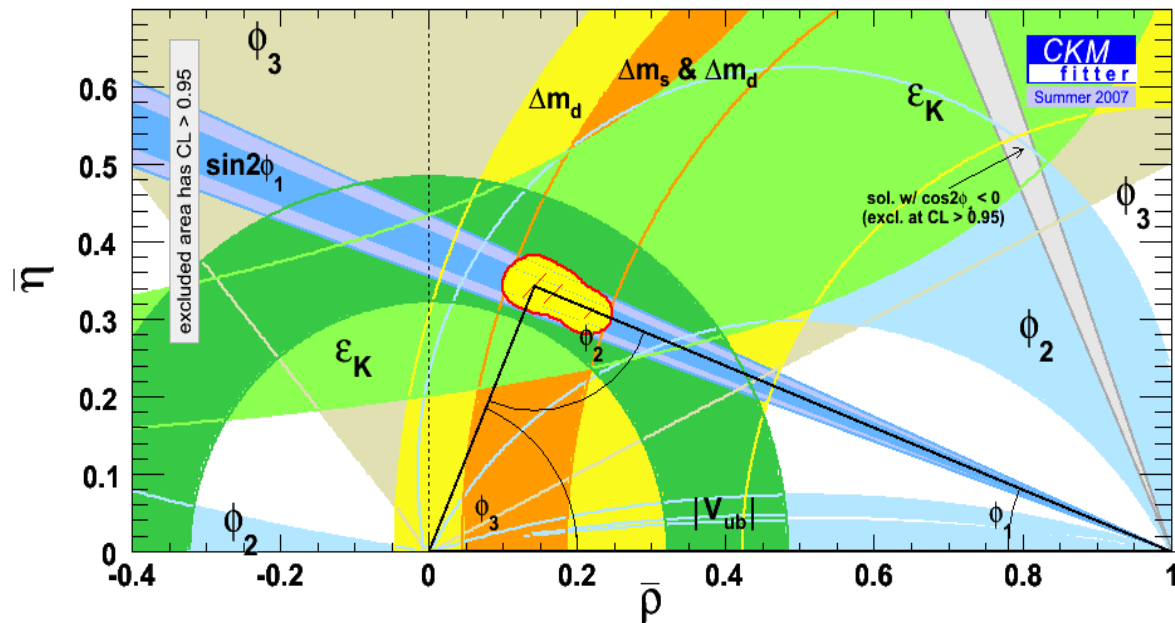
Summary

Motivation

Test of unitarity of the CKM matrix

Overconstrain the unitarity triangle by various parameters

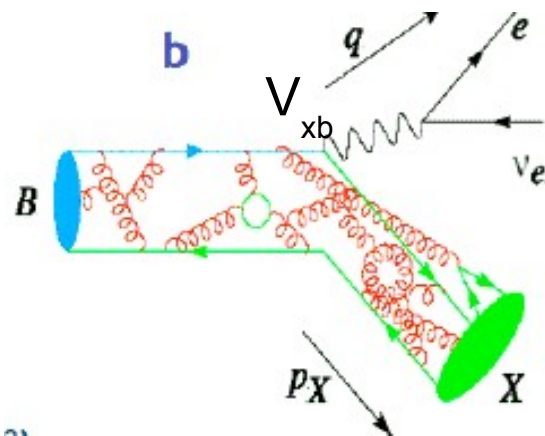
- Two of the important variables are $|V_{ub}|$ and $|V_{cb}|$
- $|V_{ub}|$ and $|V_{cb}|$ constrain sides of the unitarity triangle



How to measure $|V_{cb}|$ & $|V_{ub}|$

Use semileptonic B decay

Clear lepton signal, tree level diagram but...



Quarks are bound by soft gluons:
non-perturbative

Use different two approaches

Inclusive analyses

Needs: extrapolation to the full phase space by theory

Exclusive analyses

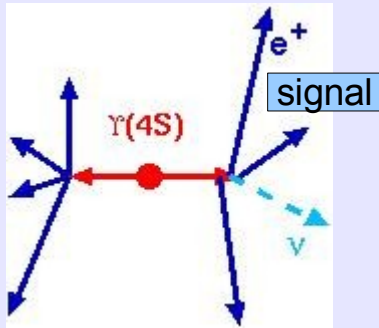
Needs: prediction of form factor by theory

Experimental technique

The event contain missing neutrino(s)

Various method according to the size of luminosity and expected BF

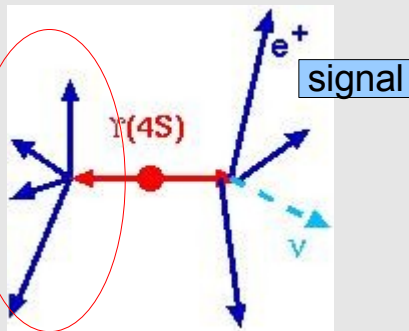
Kinematics



Use only signal side:

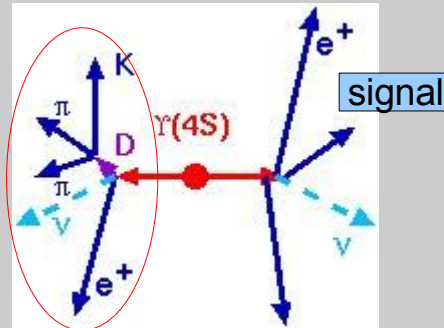
$$\cos \theta_{B, D^*} = \frac{2 E_B E_{D^*} - m_B^2 - m_{D^*}^2}{2 p_B p_{D^*}}$$

Untagged



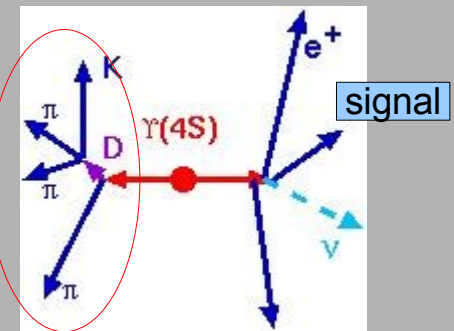
Use for ν recon

Semileptonic (SL) tag



Tag by $D^{(*)} l \nu$
+kinematics

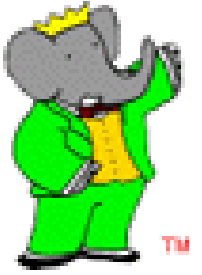
Full reconstruction (B_{reco}) tag



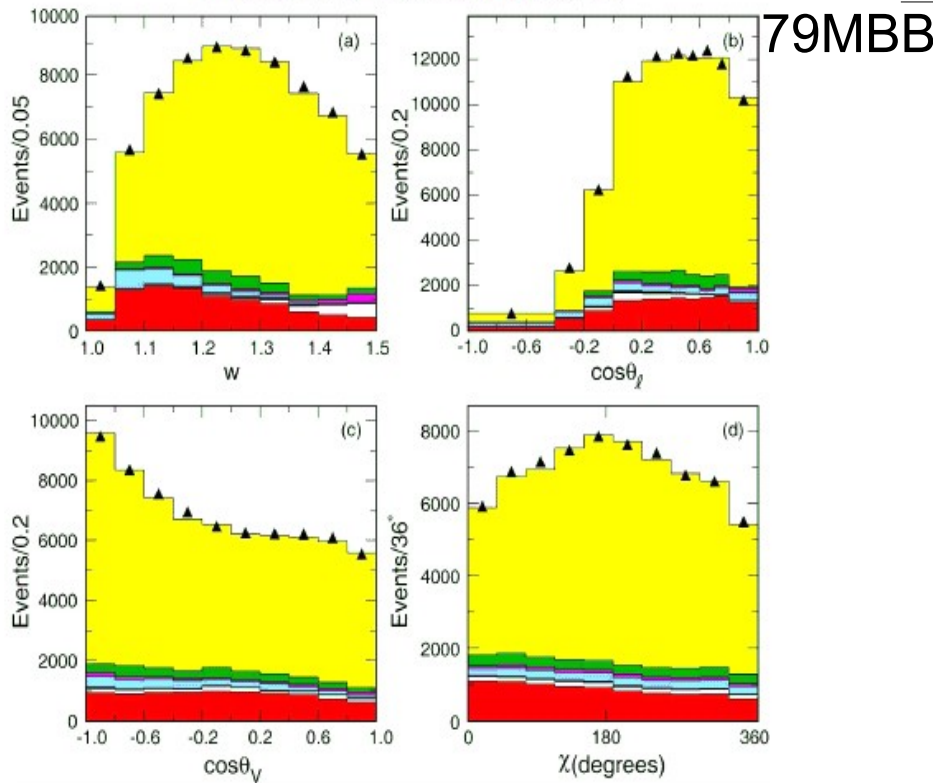
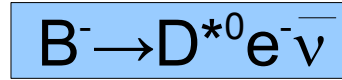
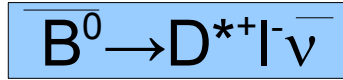
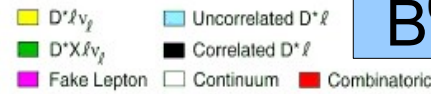
Tag by a fully
reconstructed B

low ← ————— purity ————— → high
high efficiency low

$$|V_{cb}|$$



$$\frac{d\Gamma(B \rightarrow D^* l \nu)}{dW} = K(W) F(w)^2 |V_{cb}|^2$$



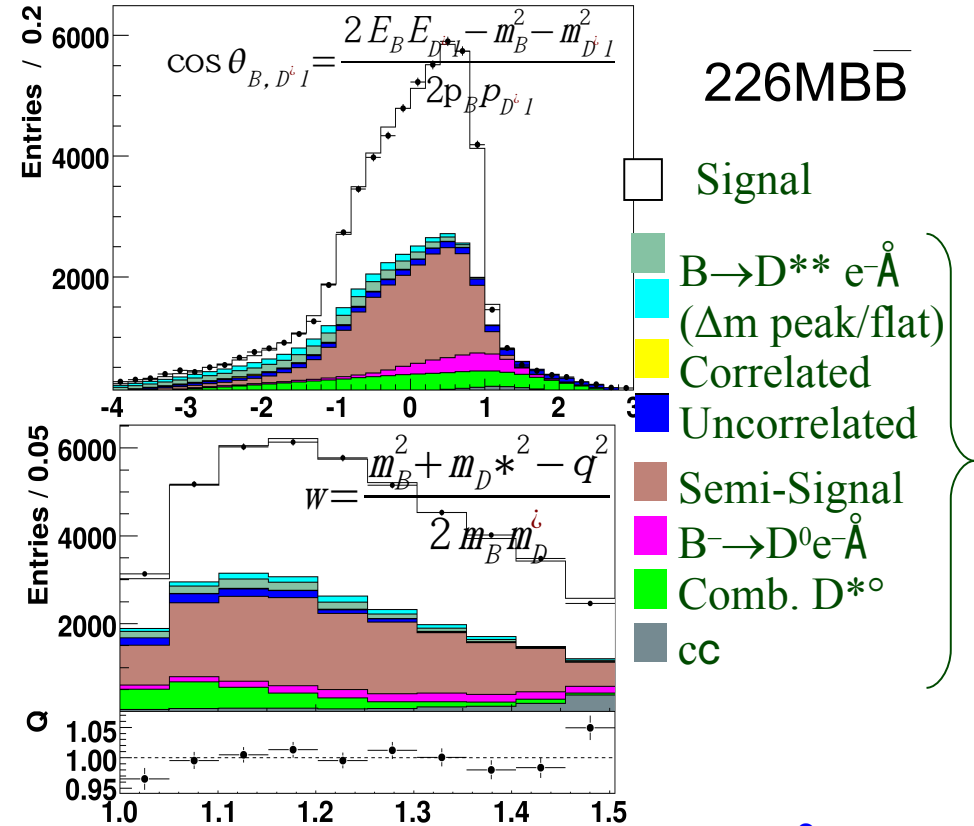
$$F(1)|V_{cb}| = (34.7 \pm 0.4 \pm 1.0) \times 10^{-3}$$

Form factor parameters:

$$\rho^2 = 1.157 \pm 0.094 \pm 0.027$$

$$R_1(1) = 1.327 \pm 0.131 \pm 0.043$$

$$R_2(1) = 0.859 \pm 0.077 \pm 0.021$$



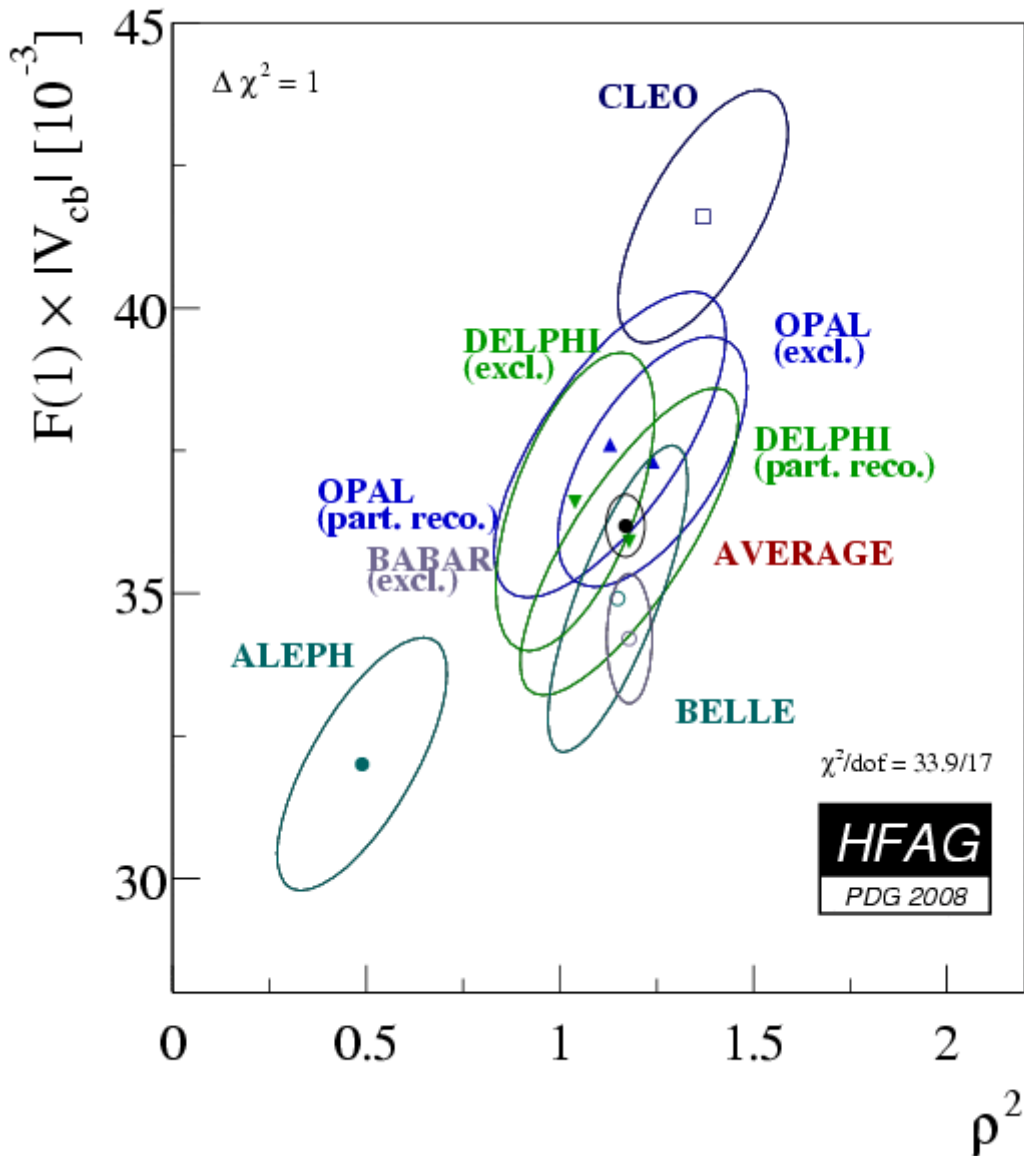
$$F(1)|V_{cb}| = (35.9 \pm 0.6 \pm 1.4) \times 10^{-3}$$

$$\rho^2 = 1.16 \pm 0.06 \pm 0.08$$

$$\text{BF}(B^- \rightarrow D^{*0} e^- \bar{\nu}) = (5.56 \pm 0.08 \pm 0.41)\%$$

Complementary to $D^{*+} e^- \bar{\nu}$ analyses

$|V_{cb}|$ from $D^{*+}l^{-}\bar{\nu}$



$$F(1)|V_{cb}| = (36.18 \pm 0.55) \times 10^{-3}$$

$$\rho^2 = 1.17 \pm 0.05$$

Lattice calculation predicts:

$$F(1) = 0.919 \pm 0.033$$

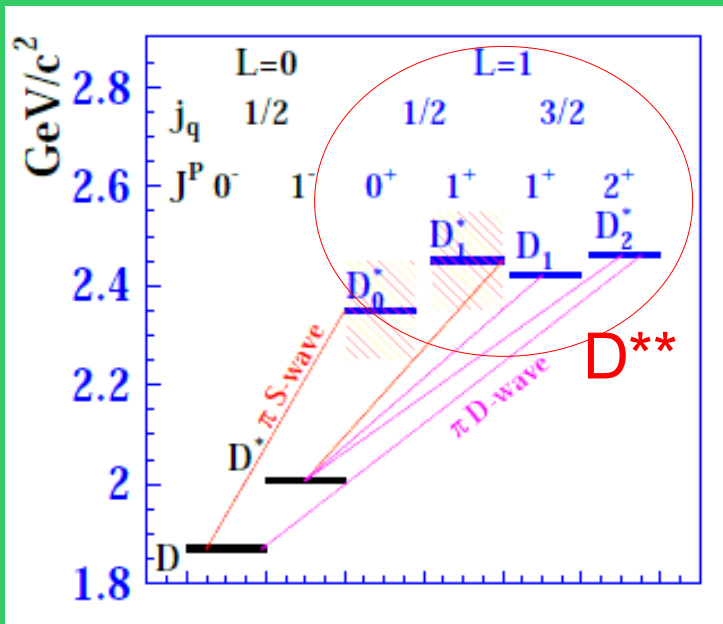
$$|V_{cb}| = (39.37 \pm 0.60 \pm 1.41) \times 10^{-3}$$



Error is dominated by the uncertainty in the lattice calculation

B → D^{**} l ν: Introduction

- Not directly used for $|V_{cb}|$ extraction but is important for systematics for e.g. $|V_{cb}|$ measurement by $D^* l ν$
- D^{**} spectroscopy itself is interesting:



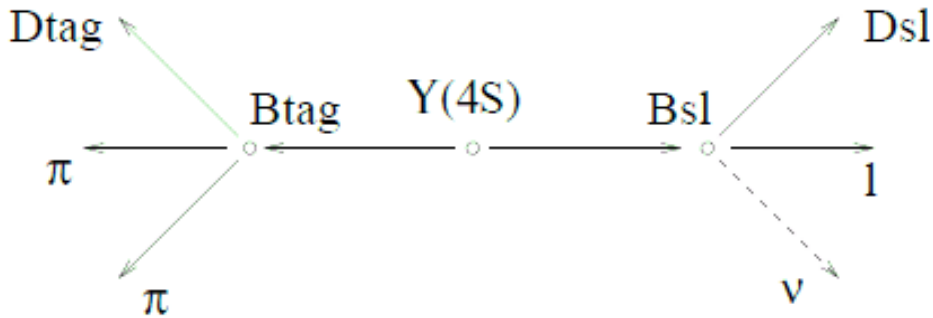
HQET predicts:

$$\begin{aligned} \text{Br}(B \rightarrow D_1 l \nu) &>> \text{Br}(B \rightarrow D_0^* l \nu) \\ \text{Br}(B \rightarrow D_2^* l \nu) &>> \text{Br}(B \rightarrow D_1' l \nu) \\ \text{Narrow } D^{**} &>> \text{Wide } D^{**} \end{aligned}$$

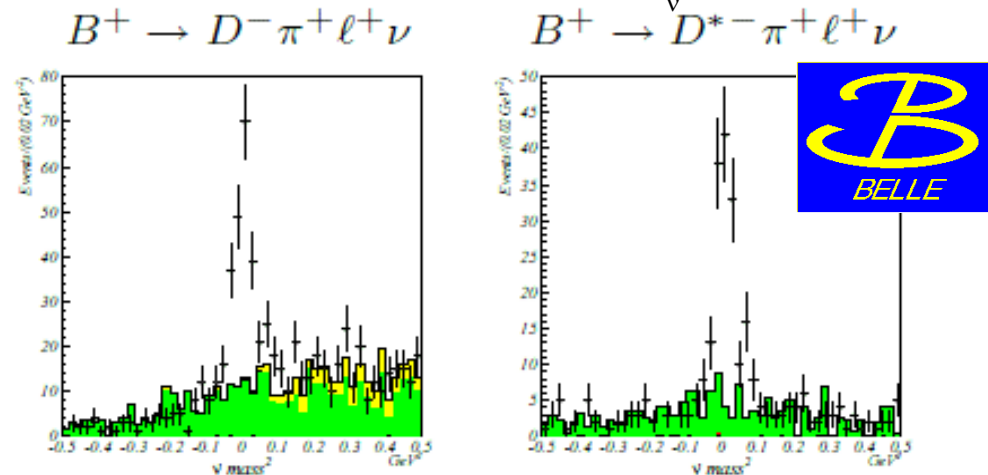
Bigi et al.
arXiv:0708.1621

B → D**lν: analysis method

B_{reco} tag method to obtain good M_ν² resolution

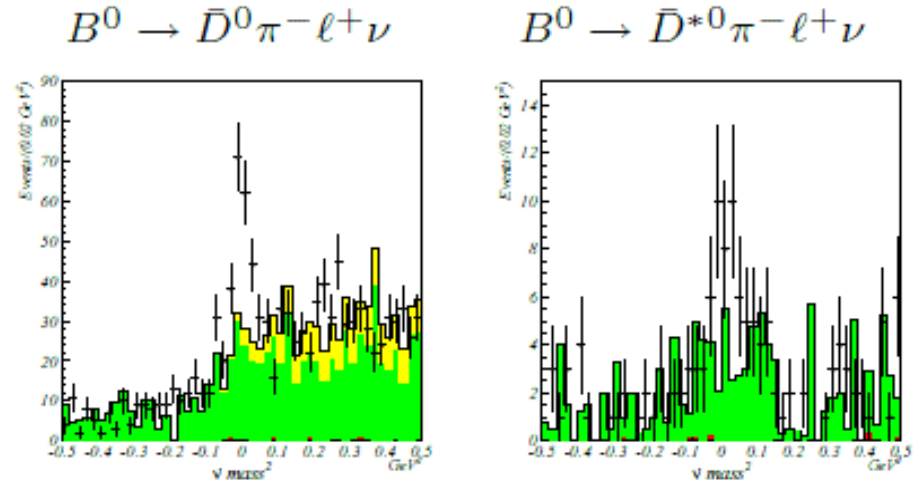


Distributions of M_ν²

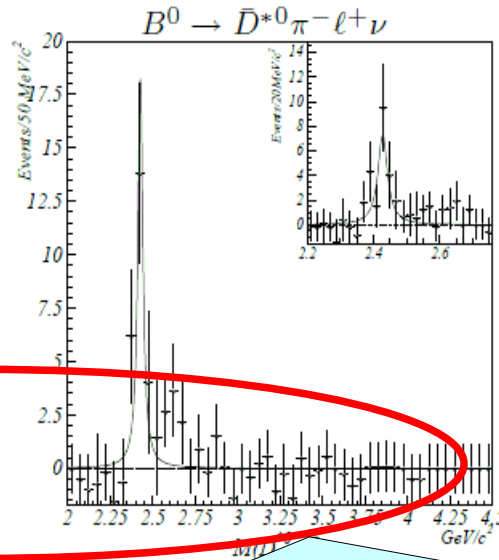
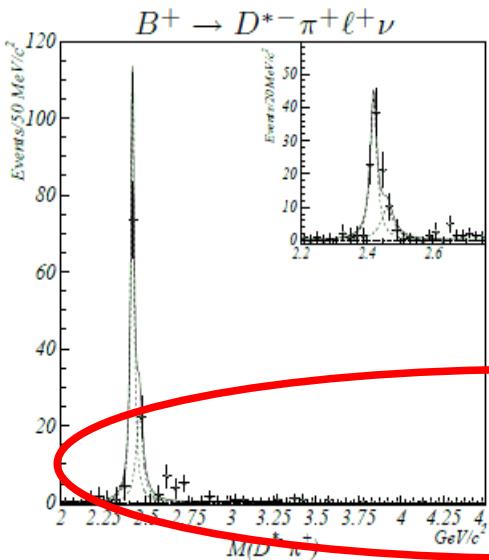
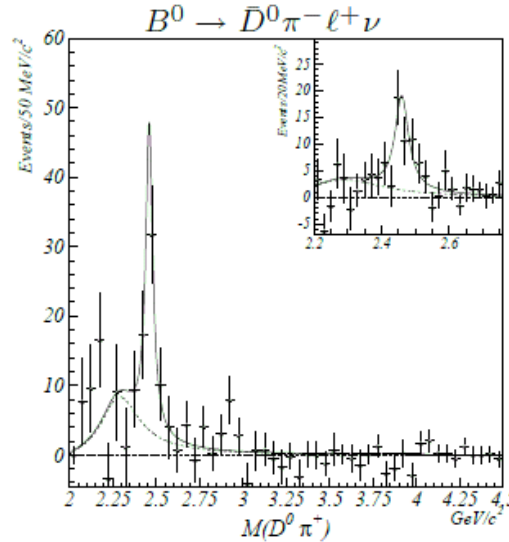
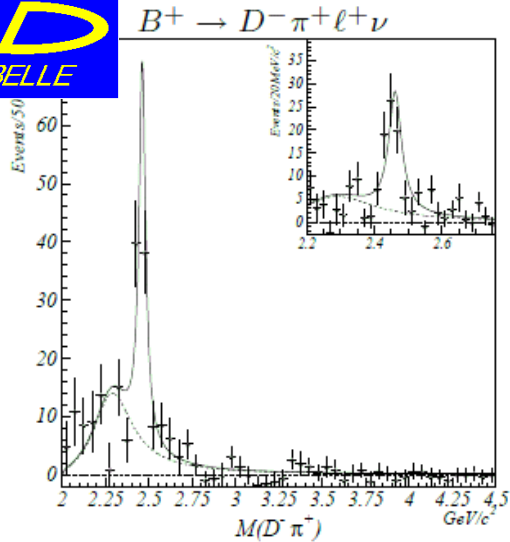


Calculate missing mass squared M_ν²

$$M_\nu^2 = (P_{\text{beam}} - P_{B_{\text{tag}}} - P_{B_{\text{sl}}})^2$$



B → D** l ν : D** states from Belle



Large BF for $D_0^* l \nu$



HQET prediction

$$\frac{\text{BF}(B \rightarrow D_2^* l \nu)}{\text{BF}(B \rightarrow D_0^* l \nu)} \sim 10$$

$B(\text{mode}) \rightarrow D^{**} l \nu \times B(D^{**} \rightarrow D^{(*)} \pi^+)$
 π invariant mass study

Mode	Yield	B, %	Signif.
$B^+ \rightarrow D_0^{*0} \ell^+ \nu$	102 ± 19	$0.24 \pm 0.04 \pm 0.06$	5.4
$B^+ \rightarrow \bar{D}_2^{*0} \ell^+ \nu$	94 ± 13	$0.22 \pm 0.03 \pm 0.04$	8.0
$B^0 \rightarrow D_0^{*-} \ell^+ \nu$	61 ± 22	$0.20 \pm 0.07 \pm 0.05$	2.6
$B^0 \rightarrow D_2^{*-} \ell^+ \nu$	68 ± 13	$0.22 \pm 0.04 \pm 0.04$	5.5

$D^* \pi$ invariant mass study

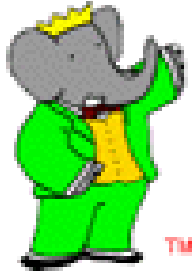
Mode	Yield	B, %	Signif.
$B^+ \rightarrow D_1^{*0} \ell^+ \nu$	-5 ± 11	< 0.07 @ 90% C.L.	
$B^+ \rightarrow \bar{D}_1^{*0} \ell^+ \nu$	81 ± 13	$0.42 \pm 0.07 \pm 0.07$	6.7
$B^+ \rightarrow \bar{D}_2^{*0} \ell^+ \nu$	35 ± 11	$0.18 \pm 0.06 \pm 0.03$	3.2
$B^0 \rightarrow D_1^{*-} \ell^+ \nu$	4 ± 8	< 0.5 @ 90% C.L.	
$B^0 \rightarrow D_1^{*-} \ell^+ \nu$	20 ± 7	$0.54 \pm 0.19 \pm 0.09$	2.9
$B^0 \rightarrow D_2^{*-} \ell^+ \nu$	1 ± 6	< 0.3 @ 90% C.L.	

arXiv:0711.3252

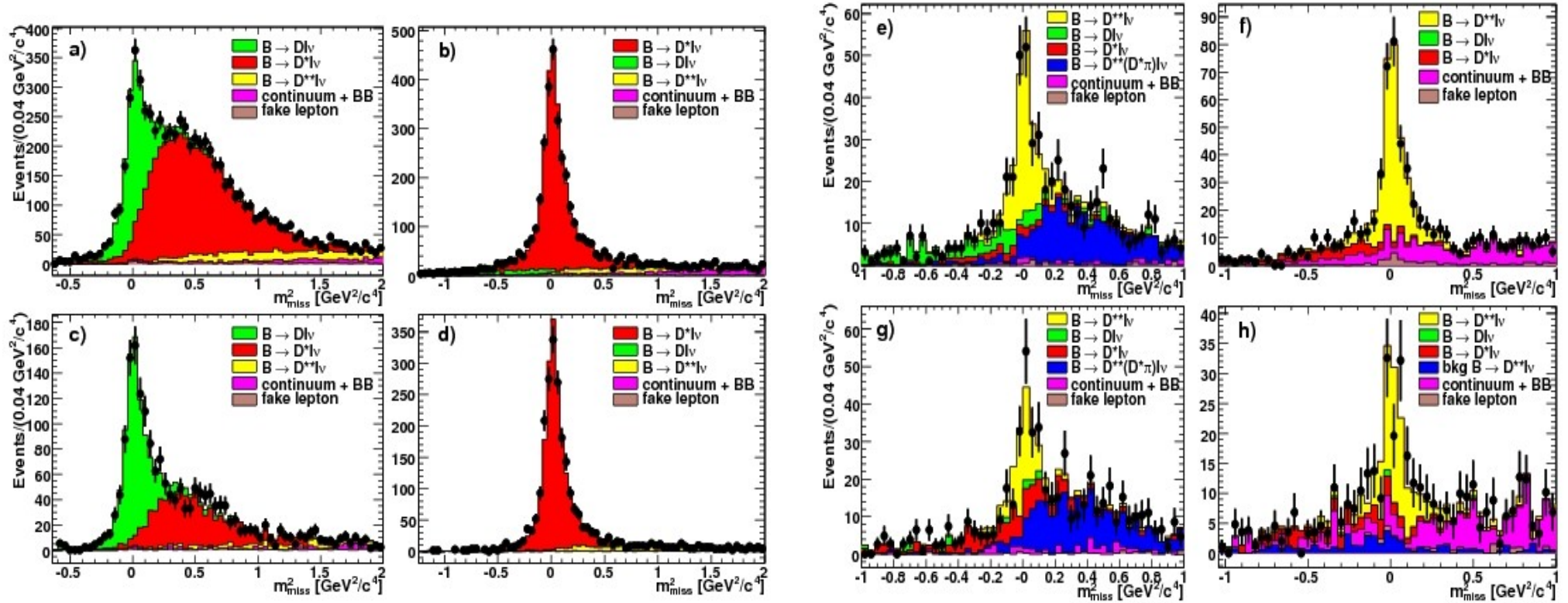
Broad resonance ($B \rightarrow D_1' l \nu$) is not seen

$B \rightarrow D\ell\nu/D^*\ell\nu/D^{**}\ell\nu$ from Babar

Measurement of branching fractions by B_{eco} tag method

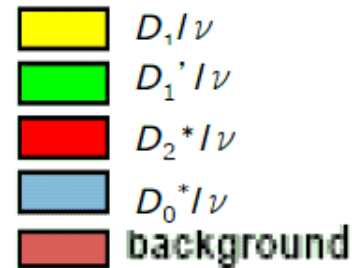
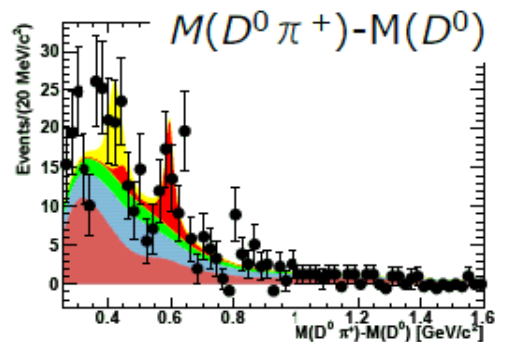
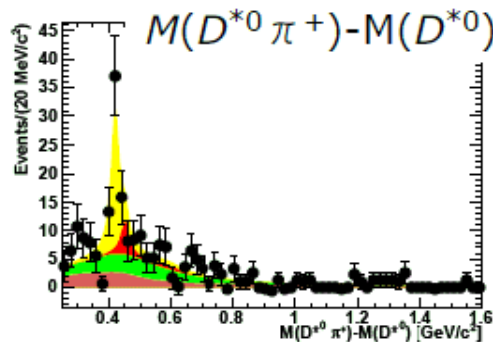
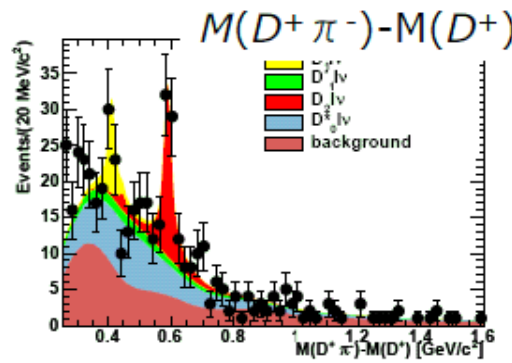
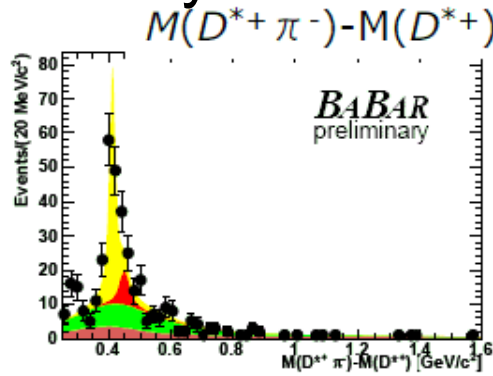


Mode	$\mathcal{B}(B^-)$ [%]	$\mathcal{B}(\bar{B}^0)$ [%]
$D\ell^-\bar{\nu}_\ell$	$2.33 \pm 0.09 \pm 0.09$	$2.21 \pm 0.11 \pm 0.12$
$D^*\ell^-\bar{\nu}_\ell$	$5.83 \pm 0.15 \pm 0.30$	$5.49 \pm 0.16 \pm 0.25$
$D\pi^\pm\ell^-\bar{\nu}_\ell$	$0.42 \pm 0.06 \pm 0.03$	$0.43 \pm 0.08 \pm 0.03$
$D^*\pi^\pm\ell^-\bar{\nu}_\ell$	$0.59 \pm 0.05 \pm 0.04$	$0.48 \pm 0.08 \pm 0.04$
$\mathcal{B}(B^- \rightarrow D^{(*)}\pi\ell^-\bar{\nu}_\ell) = (1.52 \pm 0.12_{\text{stat.}} \pm 0.10_{\text{syst.}})\%$		
$\mathcal{B}(\bar{B}^0 \rightarrow D^{(*)}\pi\ell^-\bar{\nu}_\ell) = (1.37 \pm 0.17_{\text{stat.}} \pm 0.10_{\text{syst.}})\%$		



$B \rightarrow D^{**} l \nu : D^{**}$ states from BaBar

Study of the $D^{**} l \nu$ states



$$\text{BF}(B^- \rightarrow D_1^0 l \nu) = 0.42 \pm 0.04 \pm 0.04 \%$$

$$\text{BF}(B^- \rightarrow D_1'^0 l \nu) = 0.47 \pm 0.06 \pm 0.06 \%$$

$$\text{BF}(B^- \rightarrow D_2^{*0} l \nu) = 0.29 \pm 0.05 \pm 0.03 \%$$

$$\text{BF}(B^- \rightarrow D_0^{*0} l \nu) = 0.52 \pm 0.07 \pm 0.06 \%$$

-Large Br for wide states ($D_0^* l \nu, D_1' l \nu$)

disagree with HQET prediction

-Large Br for $D_1' l \nu$

disagree with Belle result ($>6\sigma$)

$$|V_{ub}|$$

Exclusive $|V_{ub}|$

Experimentally various modes can be measured:

- $B \rightarrow \pi l \nu, \rho l \nu, \omega l \nu, \eta l \nu, \eta' l \nu$

Currently, only $B \rightarrow \pi l \nu$ can be used for $|V_{ub}|$ extraction:



Form factor calculation from various methods:

- lattice QCD (HPQCD, Fermilab,...)
- Light-Cone Sum Rules (Ball & Zwicky,...)
- quark models (ISGW2,...)

Recent results:

CLEO untagged method: Phys.Rev.Lett.99:041802 (2007)

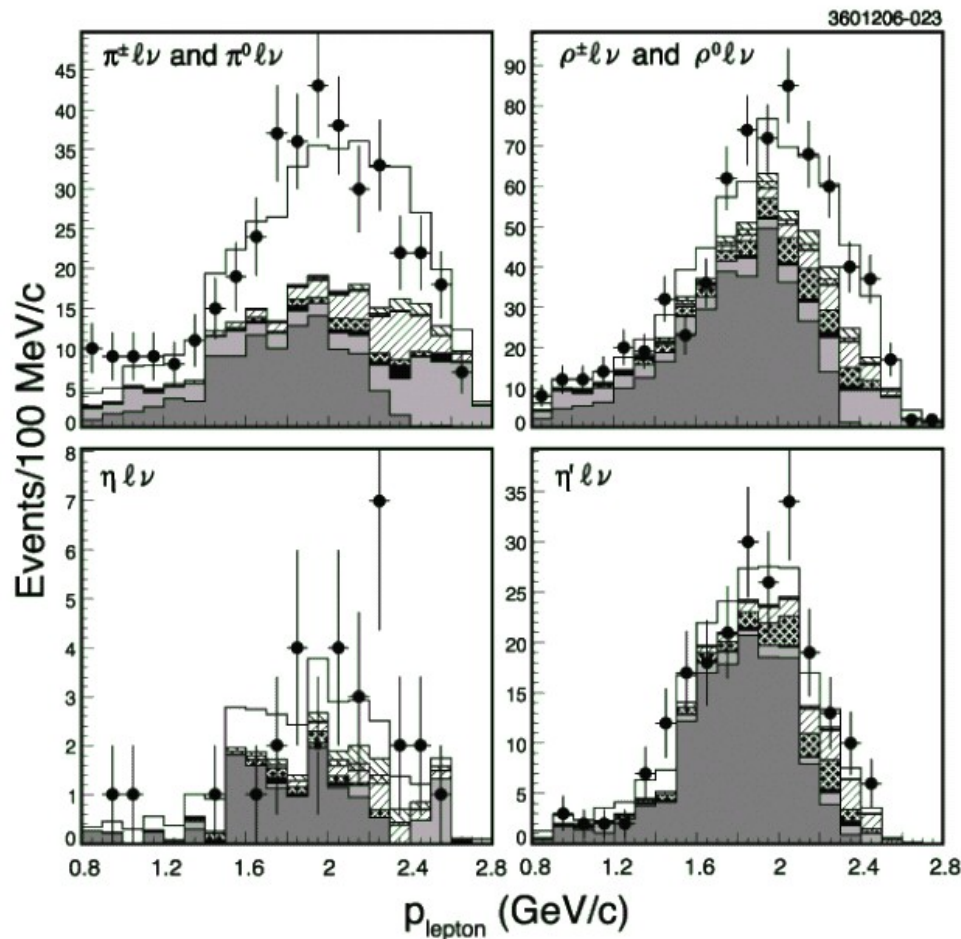
BaBar untagged method: Phys. Rev. Lett. 98:091801 (2007)

Belle SL tag method: Phys.Lett.B648:139-148 (2007)

$B \rightarrow \pi \ell \nu / \rho \ell \nu / \eta \ell \nu / \eta' \ell \nu$: untagged method

CLEO 17MBB

Lepton momentum projection

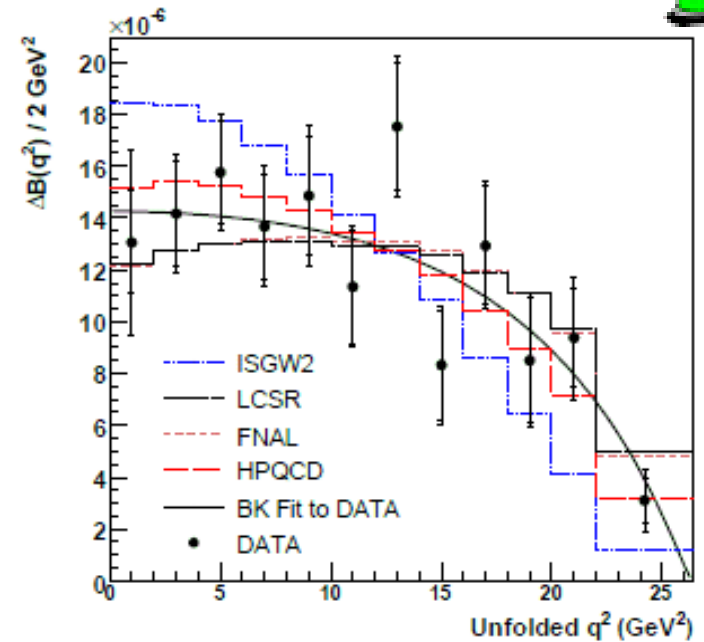
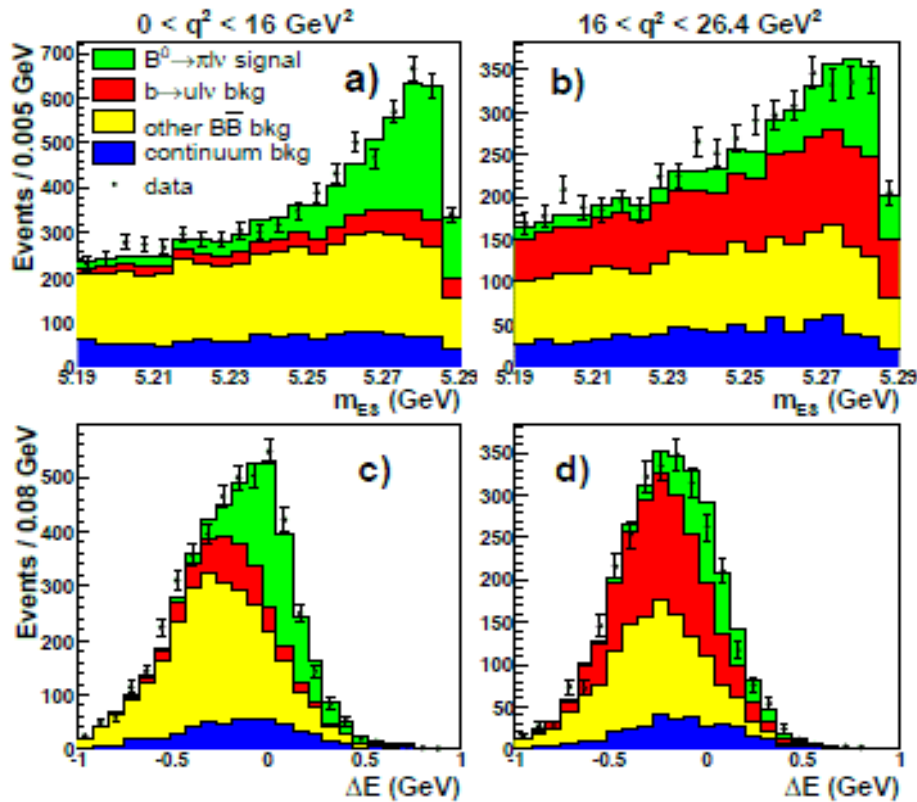
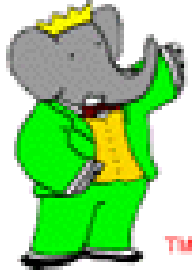


	q^2 [GeV ²]	$\cos \theta_{Wl}$	\mathcal{B} [10^{-4}]
$B^0 \rightarrow \pi^- \ell^+ \nu$	0 - 2	-1 - 1	$0.13 \pm 0.07 \pm 0.02$
	2 - 8	-1 - 1	$0.27 \pm 0.08 \pm 0.03$
	8 - 16	-1 - 1	$0.56 \pm 0.09 \pm 0.05$
	> 16	-1 - 1	$0.41 \pm 0.08 \pm 0.04$
	all phase space		$1.37 \pm 0.15 \pm 0.11$
$B^0 \rightarrow \rho^- \ell^+ \nu$	0 - 2	-1 - 1	$0.45 \pm 0.20 \pm 0.15$
	2 - 8	-1 - 1	$0.96 \pm 0.20 \pm 0.29$
	8 - 16	0 - 1	$0.75 \pm 0.16 \pm 0.14$
	> 16	0 - 1	$0.35 \pm 0.07 \pm 0.05$
	> 8	-1 - 0	$0.42 \pm 0.18 \pm 0.31$
	all phase space		$2.93 \pm 0.37 \pm 0.37$
$B^0 \rightarrow \eta \ell^+ \nu$	all phase space		$0.44 \pm 0.23 \pm 0.11$
$B^0 \rightarrow \eta' \ell^+ \nu$	all phase space		$2.66 \pm 0.80 \pm 0.56$

$B \rightarrow \pi l \nu$: untagged method

BaBar 227MBB

Loose neutrino reconstruction



	q^2 (GeV ²)	$\Delta\zeta$ (ps ⁻¹)	$ V_{ub} $ (10 ⁻³)
HPQCD [3]	> 16	1.46 ± 0.35	$4.1 \pm 0.2 \pm 0.2^{+0.6}_{-0.4}$
FNAL [4]	> 16	1.83 ± 0.50	$3.7 \pm 0.2 \pm 0.2^{+0.6}_{-0.4}$
LCSR [5]	< 16	5.44 ± 1.43	$3.6 \pm 0.1 \pm 0.1^{+0.6}_{-0.4}$
ISGW2 [6]	0-26.4	9.6 ± 4.8	$3.2 \pm 0.1 \pm 0.1^{+1.3}_{-0.6}$

Phys. Rev. Lett. 98:091801 (2007)

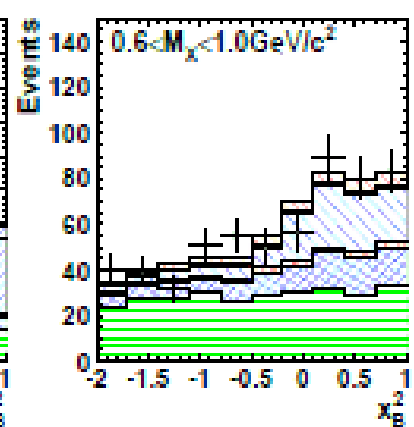
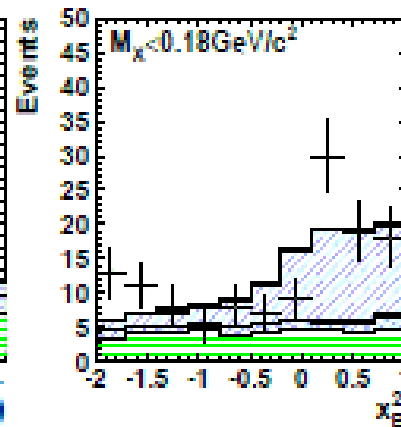
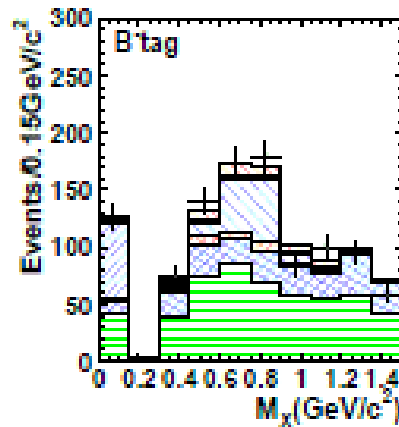
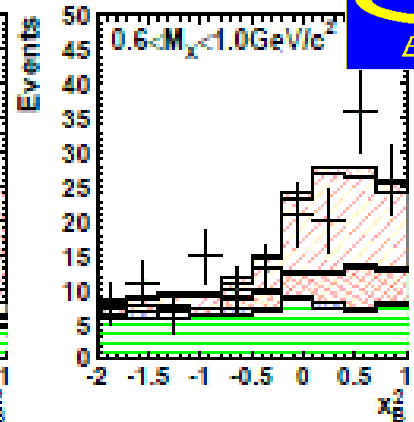
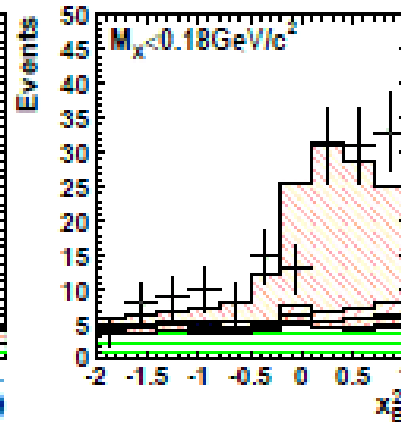
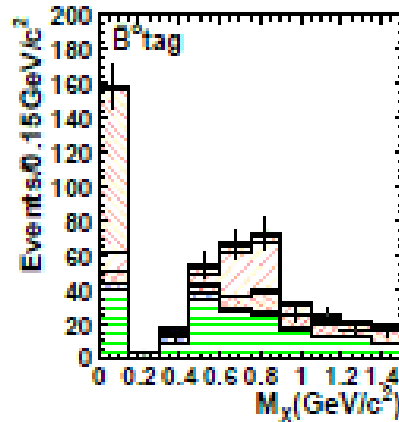
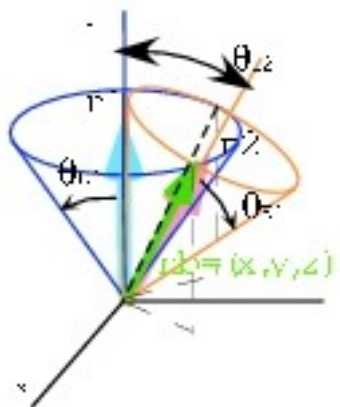
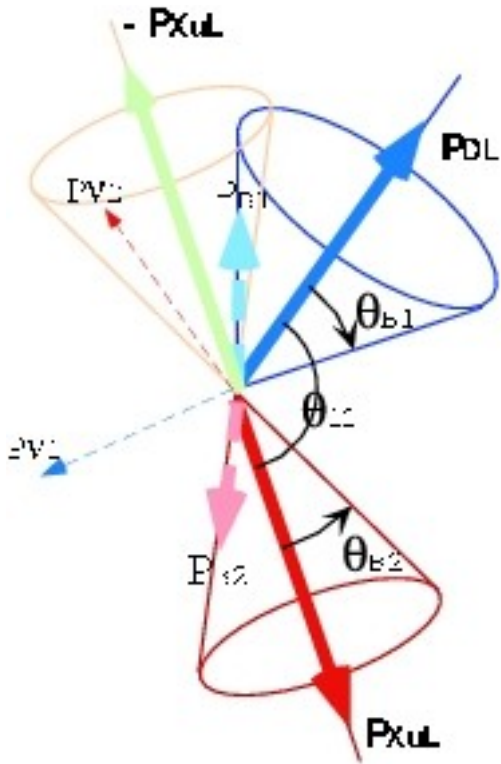
$B \rightarrow \pi l \nu / \rho l \nu$: $D(^*) l \nu$ tag method

- $B \rightarrow D(^*) l \nu$ tag

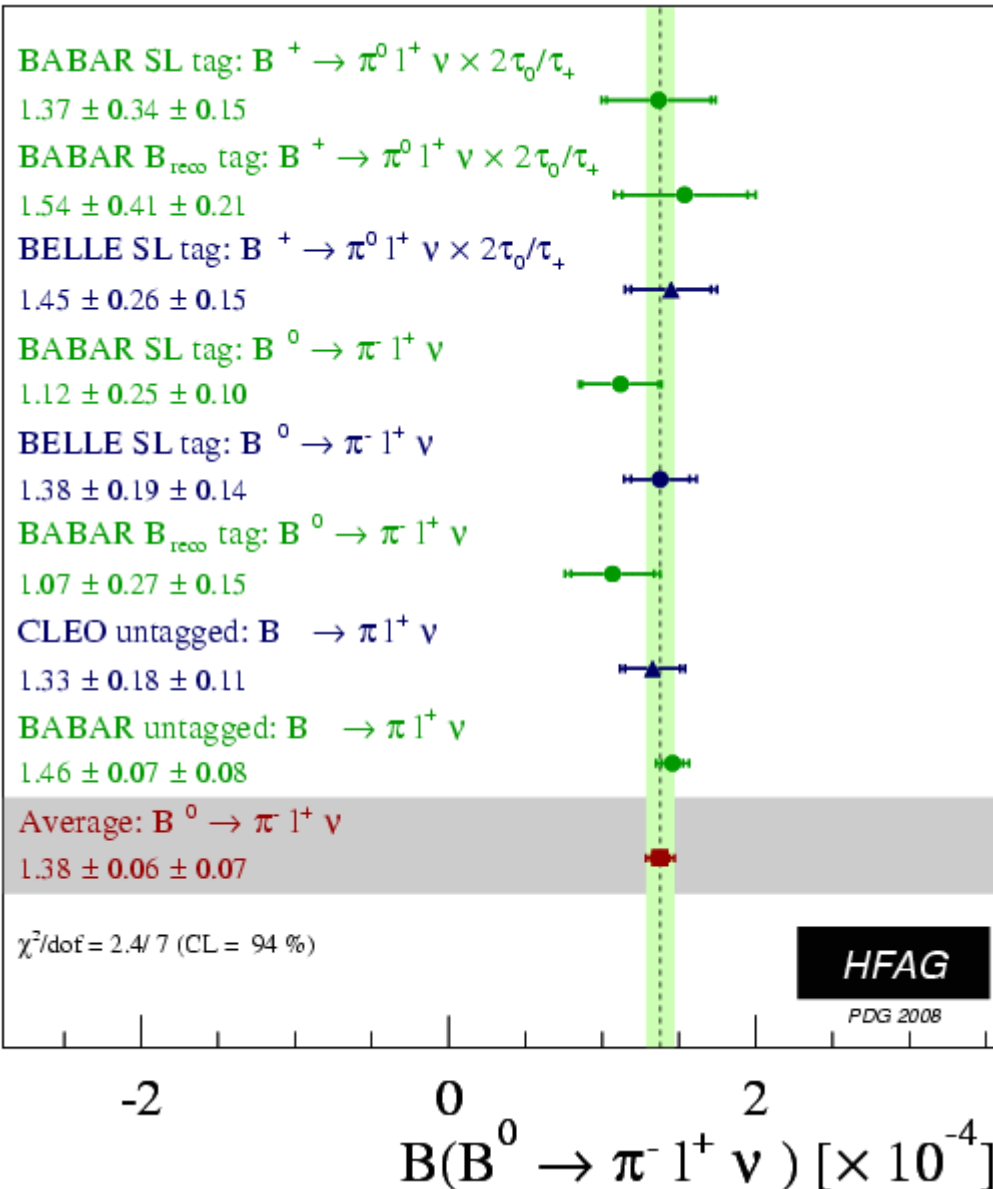
Belle 275MBB

- to handle two neutrinos, use a kinematical variable: x_B^2

$$x_B^2 = 1 - \frac{1}{\sin^2 \theta_{12}^*} (\cos^2 \theta_{B_1}^* + \cos^2 \theta_{B_2}^* - 2 \cos \theta_{B_1}^* \cos \theta_{B_2}^* \cos \theta_{12}^*)$$



$|V_{ub}|$ from $B \rightarrow \pi l \nu$



Many measurements that are not covered in this talk

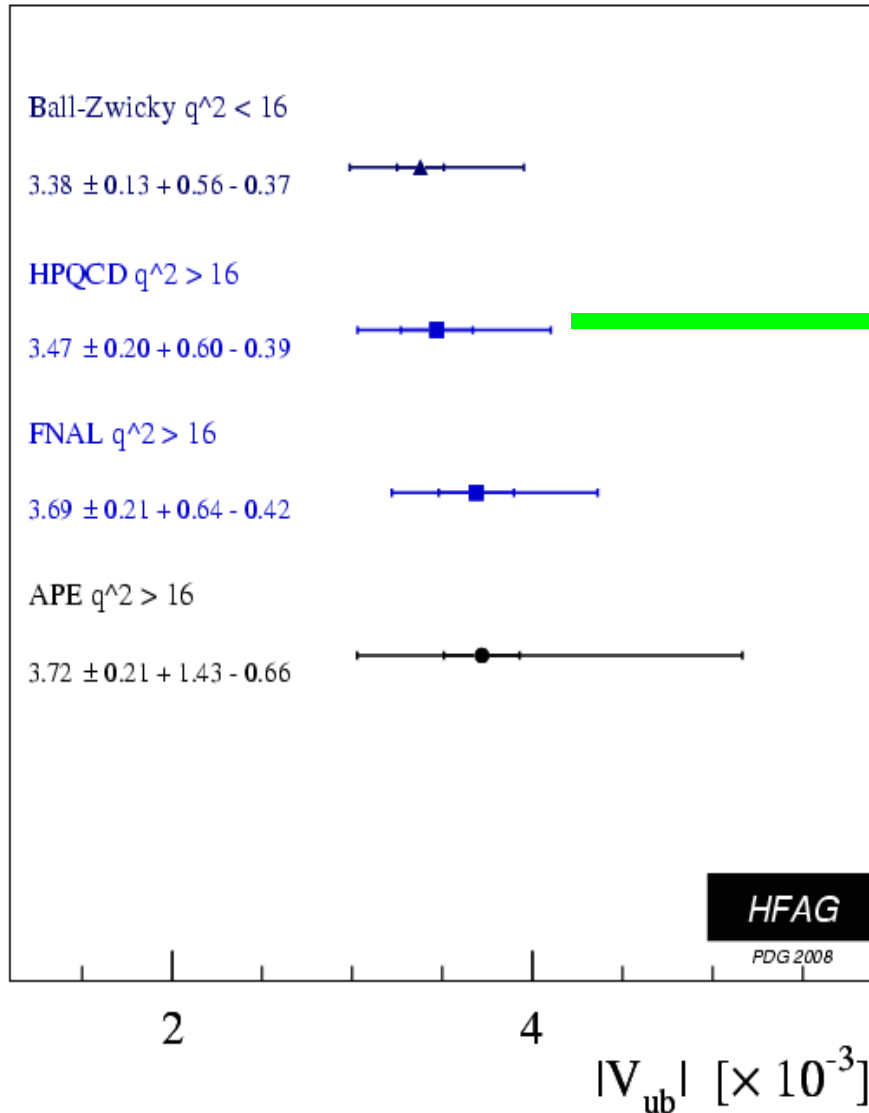
Average

$$B(B^0 \rightarrow \pi^- l^+ \nu) = 1.38 \pm 0.06 \pm 0.07$$

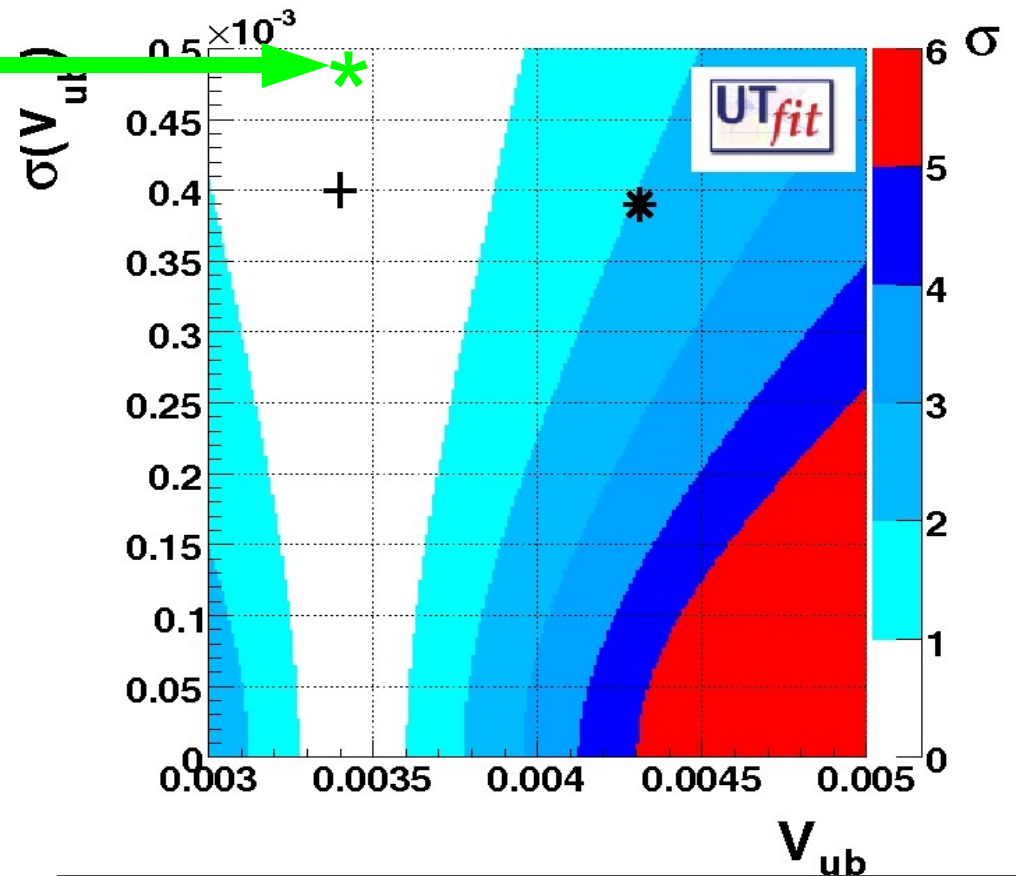
More results will be coming soon:
e.g.

B_{reco} tag analysis from Belle
 SL tag analysis from BaBar

$|V_{ub}|$ from $B \rightarrow \pi l \nu$



Expected $|V_{ub}|$ from global UT fit w/o $|V_{ub}|$



Consistent with global UT fit result

Summary

$|V_{cb}|$ from $B \rightarrow D^* l \nu$:

$$|V_{cb}| = (39.37 \pm 0.60 \pm 1.41) \times 10^{-3}$$

- new measurement w/ form factor parameters
- uncertainty of $F(1)$ is dominant
- $\sim 1.5\sigma$ difference from inclusive $|V_{cb}| = (42.04 \pm 0.34 \pm 0.59) \times 10^{-3}$

Study of D^{**} states in $B \rightarrow D^{**} l \nu$ decay

- Measured branching ratio(s) contradicts the HQET prediction
- need theoretical and experimental effort for understanding

$|V_{ub}|$ from $B \rightarrow \pi l \nu$:

- Many measurements from various techniques
more results will be coming soon
- Progress of the form factor calculation: “unquenched” lattice QCD
 $|V_{ub}| = (3.47 \pm 0.20 + 0.60 - 0.39) \times 10^{-3}$ (HPQCD, $q^2 > 16 \text{ GeV}^2$)

backup

D**lv analysis

D π invariant mass is fitted in bins of helicity and w

