

CP Violation in the Neutrino Sector

FPCP 2008:

Stephen Parke
Fermilab

$$|\nu_e, \nu_\mu, \nu_\tau\rangle_{flavor}^T = U_{\alpha i} |\nu_1, \nu_2, \nu_3\rangle_{mass}^T$$

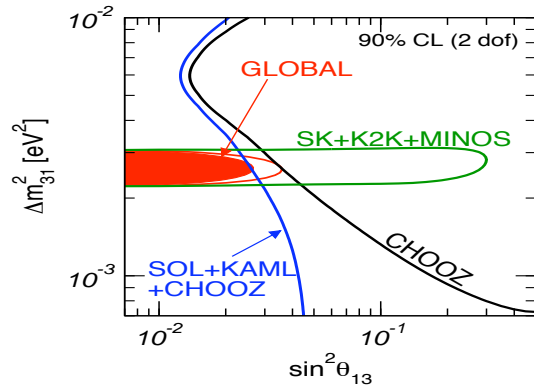
$$U_{\alpha i} = \begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & & s_{13}e^{-i\delta} \\ & 1 & \\ -s_{13}e^{i\delta} & & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} \\ -s_{12} & c_{12} \\ & & 1 \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{i\alpha} & \\ & & e^{i\beta} \end{pmatrix}$$

Atmos. L/E $\mu \rightarrow \tau$ Atmos. L/E $\mu \leftrightarrow e$ Solar L/E $e \rightarrow \mu, \tau$ $0\nu\beta\beta$ decay

500km/GeV

15km/MeV

$$\sin^2 \theta_{13} < 0.03$$



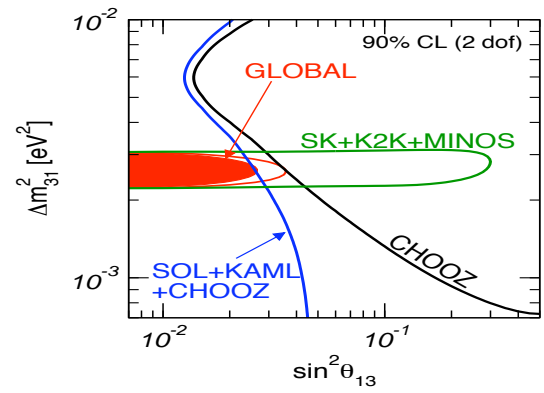
Maltoni et al hep-ph/0405172v5

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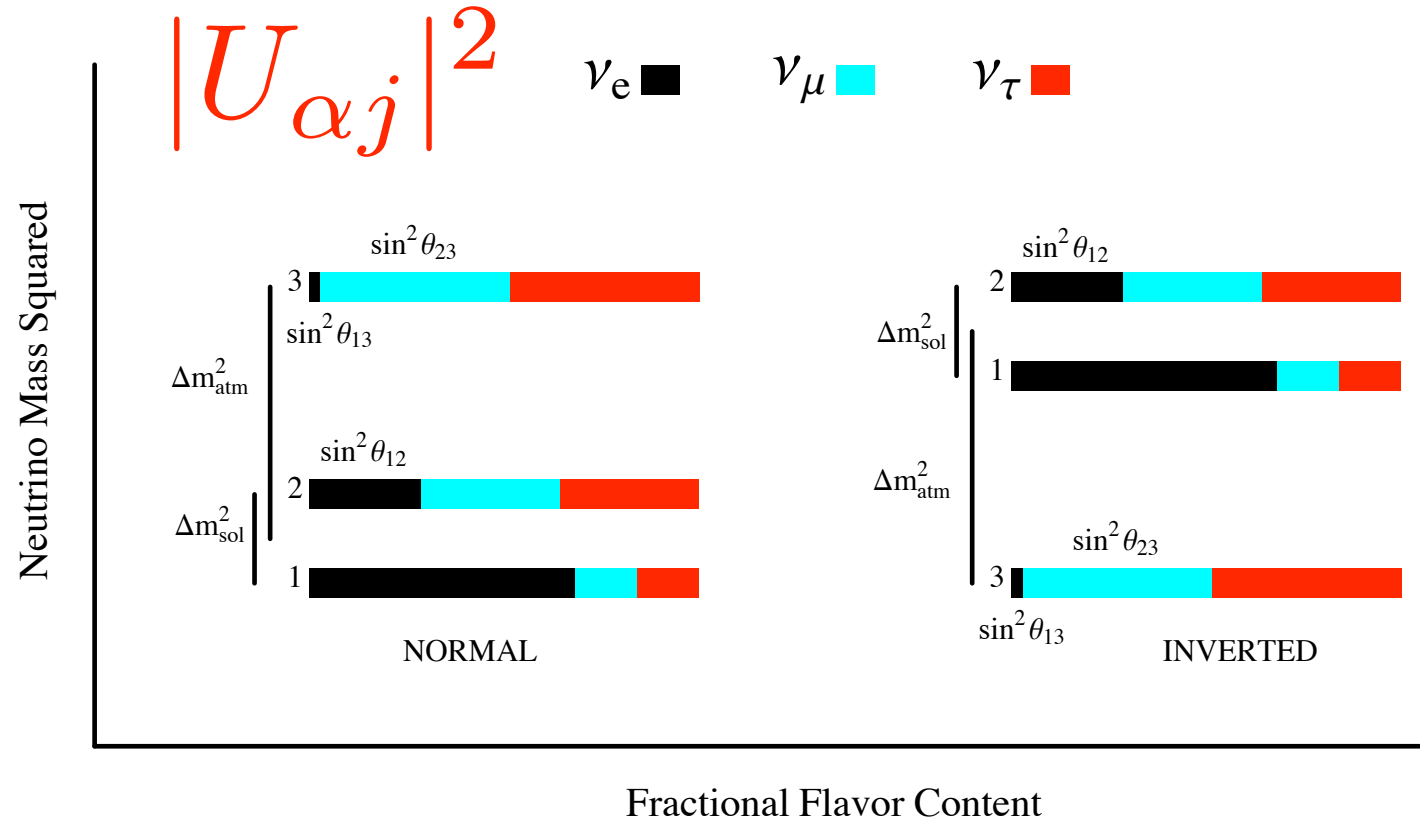
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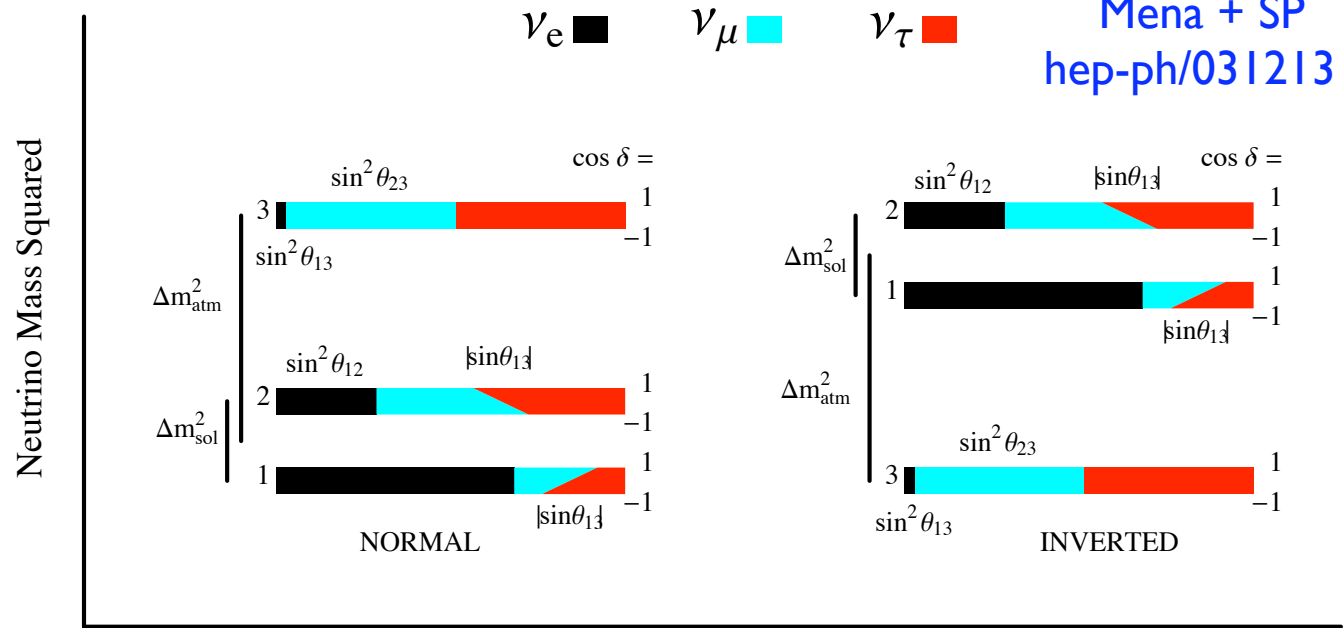
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Maltoni et al hep-ph/0405172v5



Sine/Signs

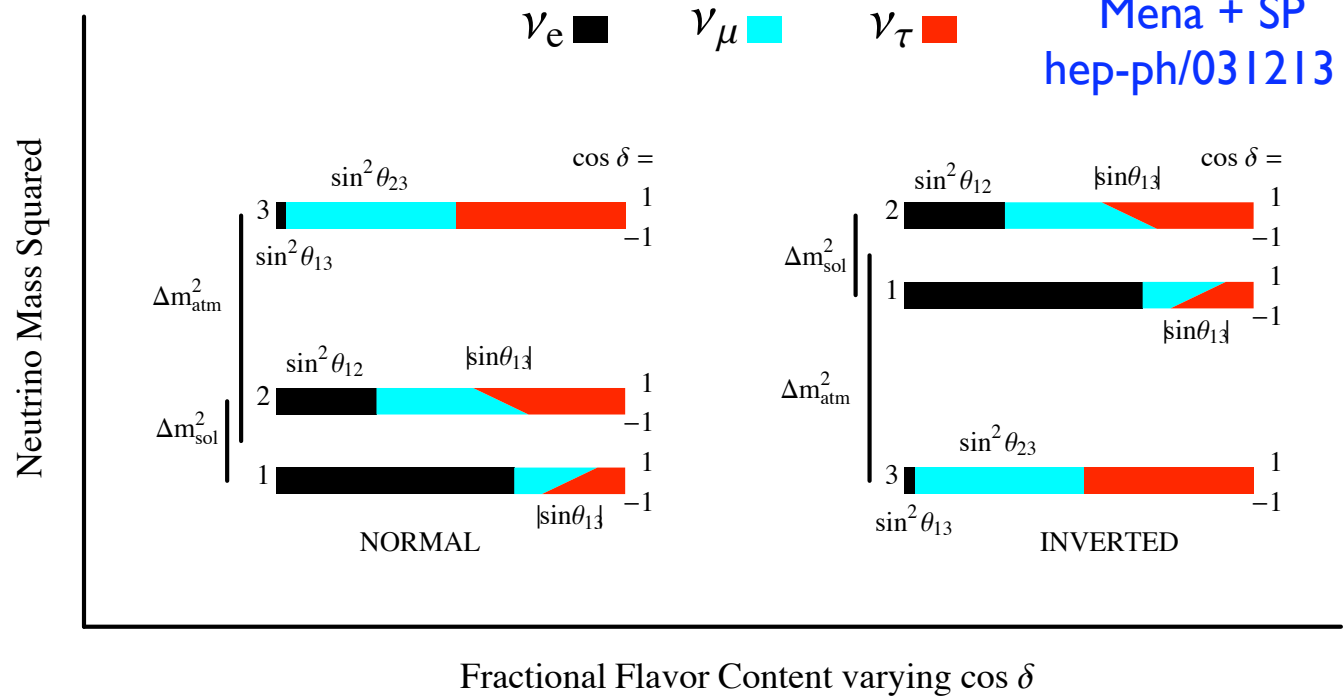


Fractional Flavor Content varying $\cos \delta$

States 1 and 2 are ν_e rich.

CPT: $\delta \Leftrightarrow -\delta$ Invariant!

Sine/Signs



- $|U_{e3}|^2: \sin^2 \theta_{13}$
- Hierarchy: $sign(\delta m_{31}^2 \text{ or } \delta m_{32}^2)$
- CPV: $\sin \delta$
- Maximal Mixing: $\sin^2 \theta_{23} = \frac{1}{2}$
- Quadrant of δ : $\cos \delta = \pm \sqrt{1 - \sin^2 \delta}$
- Unitarity: lite sterile ν 's
- New Interactions and Surprises

States 1 and 2 are ν_e rich.

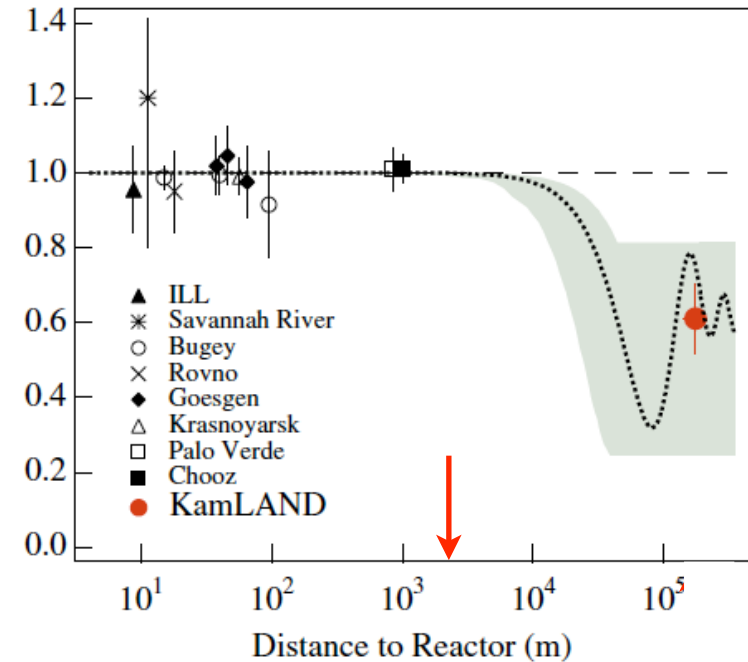
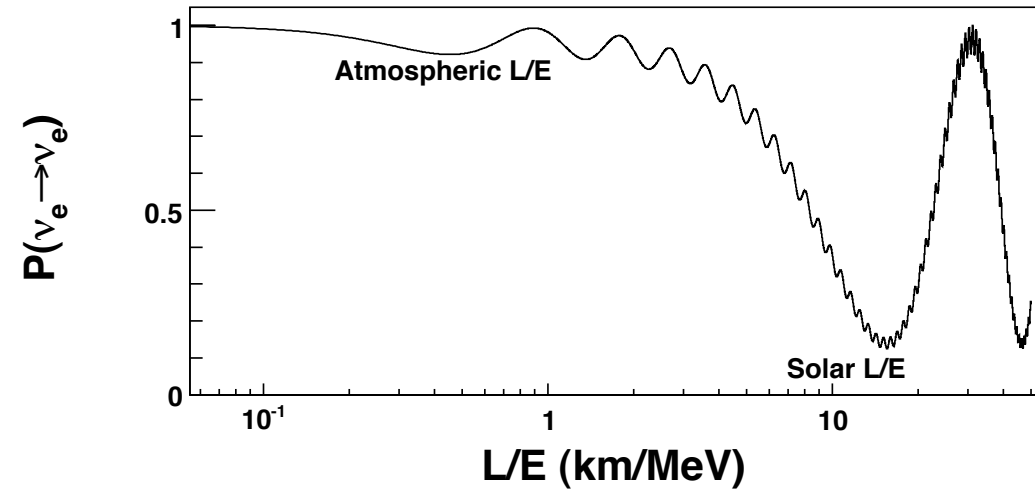
CPT: $\delta \Leftrightarrow -\delta$ Invariant!

θ_{13} from Reactor Disappearance

kinematic phase:

$$\Delta_{ij} \equiv \frac{\delta m_{ij}^2 L}{4E}$$

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$



$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \approx 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\delta m_{ee}^2 L}{4E} \right) - \mathcal{O}(\Delta_{21})^2 < 0.002$$

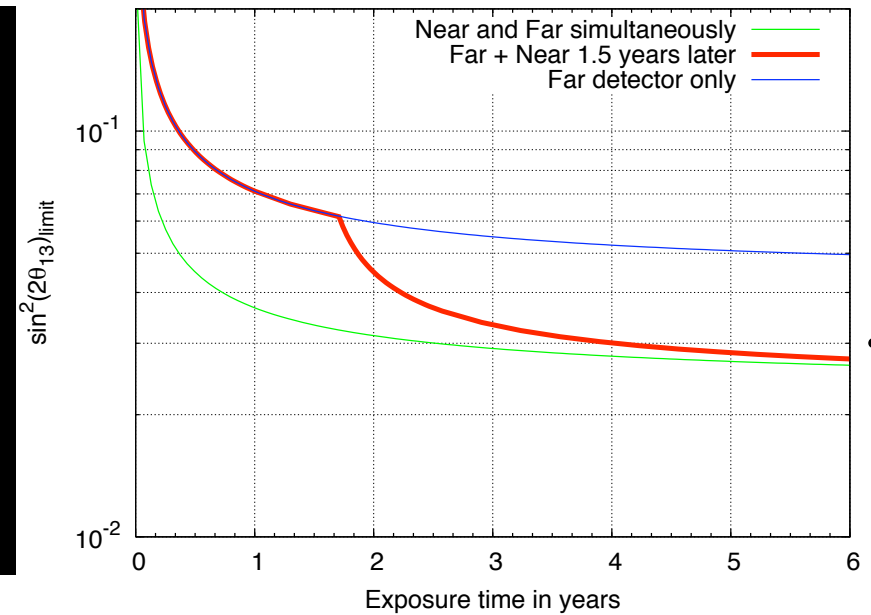
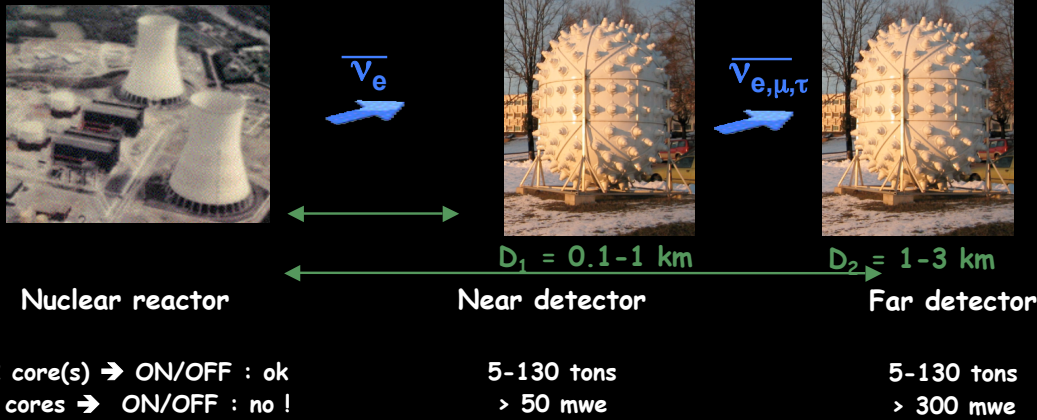
> 0.01

$$\delta m_{ee}^2 = \cos^2 \theta_{12} |\delta m_{31}^2| + \sin^2 \theta_{12} |\delta m_{32}^2|$$

Double Chooz:



One nuclear plant & two detectors



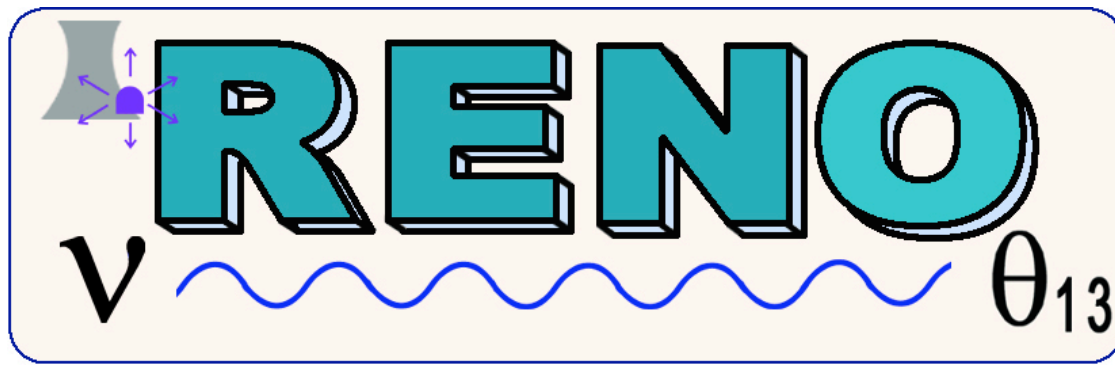
.03

Figure 18: $\sin^2(2\theta_{13})$ sensitivity limit for the detectors installation scheduled scenario

Daya Bay



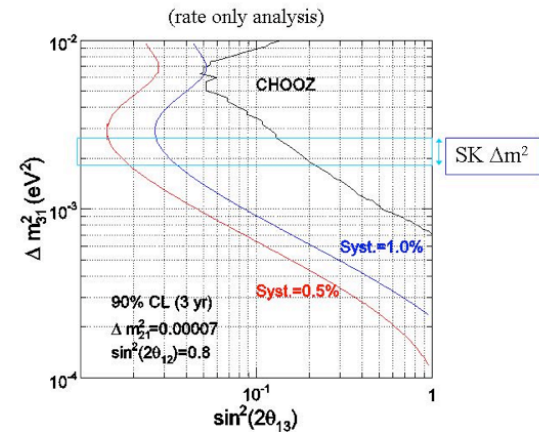
push the limit on
 $\sin^2 2\theta_{13} < 0.01$



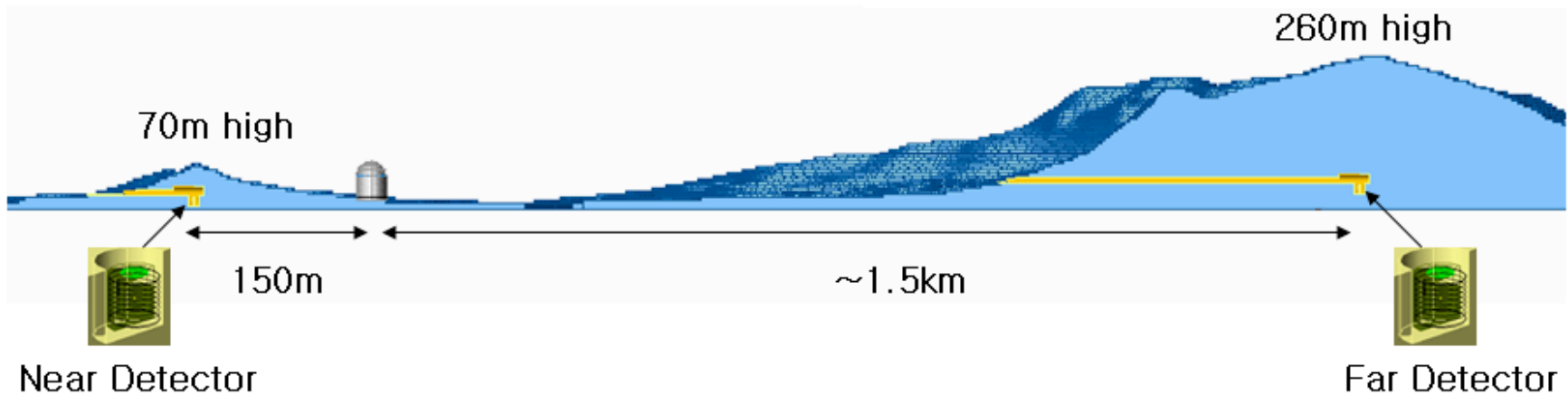
(Reactor Experiment for Neutrino Oscillation)



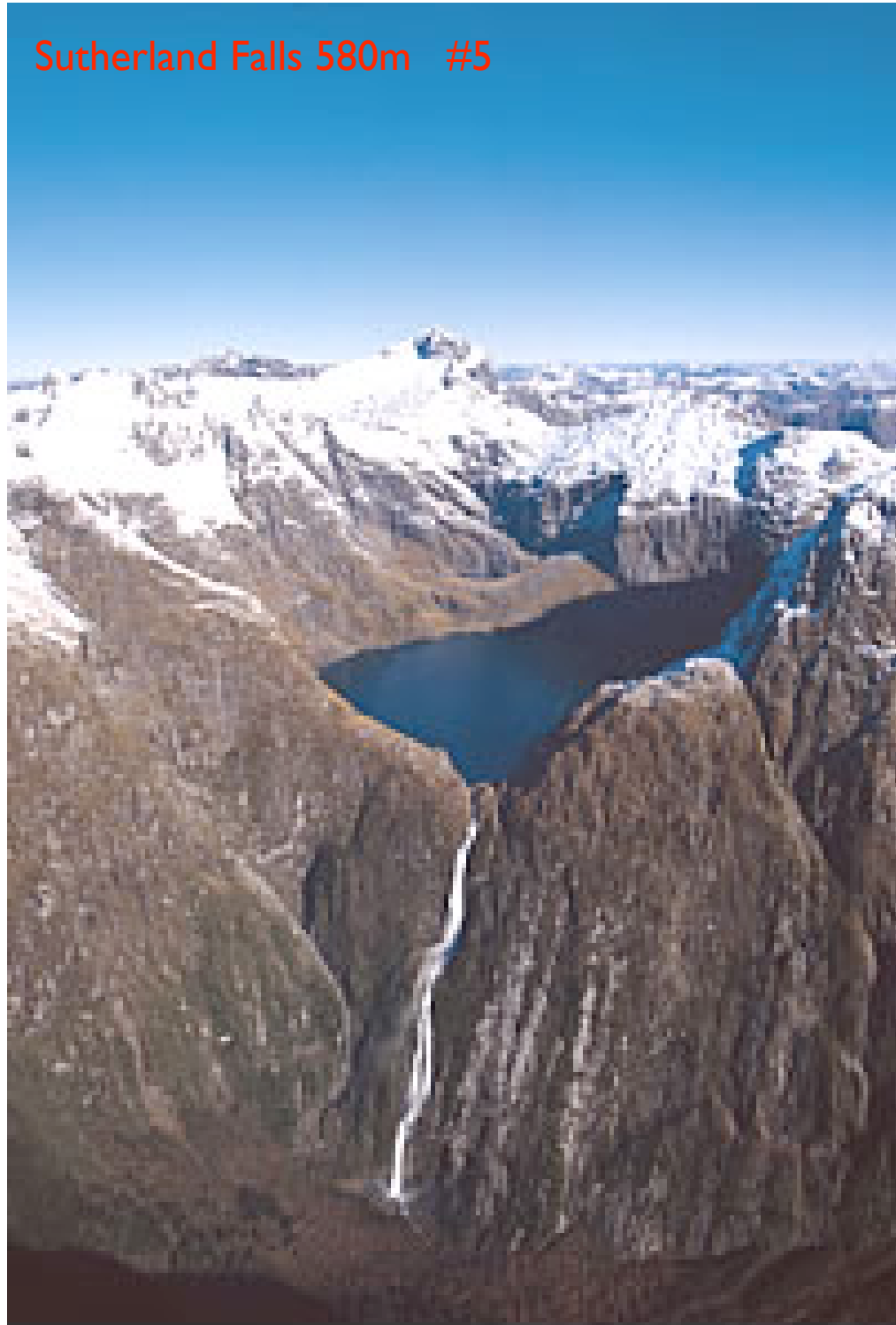
RENO Expected Sensitivity



10x better sensitivity than current limit



Sutherland Falls 580m #5

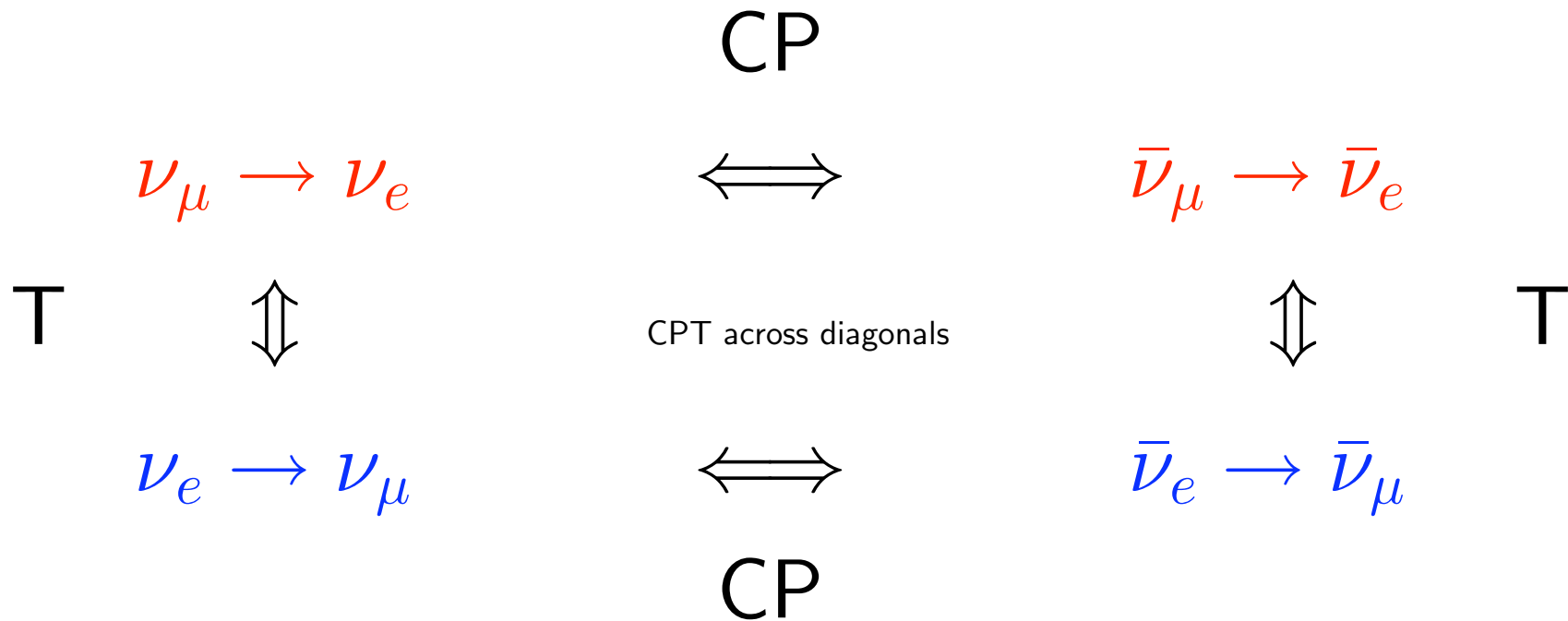


Sutherland Falls 580m #5



$$\nu_{\mu} \longrightarrow \nu_e$$

and related processes:



- First Row: Superbeams where ν_e contamination $\sim 1\%$
- Second Row: ν -Factory or β -Beams, no beam contamination

$$\mathcal{V}_\mu \rightarrow \mathcal{V}_e$$

$$\left| U_{\mu 3}^* e^{-im_3^2 L/2E} U_{e3} + U_{\mu 2}^* e^{-im_2^2 L/2E} U_{e2} + U_{\mu 1}^* e^{-im_1^2 L/2E} U_{e1} \right|^2$$

$$\nu_\mu \longrightarrow \nu_e$$

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use unitarity to eliminate $U_{\mu 1}^* U_{e1}$ term:

$$P(\nu_\mu \longrightarrow \nu_e) = \left| 2U_{\mu 3}^* U_{e3} \sin \Delta_{31} e^{-i\Delta_{32}} + 2U_{\mu 2}^* U_{e2} \sin \Delta_{21} \right|^2$$

$$\nu_\mu \longrightarrow \nu_e$$

$$\left| U_{\mu 3}^* e^{-im_3^2 L/2E} U_{e3} + U_{\mu 2}^* e^{-im_2^2 L/2E} U_{e2} + U_{\mu 1}^* e^{-im_1^2 L/2E} U_{e1} \right|^2$$

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Atmospheric δm^2

Solar δm^2

Vacuum LBL:

$$\nu_{\mu} \longrightarrow \nu_e$$

$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

$$\Delta_{ij} = \delta m_{ij}^2 L / 4E$$

CP violation !!!

where $\sqrt{P_{atm}} = \sin \theta_{23} \sin 2\theta_{13} \sin \Delta_{31}$

and $\sqrt{P_{sol}} = \cos \theta_{23} \sin 2\theta_{12} \sin \Delta_{21}$

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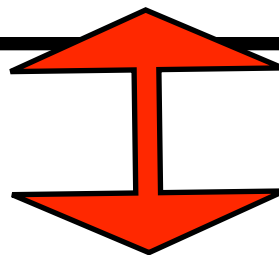
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and $\sqrt{P_{sol}} = \cos \theta_{23} \sin 2\theta_{12} \sin \Delta_{21}$

$$P_{\mu \rightarrow e} \approx P_{atm} + 2\sqrt{P_{atm}P_{sol}} \cos(\Delta_{32} \pm \delta) + P_{sol}$$

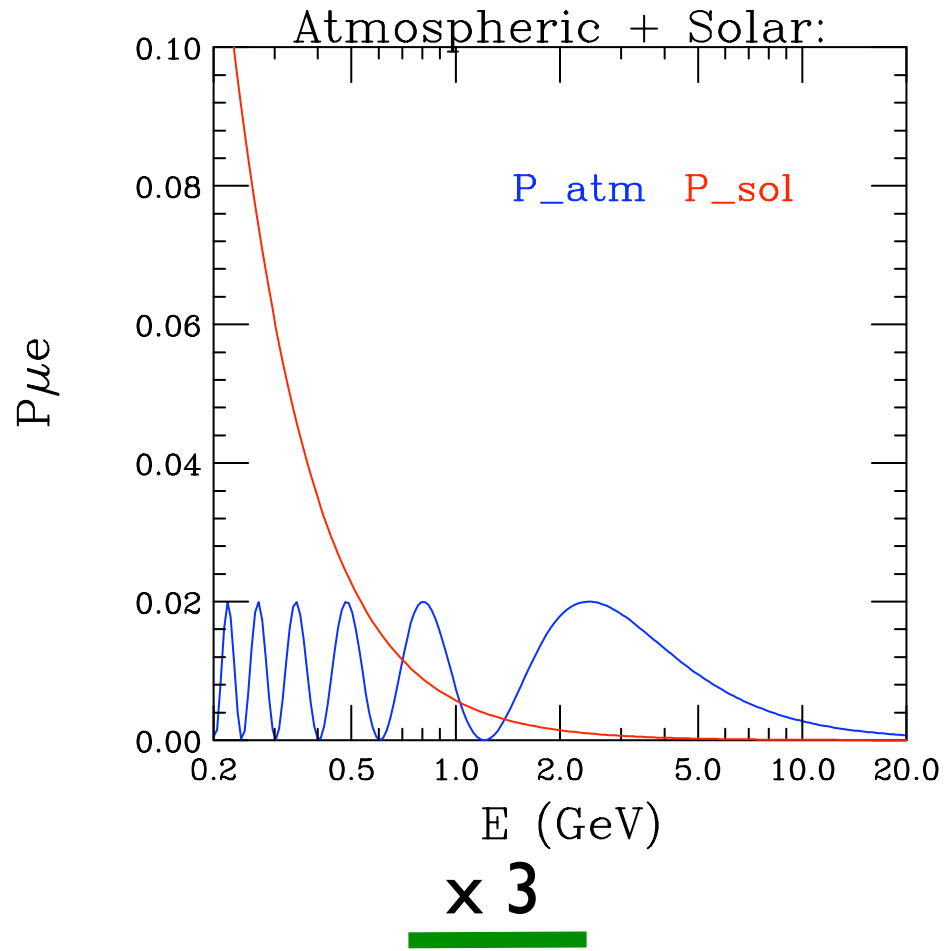


only CPV

$$\cos(\Delta_{32} \pm \delta) = \cos \Delta_{32} \cos \delta \mp \sin \Delta_{32} \sin \delta$$

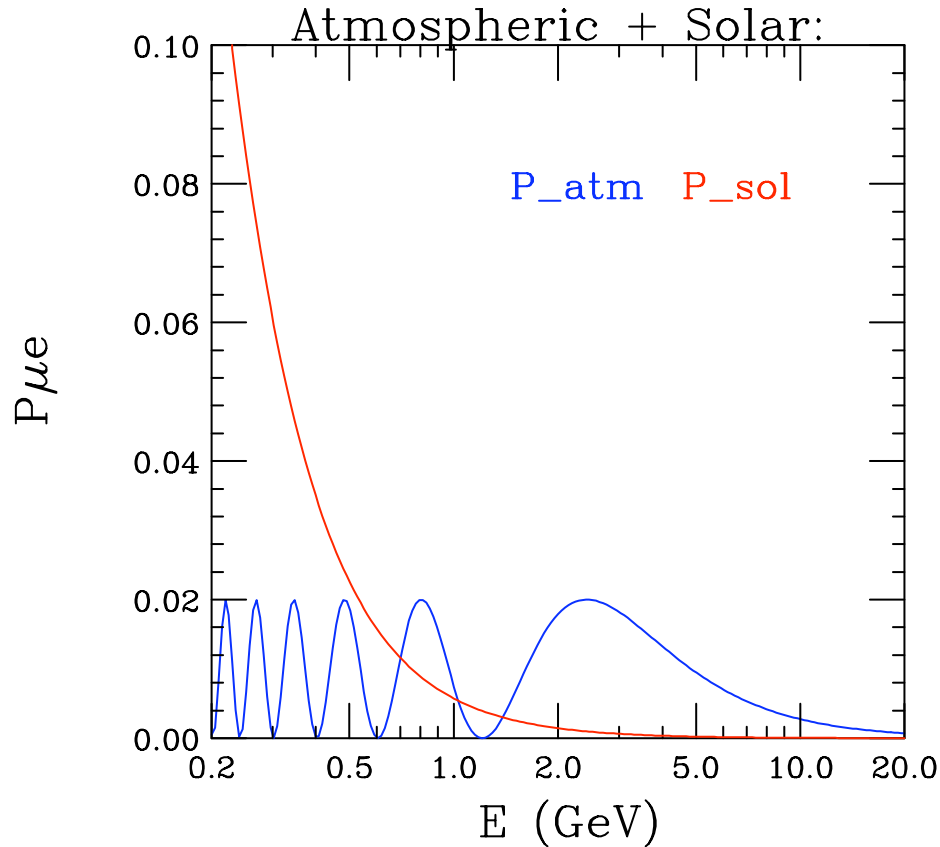
$$P(\nu_\mu \rightarrow \nu_e) \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} + \delta)} + \sqrt{P_{sol}} \right|^2$$

For $L = 1200 \text{ km}$
and $\sin^2 2\theta_{13} = 0.04$

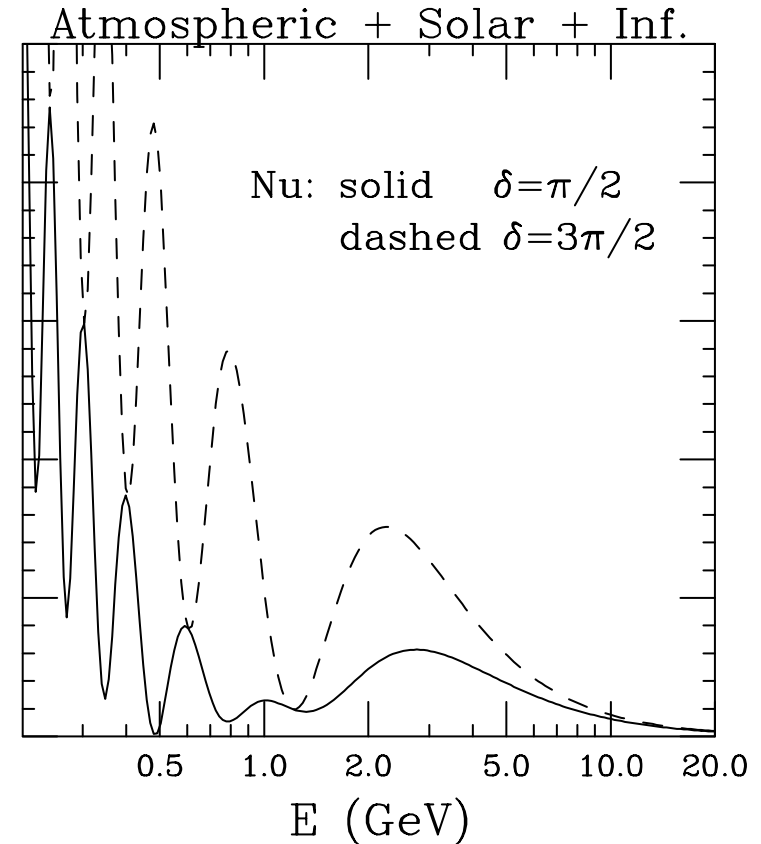


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x 3

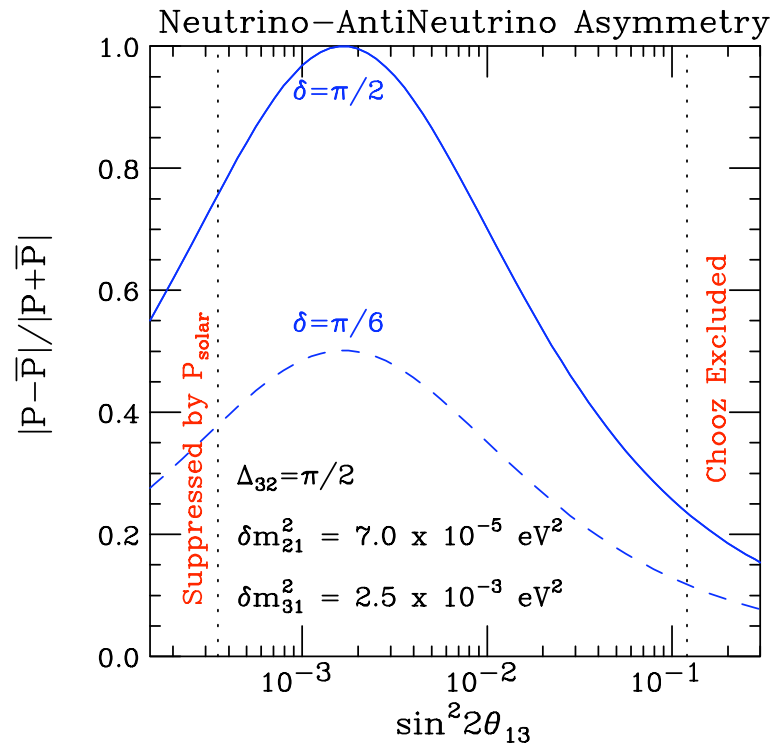


phase varies



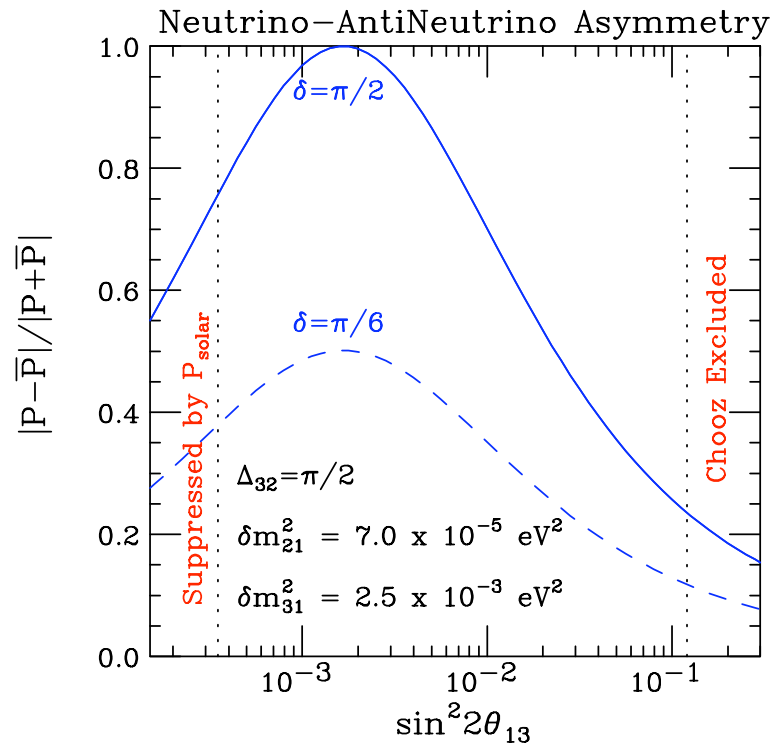
$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

Asymmetry Peaks:



$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

Asymmetry Peaks:



$$P_{atm} \leq P_{sol} \quad \text{when} \quad \sin^2 2\theta_{13} \leq \frac{\sin^2 2\theta_{12}}{\tan^2 \theta_{23}} \left(\frac{\delta m_{21}^2}{\delta m_{31}^2} \right)^2 \approx 0.001$$

In Matter:

$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

where $\sqrt{P_{atm}} = \sin \theta_{23} \sin 2\theta_{13} \frac{\sin(\Delta_{31} \mp aL)}{(\Delta_{31} \mp aL)} \Delta_{31}$

and $\sqrt{P_{sol}} = \cos \theta_{23} \sin 2\theta_{12} \frac{\sin(aL)}{(aL)} \Delta_{21}$

$$a = G_F N_e / \sqrt{2} = (4000 \text{ km})^{-1},$$

In Matter:

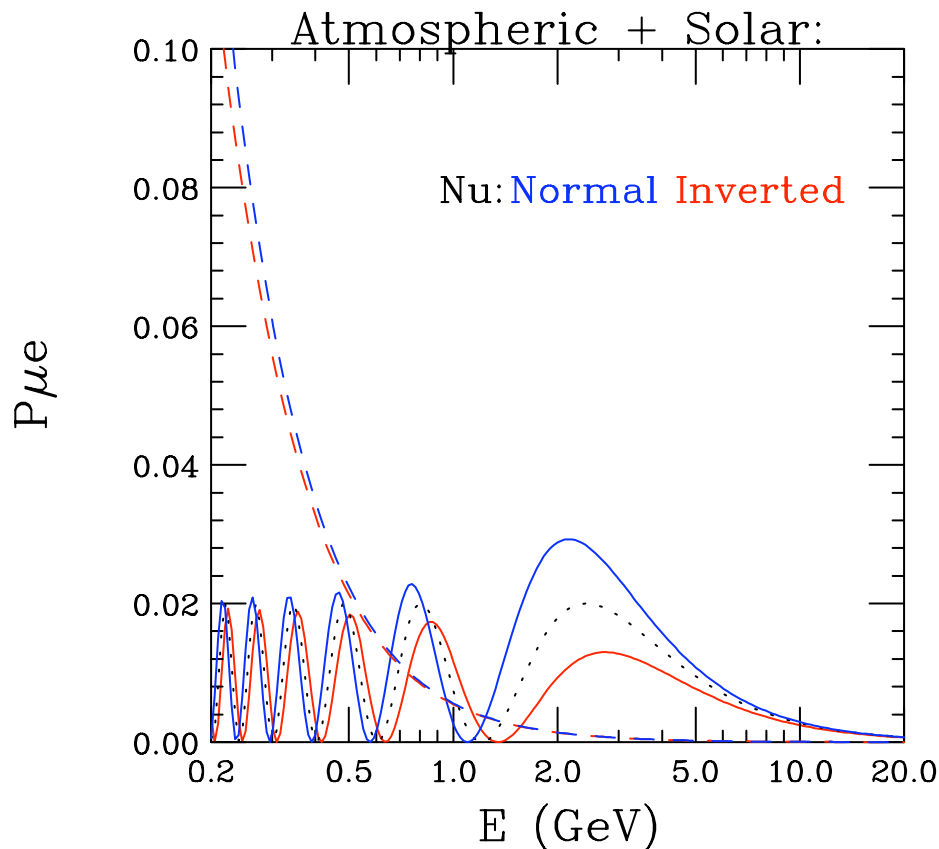
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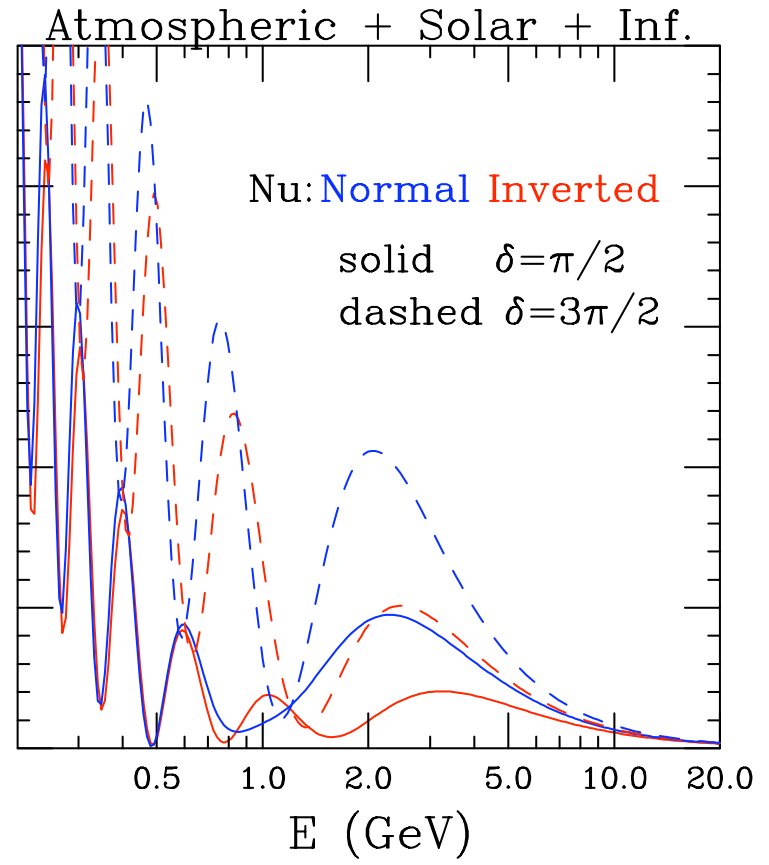
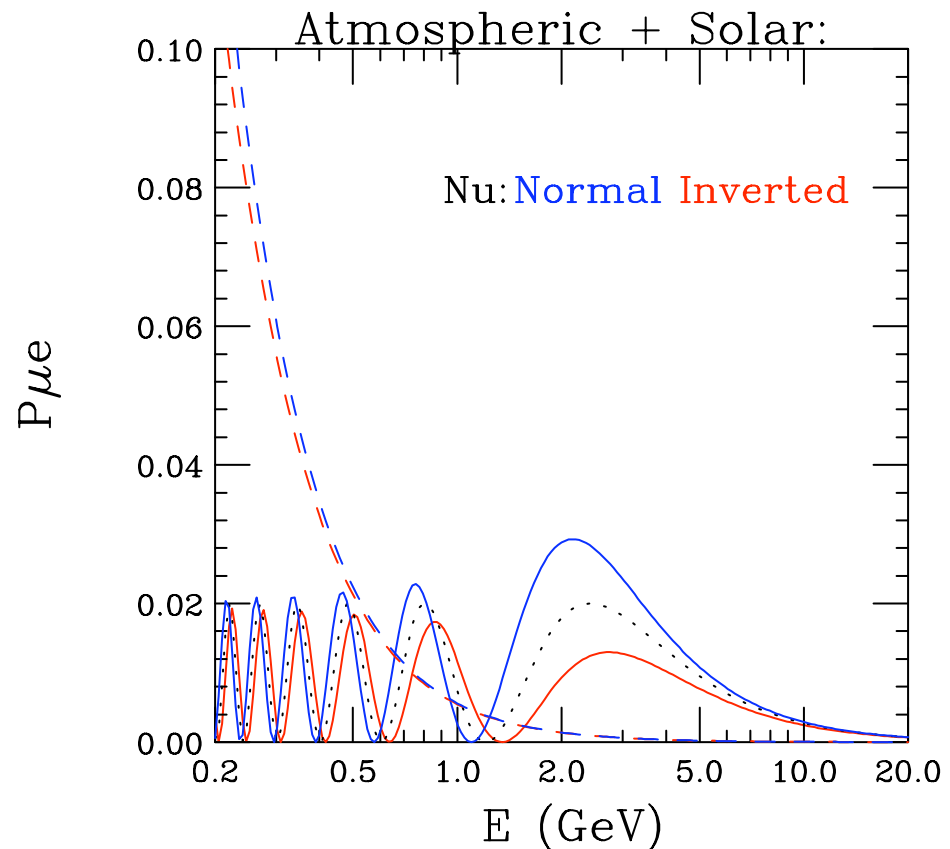
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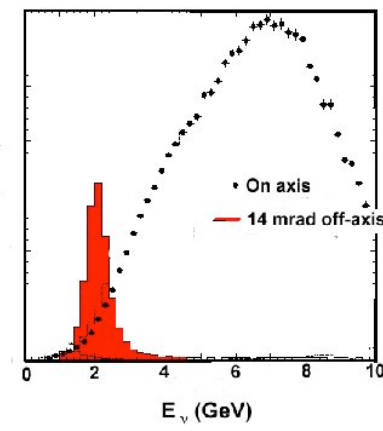
$$a = G_F N_e / \sqrt{2} = (4000 \text{ km})^{-1},$$

Anti-Nu: Normal Inverted
dashes $\delta = \pi/2$
solid $\delta = 3\pi/2$



Off-Axis Beams

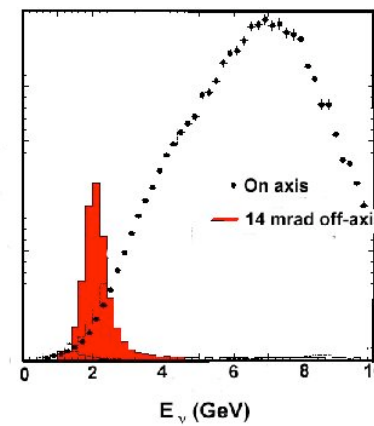
BNL 1994



π^0 suppression

Off-Axis Beams

BNL 1994



π^0 suppression

T2K

JHF \rightarrow Super-Kamiokande

- 295 km baseline
- Super-Kamiokande:
 - 22.5 kton fiducial
 - Excellent e/μ ID
 - Additional π^0/e ID
- Hyper-Kamiokande
 - 20 \times fiducial mass of SuperK
- Matter effects small
- Study using fully simulated and reconstructed data



$L=295$ km and

Energy at Vac. Osc. Max. (vom)

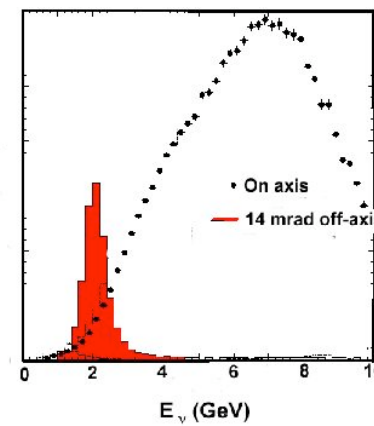
$$E_{vom} = 0.6 \text{ GeV} \left\{ \frac{\delta m_{32}^2}{2.5 \times 10^{-3} \text{ eV}^2} \right\}$$

0.75 upgrade to 4 MW

Off-Axis Beams

BNL 1994

π^0 suppression



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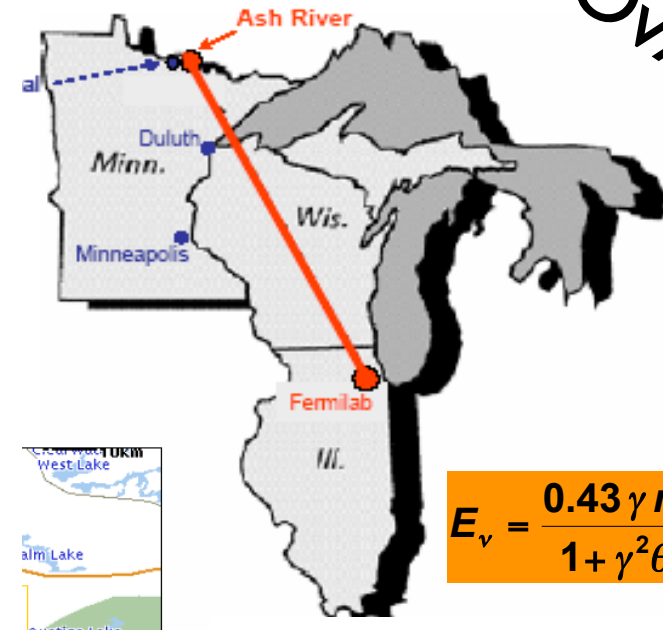
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Energy at Vac. Osc. Max. (vom)

$$E_{vom} = 0.6 \text{ GeV} \left\{ \frac{\delta m_{32}^2}{2.5 \times 10^{-3} \text{ eV}^2} \right\}$$

0.75 upgrade to 4 MW

NOVA



$$E_\nu = \frac{0.43 \gamma m_\pi}{1 + \gamma^2 \theta^2}$$

L=700 - 1000 km and

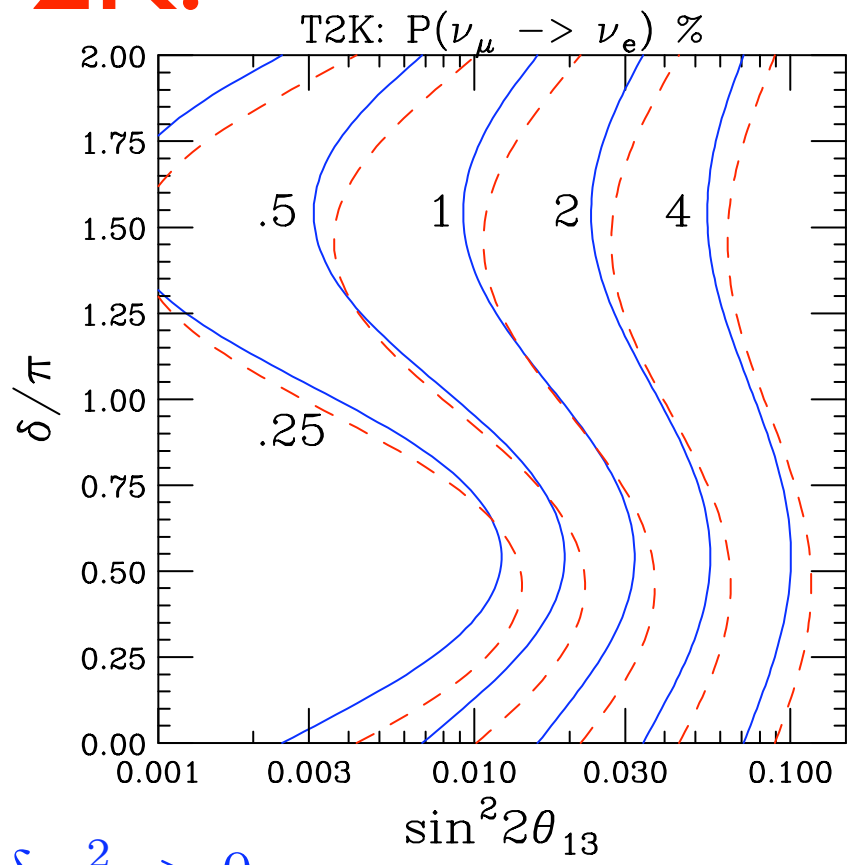
Energy near 2 GeV

$$E_{vom} = 1.8 \text{ GeV} \left\{ \frac{\delta m_{32}^2}{2.5 \times 10^{-3} \text{ eV}^2} \right\} \times \left\{ \frac{L}{820 \text{ km}} \right\}$$

0.4 upgrade to 2 MW

Sensitivity to $\sin^2 2\theta_{13}$

T2K:

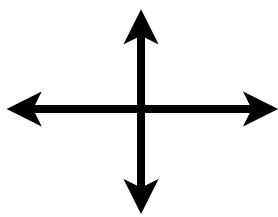


$\delta m_{31}^2 > 0$

$\delta m_{31}^2 < 0$

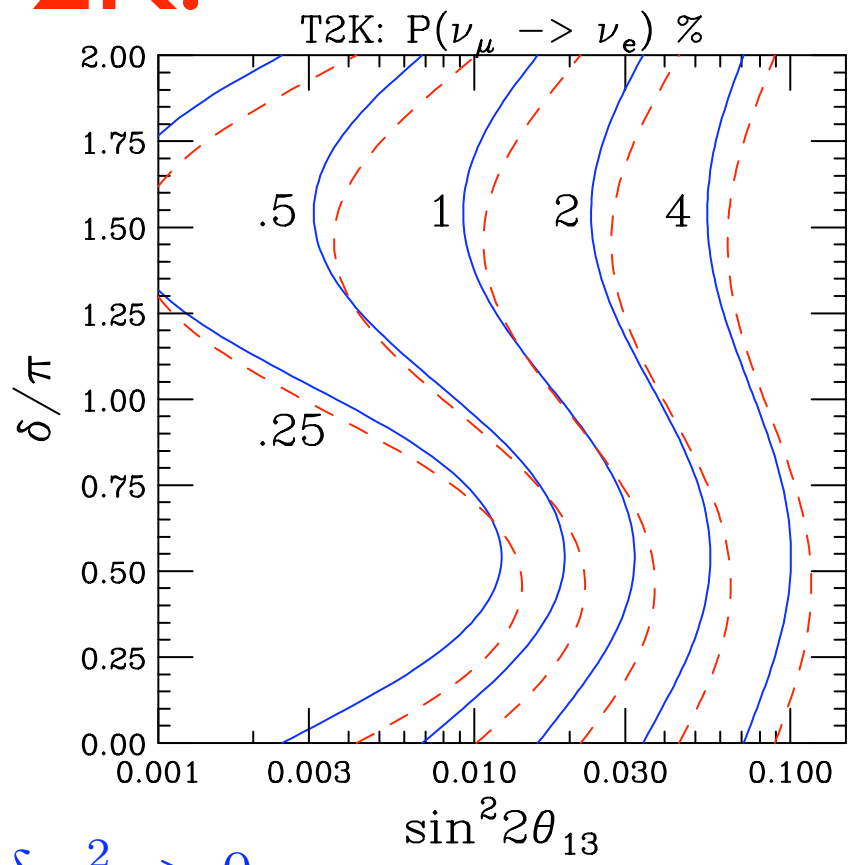
Beam 1%

VOM: $\Delta_{31} \neq \pi/2$



Matter Effect:

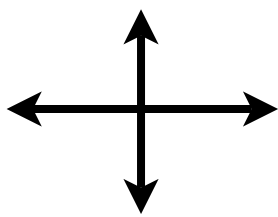
T2K:



$\delta m_{31}^2 > 0$
 $\delta m_{31}^2 < 0$

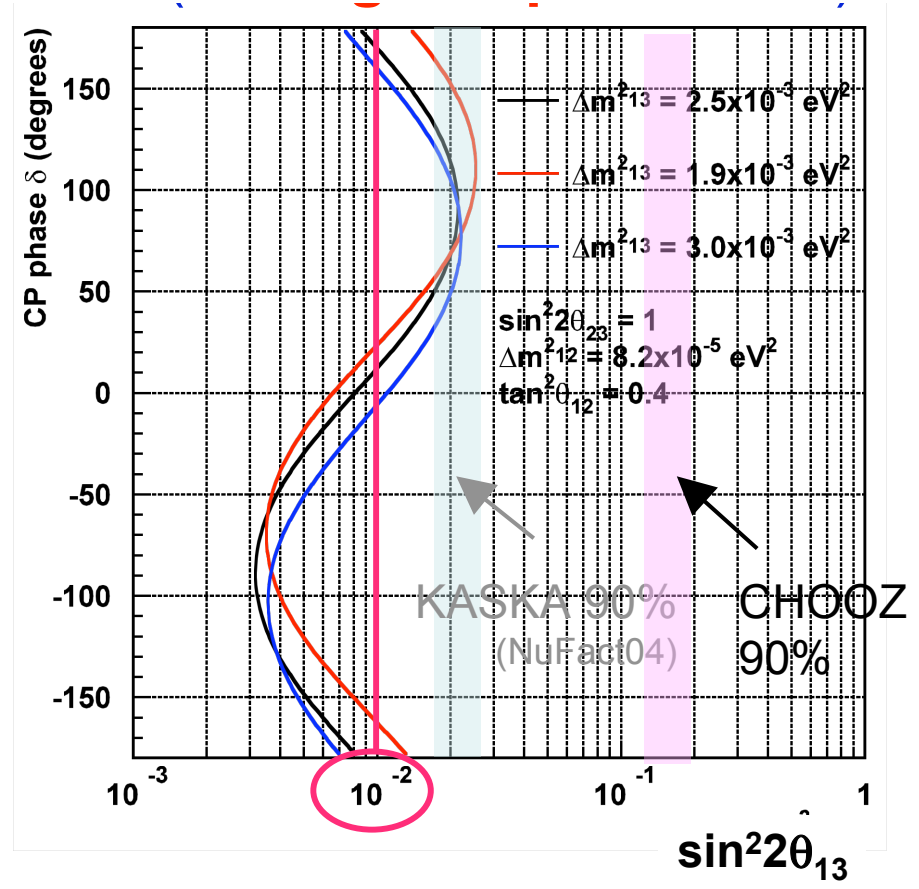
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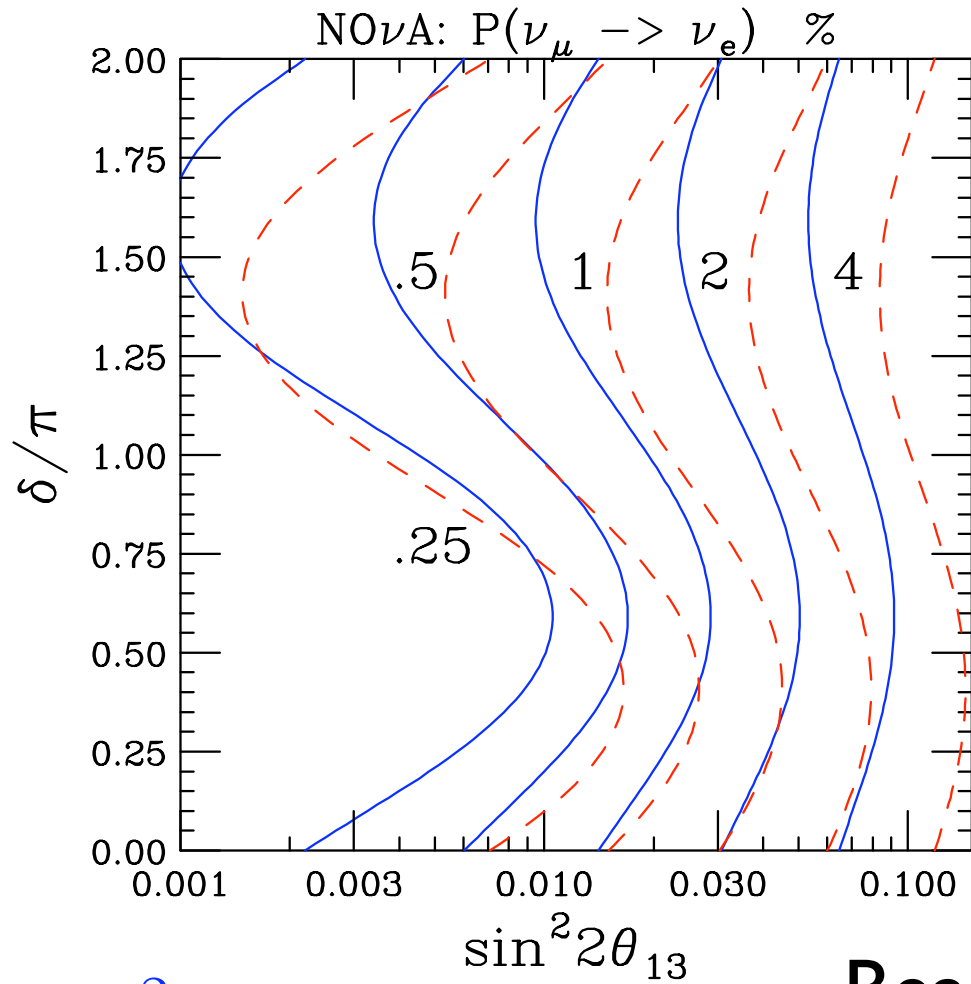
Aihara for T2K, P5 talk



Phase I

Sensitivity approx 0.5%

NO ν A:



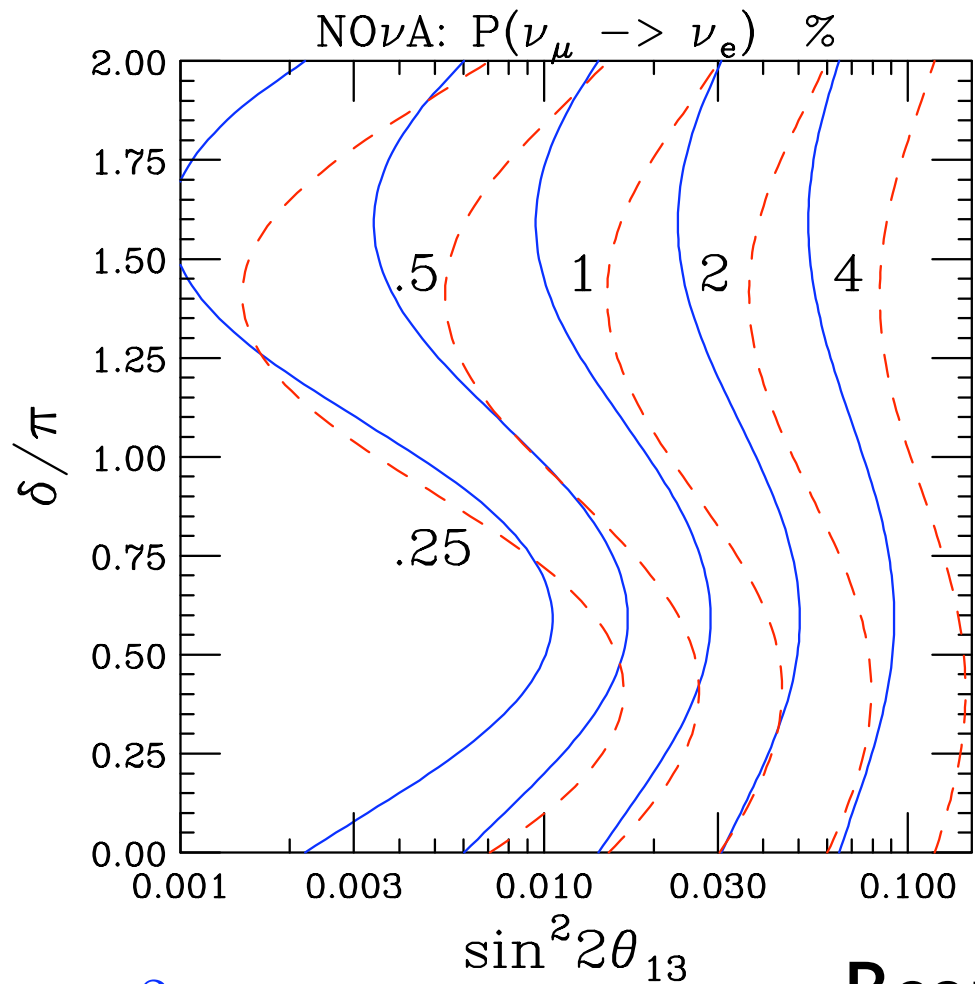
$$\delta m_{31}^2 > 0$$

$$\delta m_{31}^2 < 0$$

Beam 1%

NOvA:

NOvA @ NO-VE 2007



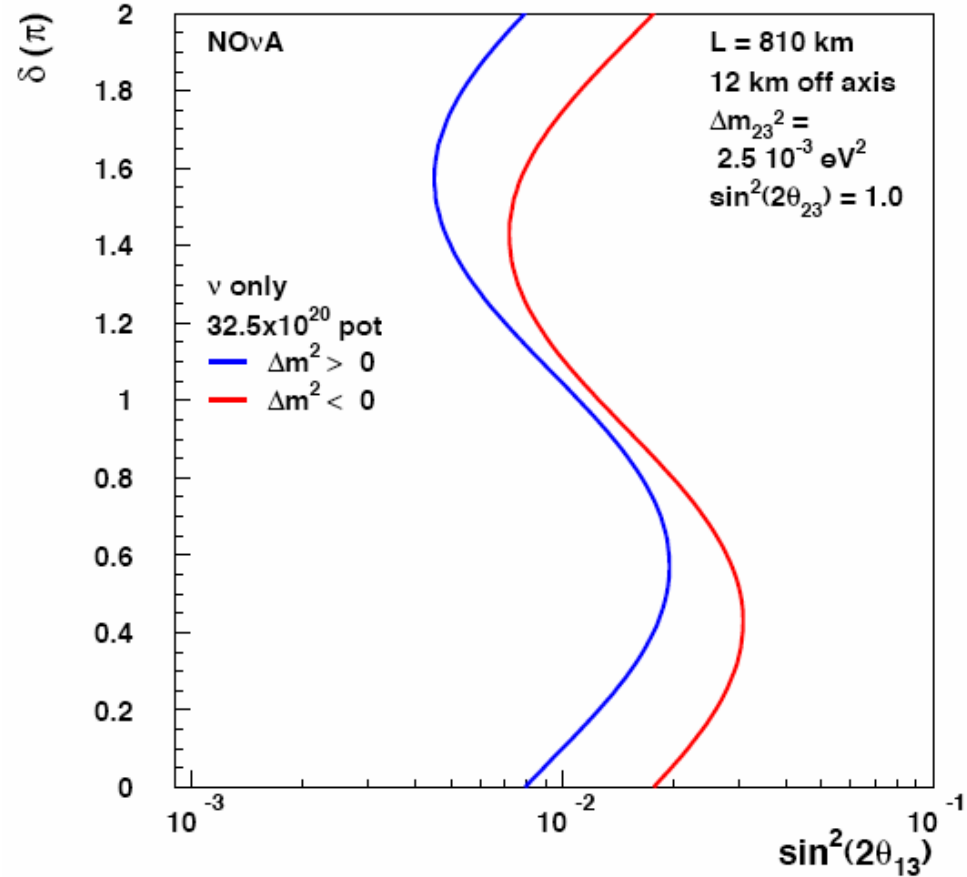
Beam 1%

$$\delta m_{31}^2 > 0$$

$$\delta m_{31}^2 < 0$$

Phase I

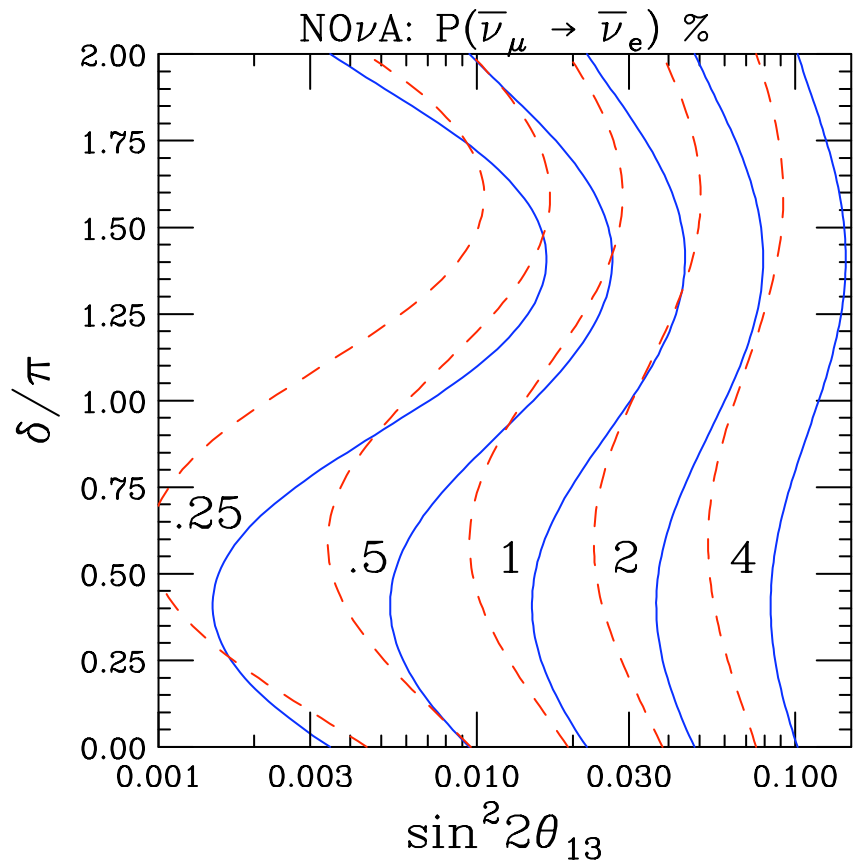
Sensitivity approx 0.5%



5 years with ν only run

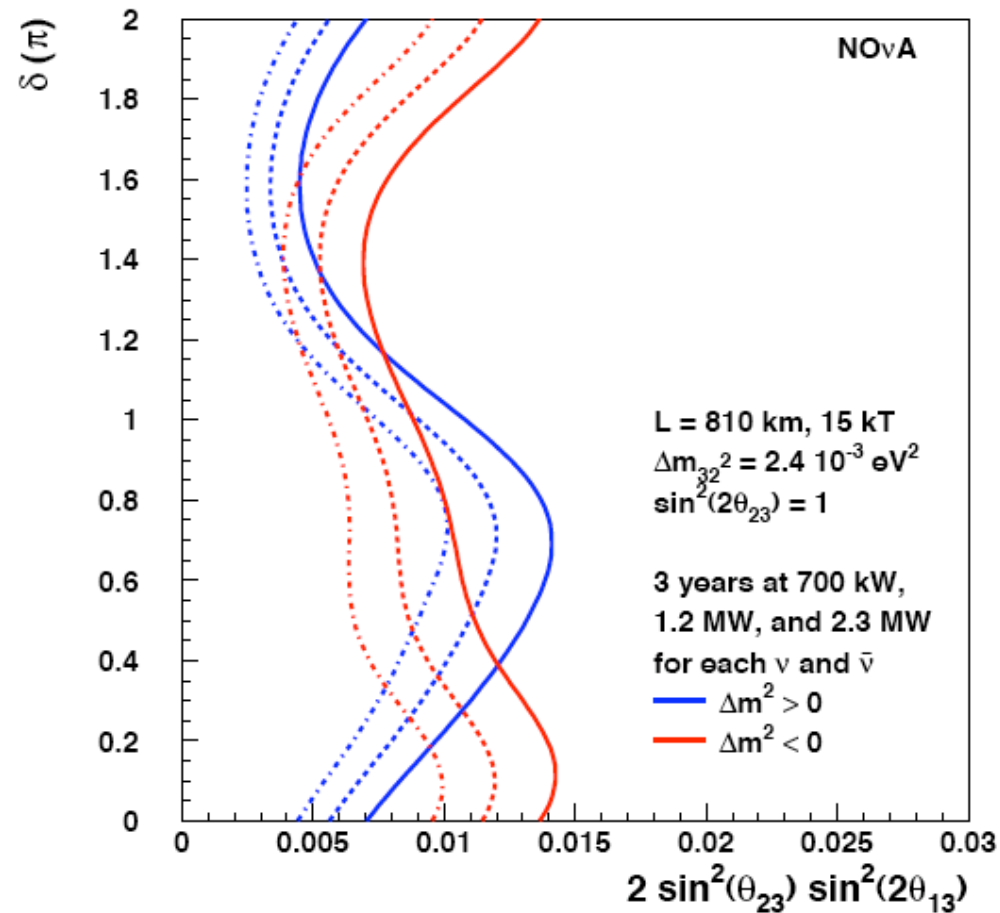
NOvA:

$$\delta m_{31}^2 > 0$$
$$\delta m_{31}^2 < 0$$



Beam $\sim 1\%$

90% CL Sensitivity to $\sin^2(2\theta_{13}) \neq 0$

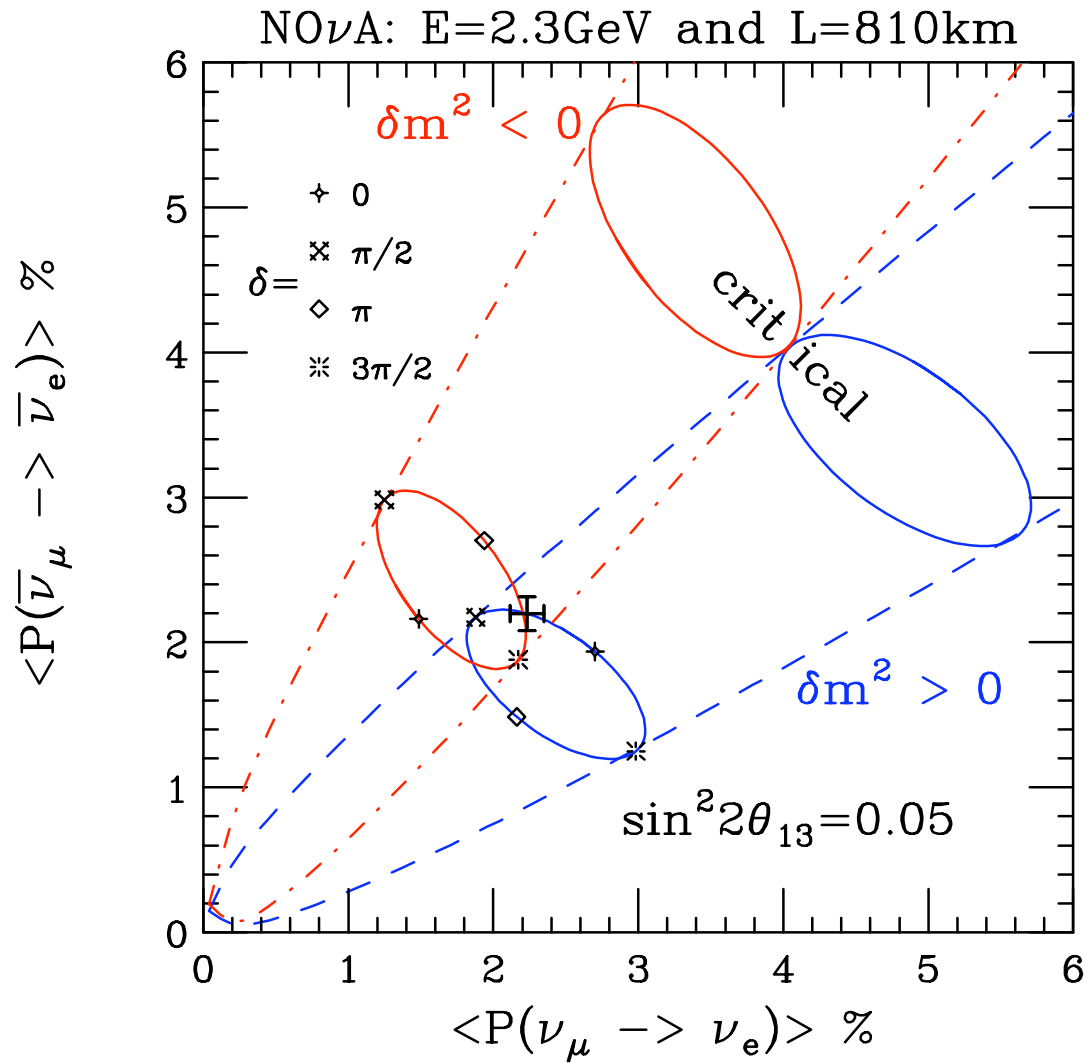


Sensitivity to Hierarchy: $sign \delta m_{31}^2$

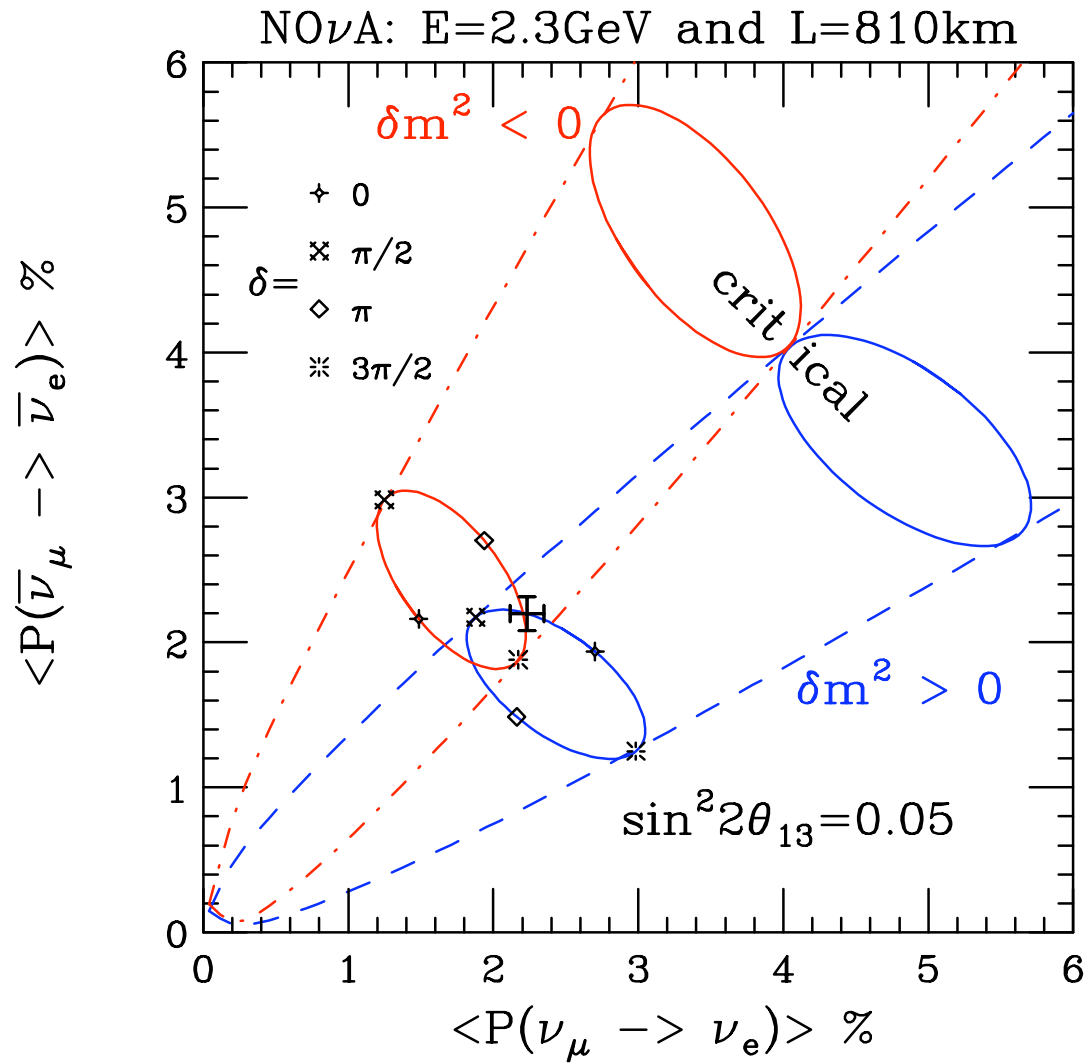
Correlations between

$$P(\nu_\mu \rightarrow \nu_e) \quad \text{and} \quad P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

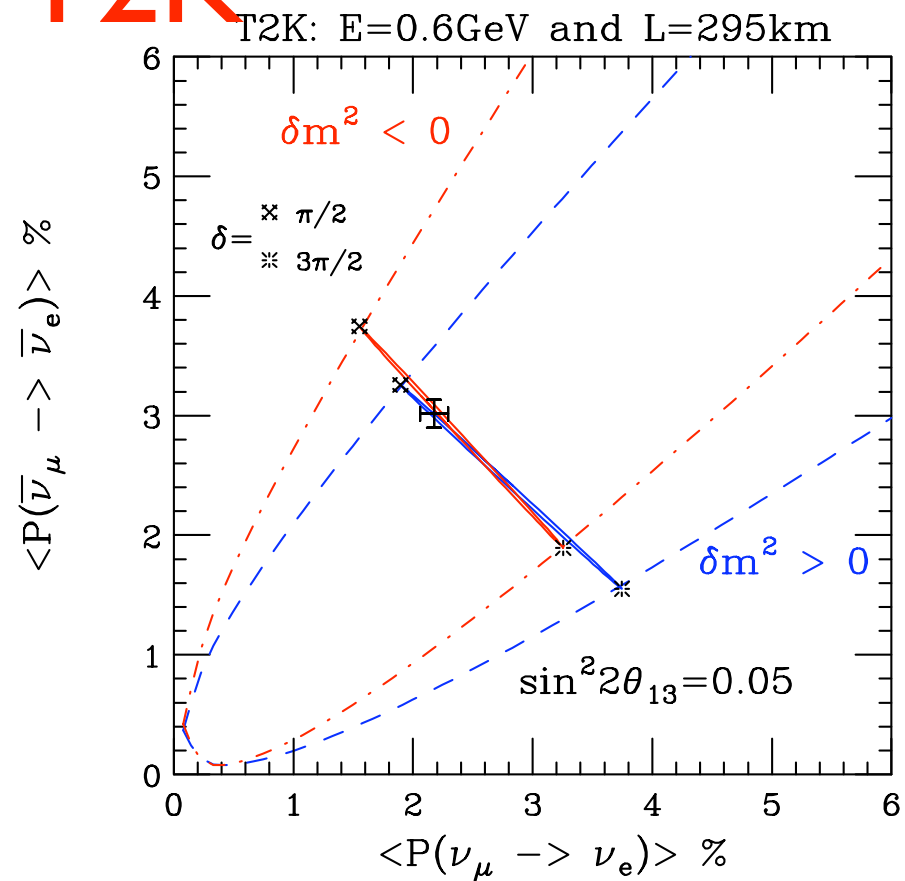
NO ν A:



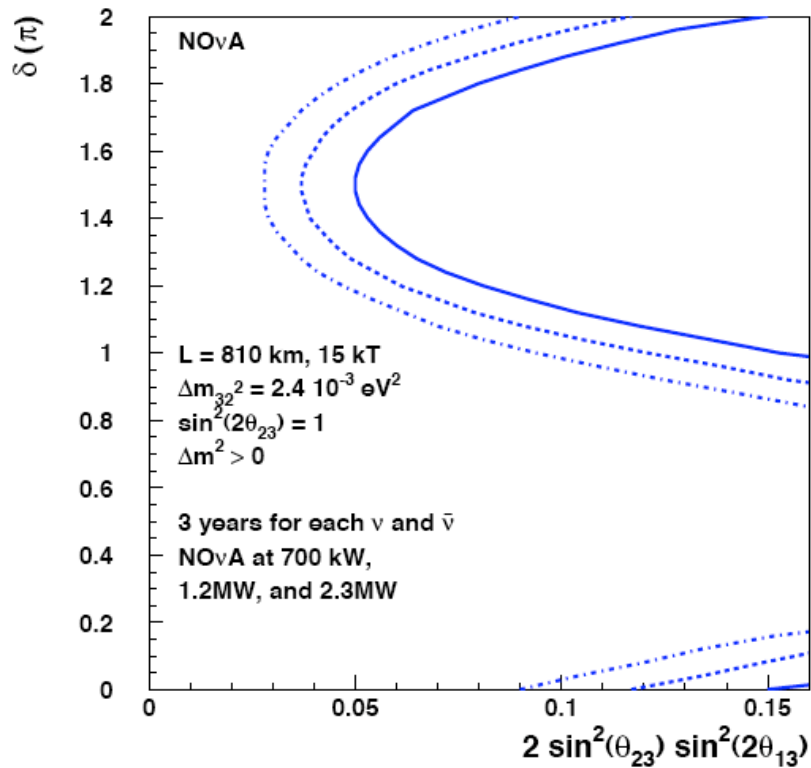
NO ν A:



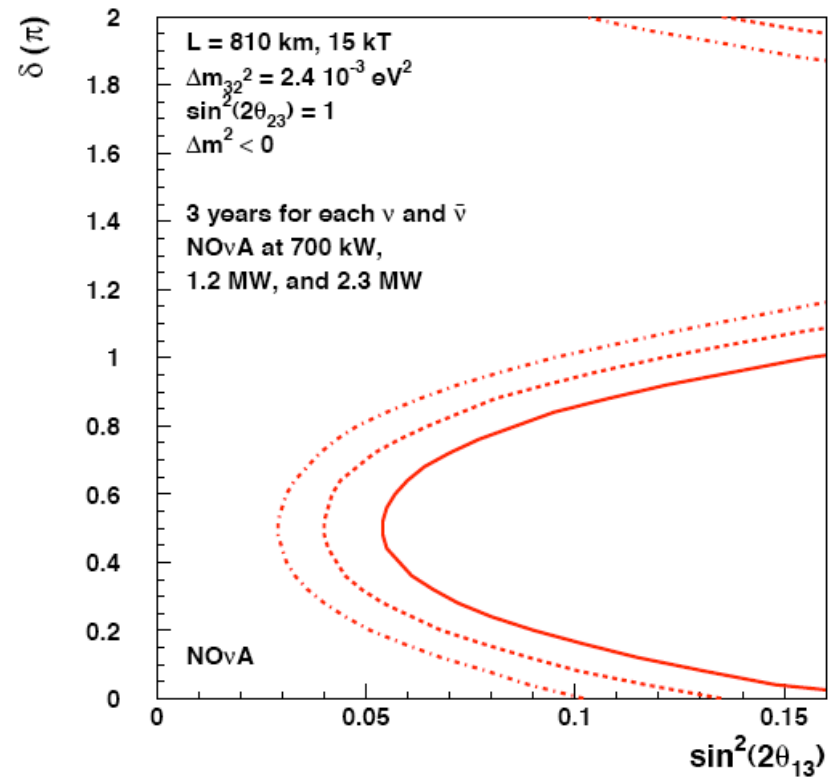
T2K



95% CL Resolution of the Mass Ordering NO ν A Alone



Normal Ordering

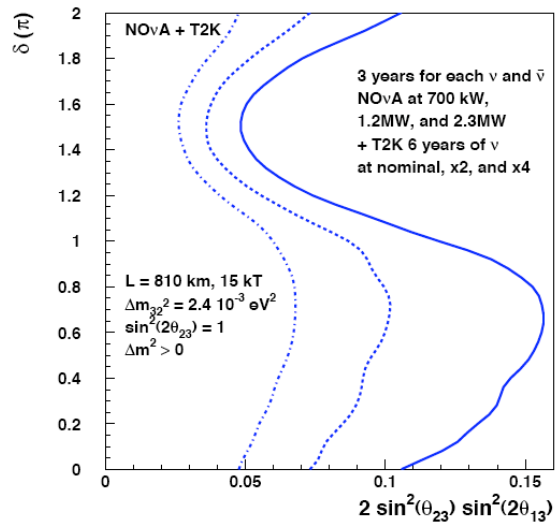


Inverted Ordering

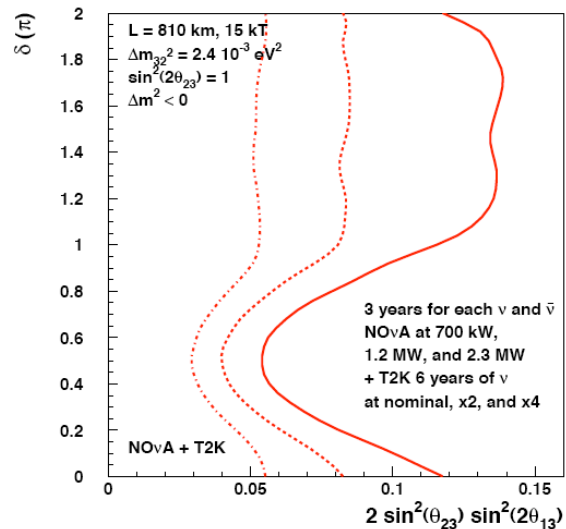
95% CL Resolution of the Mass Ordering

Ordering

NOvA Plus T2K

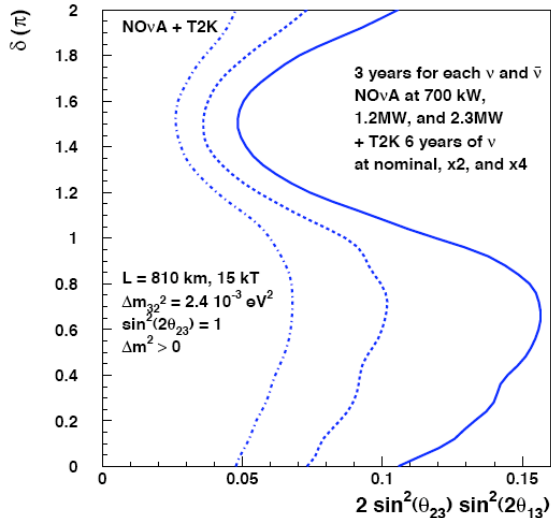


Normal Ordering

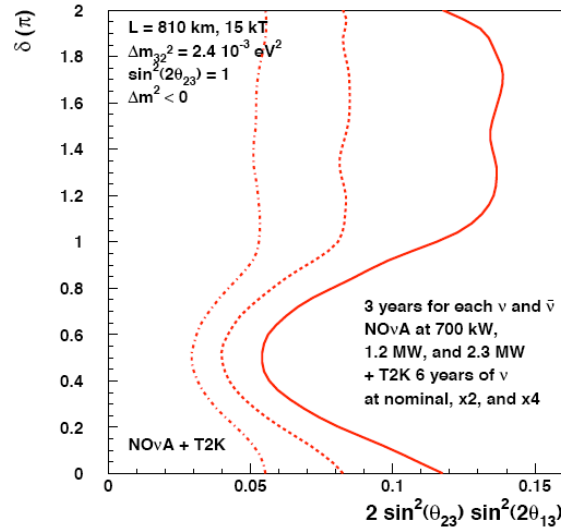


Inverted Ordering

95% CL Resolution of the Mass Ordering NOvA Plus T2K



Normal Ordering



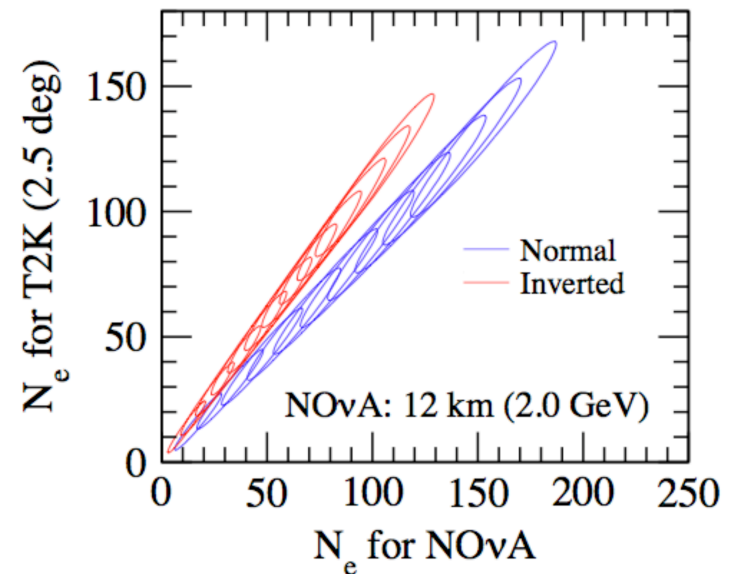
Inverted Ordering

T2K + NOvA, Neutrino Only, $\sin^2 2\theta_{13} = 0.01, 0.02, \dots, 0.1$

T2K: 0.75 MW, 5 yrs, 22.5 kton

NOvA: $6.5 \cdot 10^{20}$ POT/yr, 5 yrs, 30 kton, 24%

28



Sensitivity to CP violation: $\sin \delta$

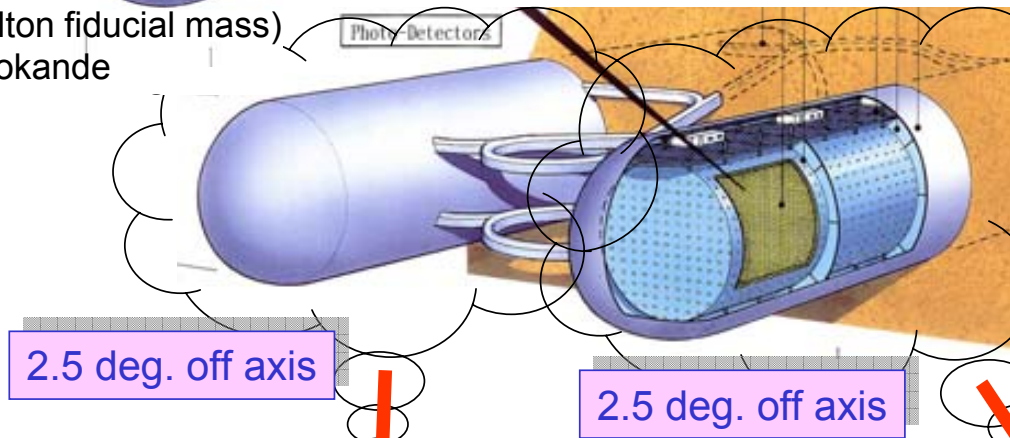
$$\text{Events} = \text{efficiency} * \text{Fid. Mass} * \text{Protons on Target} \\ (\text{Power} * \text{Time})$$

Off Axis:

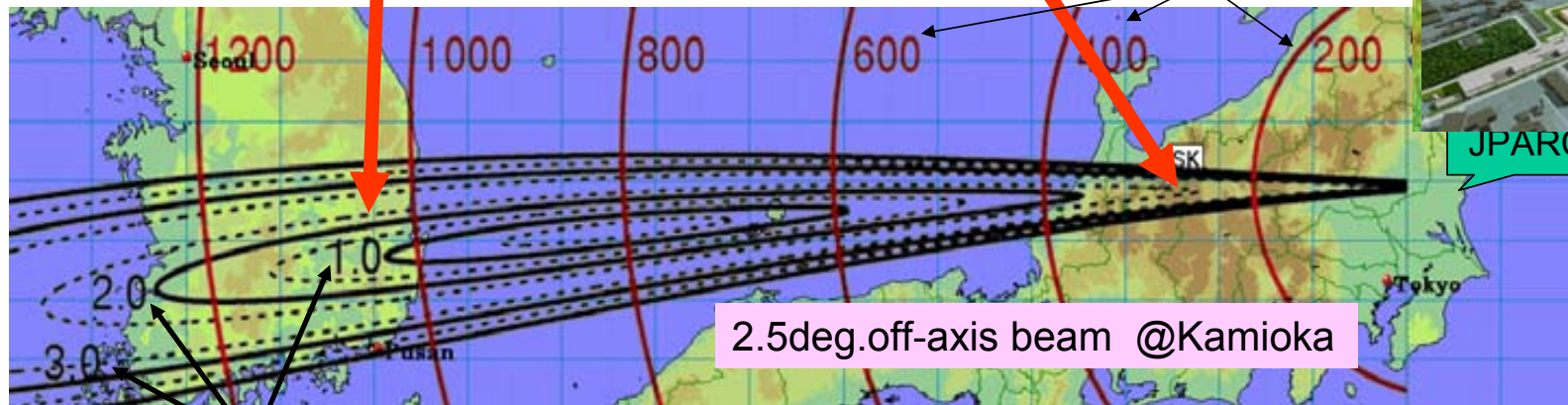


Some recent progress: detector in Korea

1Mton (0.54Mton fiducial mass)
Hyper-Kamiokande



Total cost must be similar to the baseline design.



2.5 deg. off axis

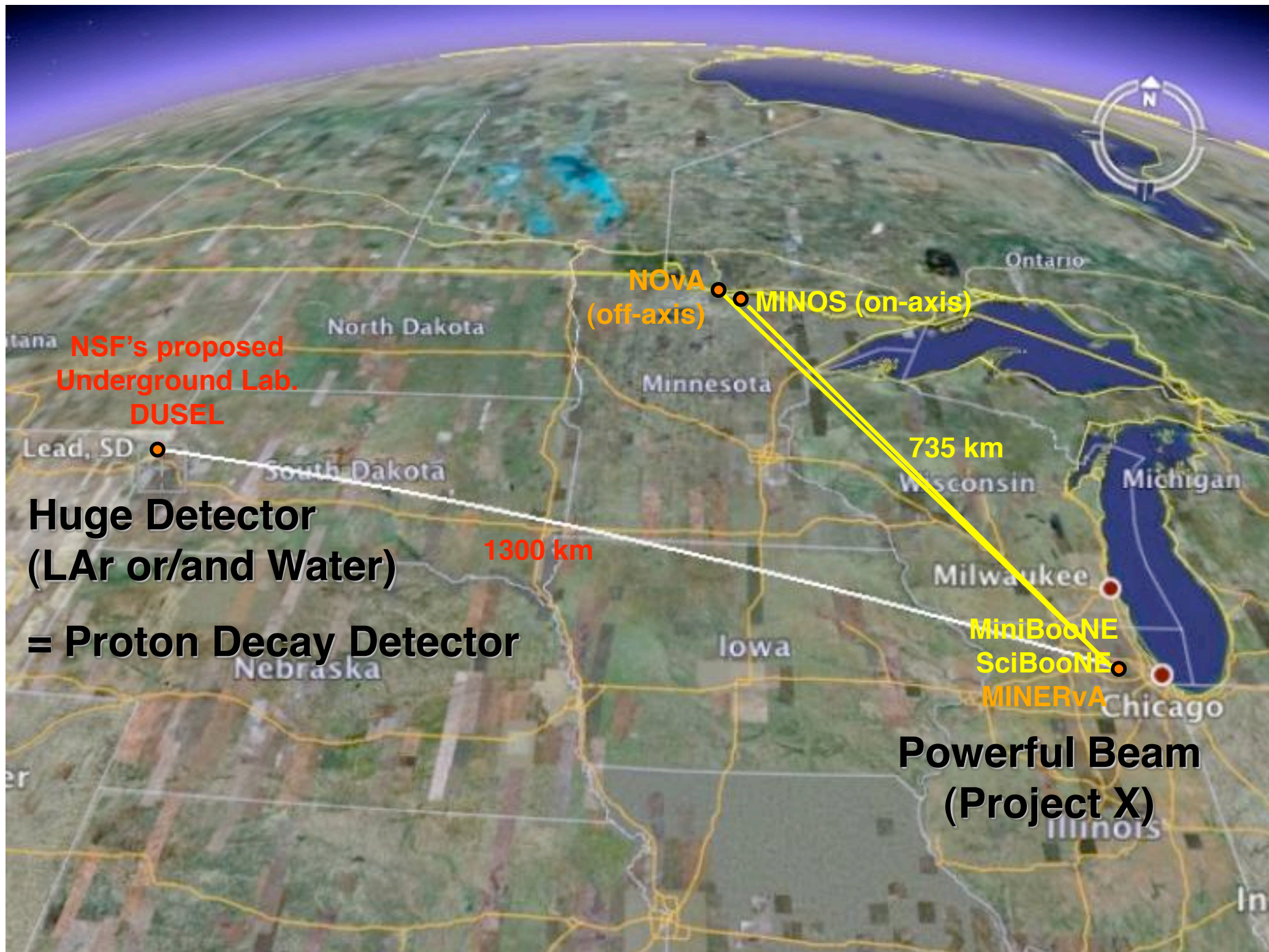
2.5 deg. off axis

Distance from the target (km)

2.5deg.off-axis beam @Kamioka

Off-axis angle

see Kajita talk:



**NSF's proposed
Underground Lab.
DUSEL**

**Huge Detector
(LAr or/and Water)
= Proton Decay Detector**

**NOvA
(off-axis)**

MINOS (on-axis)

735 km

1300 km

**MiniBooNE
SciBooNE
MINERvA**

**Powerful Beam
(Project X)**

Narrow Band Beam: Same E, Longer L T2KK

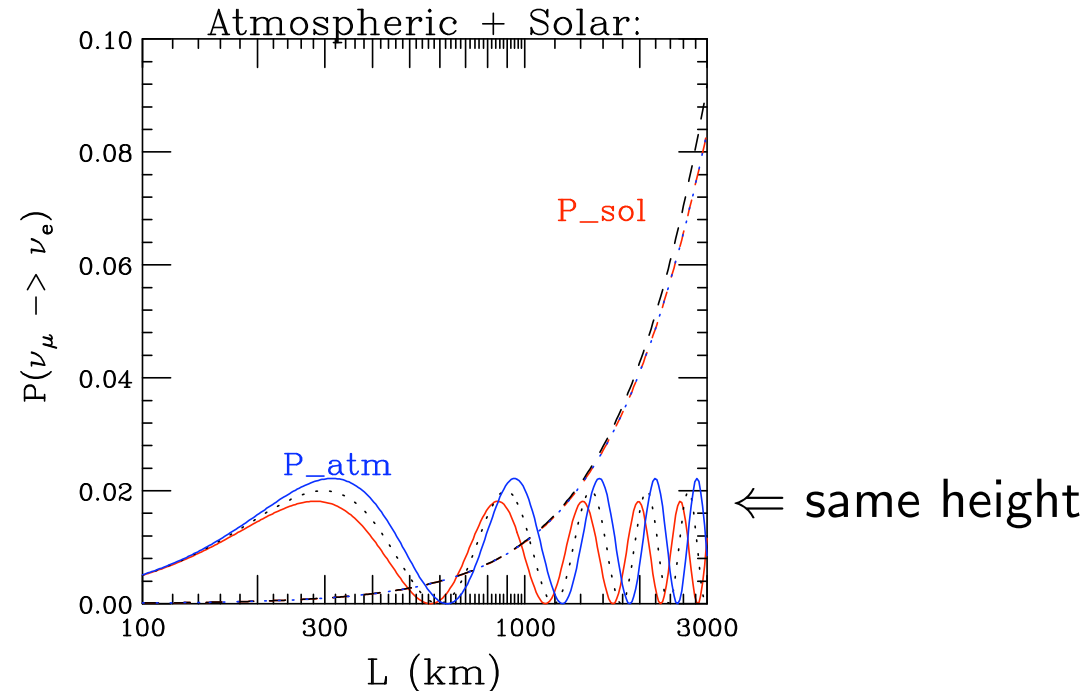
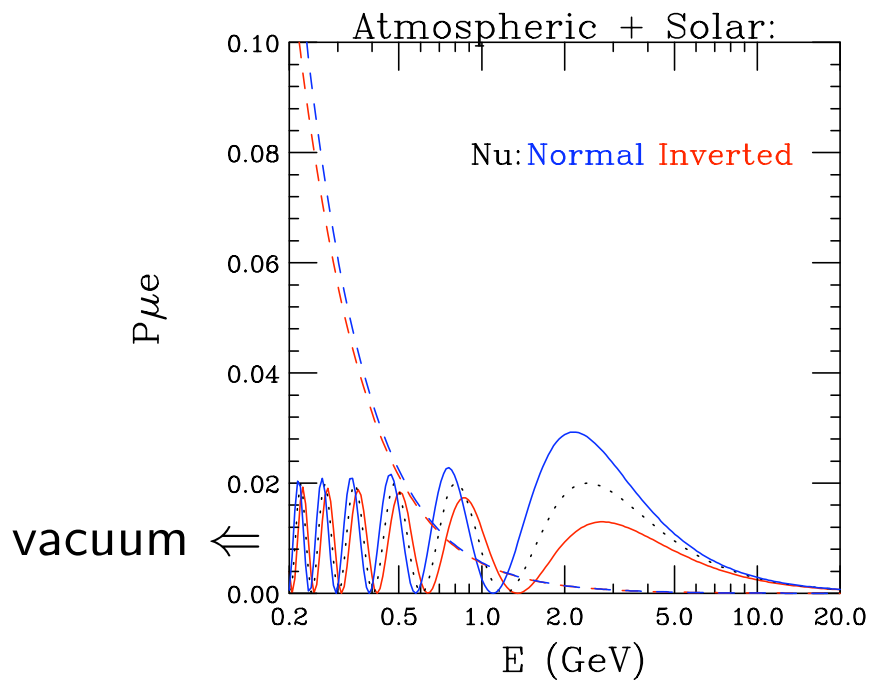
Broadband Beam: Same L, Lower E Fermilab to DUSEL

In VACUUM the SAME but NOT in MATTER

$$\sin^2 2\theta_{13} = 0.04$$

L=1200km

E=0.6 GeV



$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

Fermilab to DUSEL (T2KK similar)

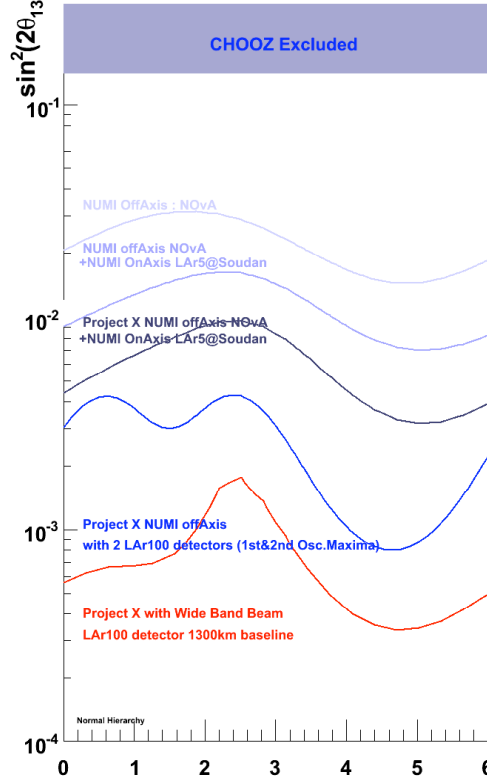
The 3σ Reach of the Successive Phases

$\sin^2 2\theta_{13}$

Mass Ordering

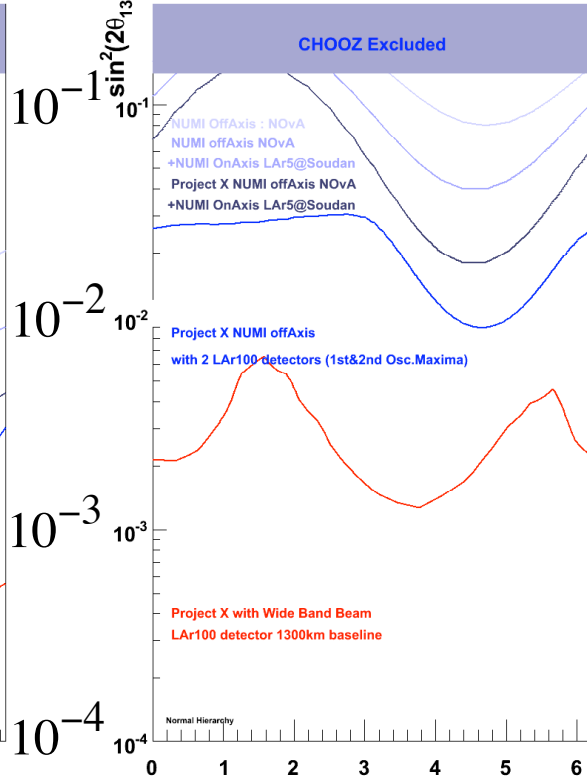
CP Violation

3σ Discovery Potential for $\sin^2(2\theta_{13}) \neq 0$



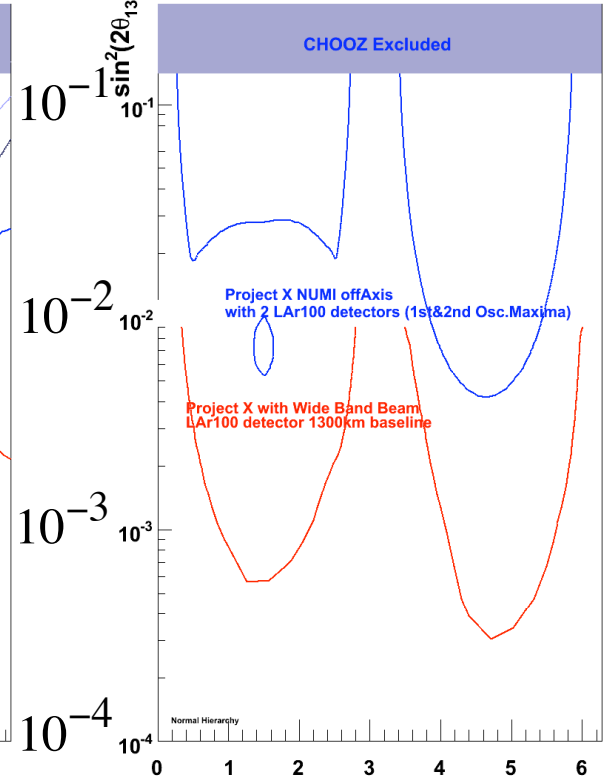
CP-Violating phase δ

Discovery Potential $\text{sign}\Delta m_{31}^2$



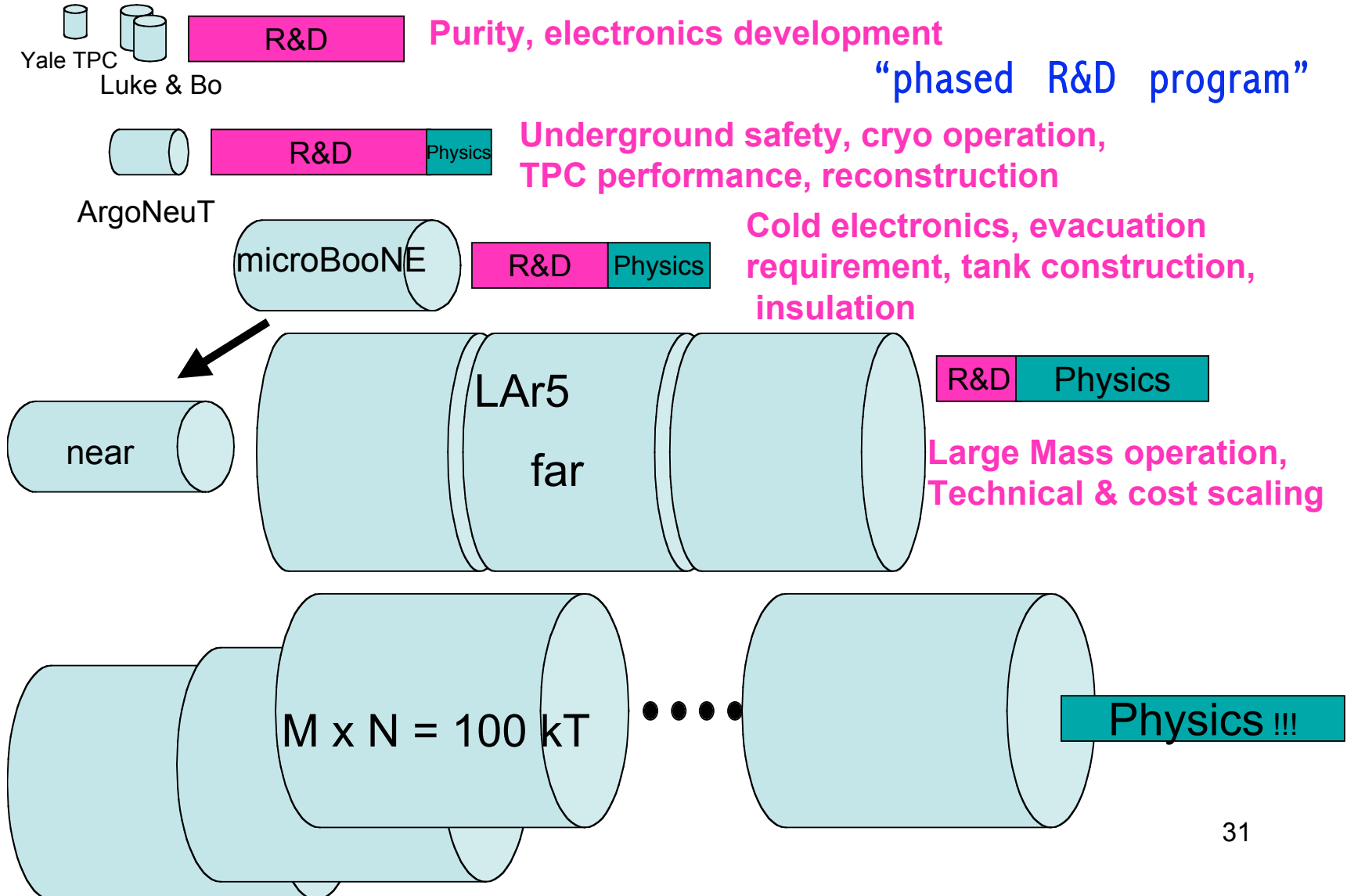
CP-Violating phase δ

3σ Discovery Potential for $\delta \neq 0$ and $(\neq \pi)$

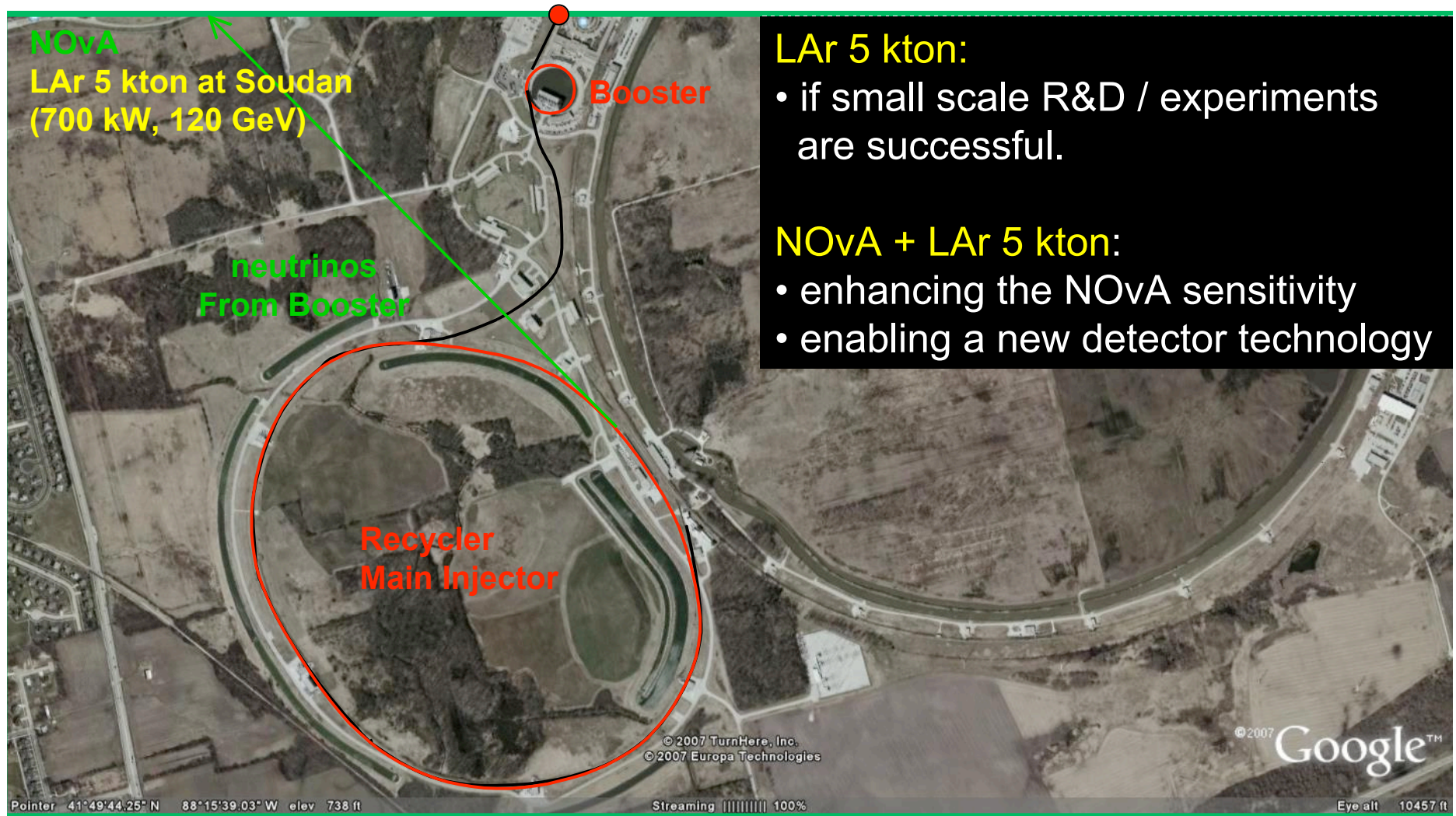


CP-Violating phase δ

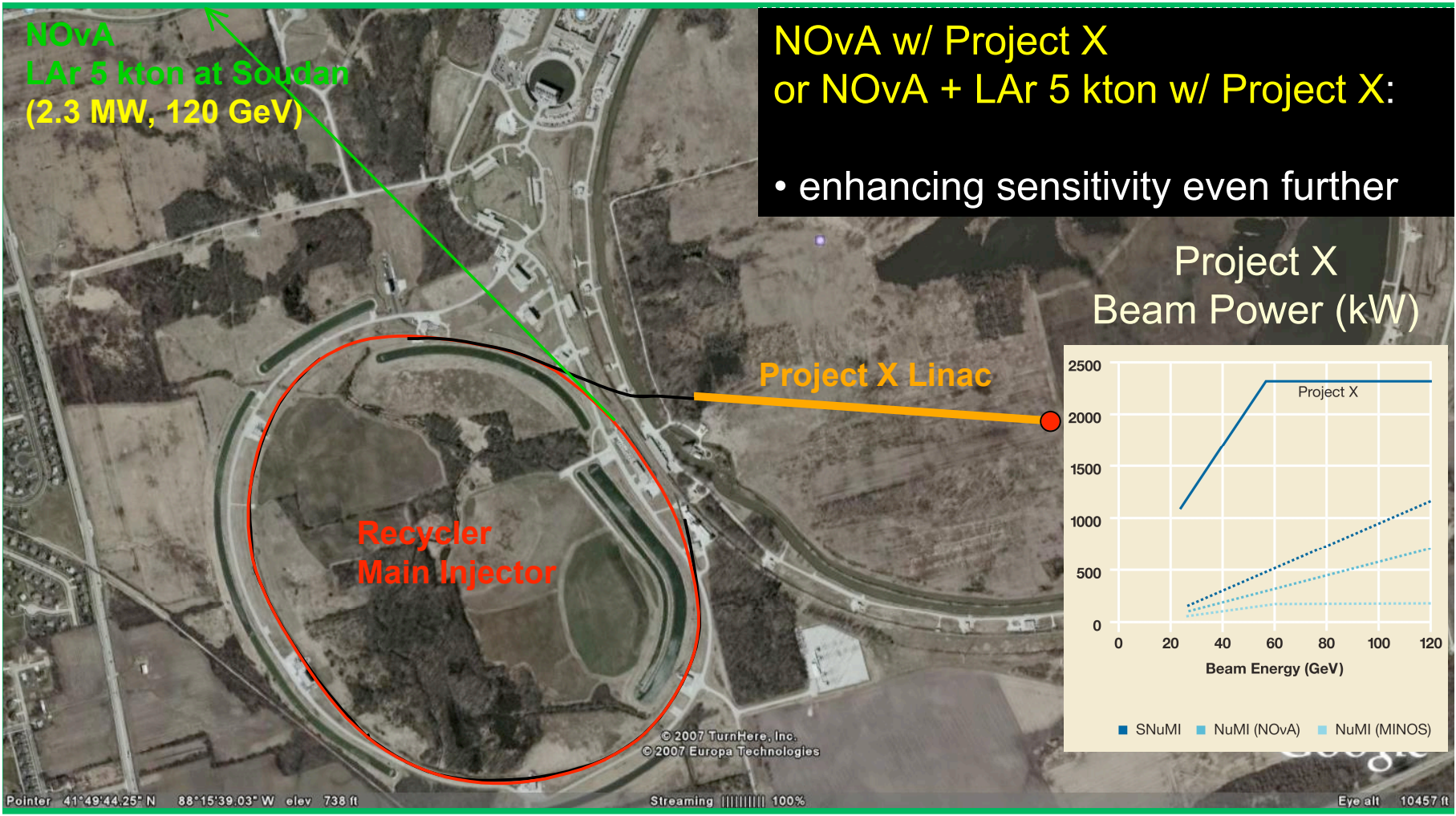
Evolution of the Liquid Argon Physics Program



Phase 1.5:



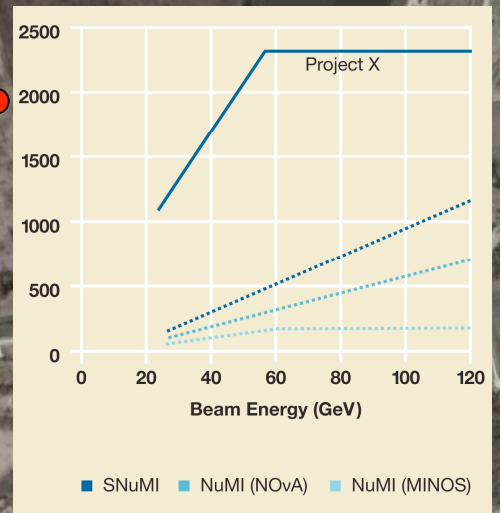
Phase 2:



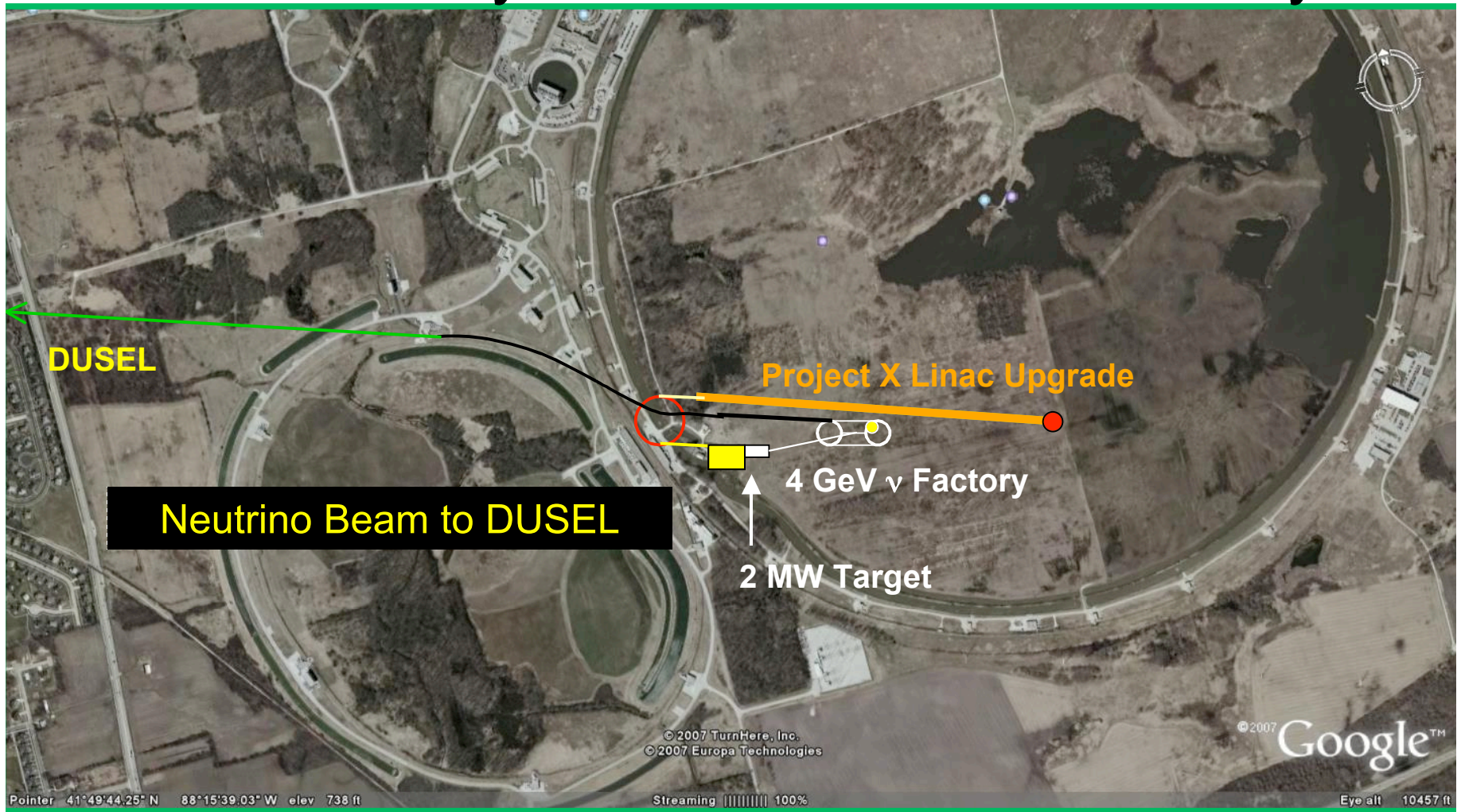
NOvA w/ Project X
or NOvA + LAr 5 kton w/ Project X:

- enhancing sensitivity even further

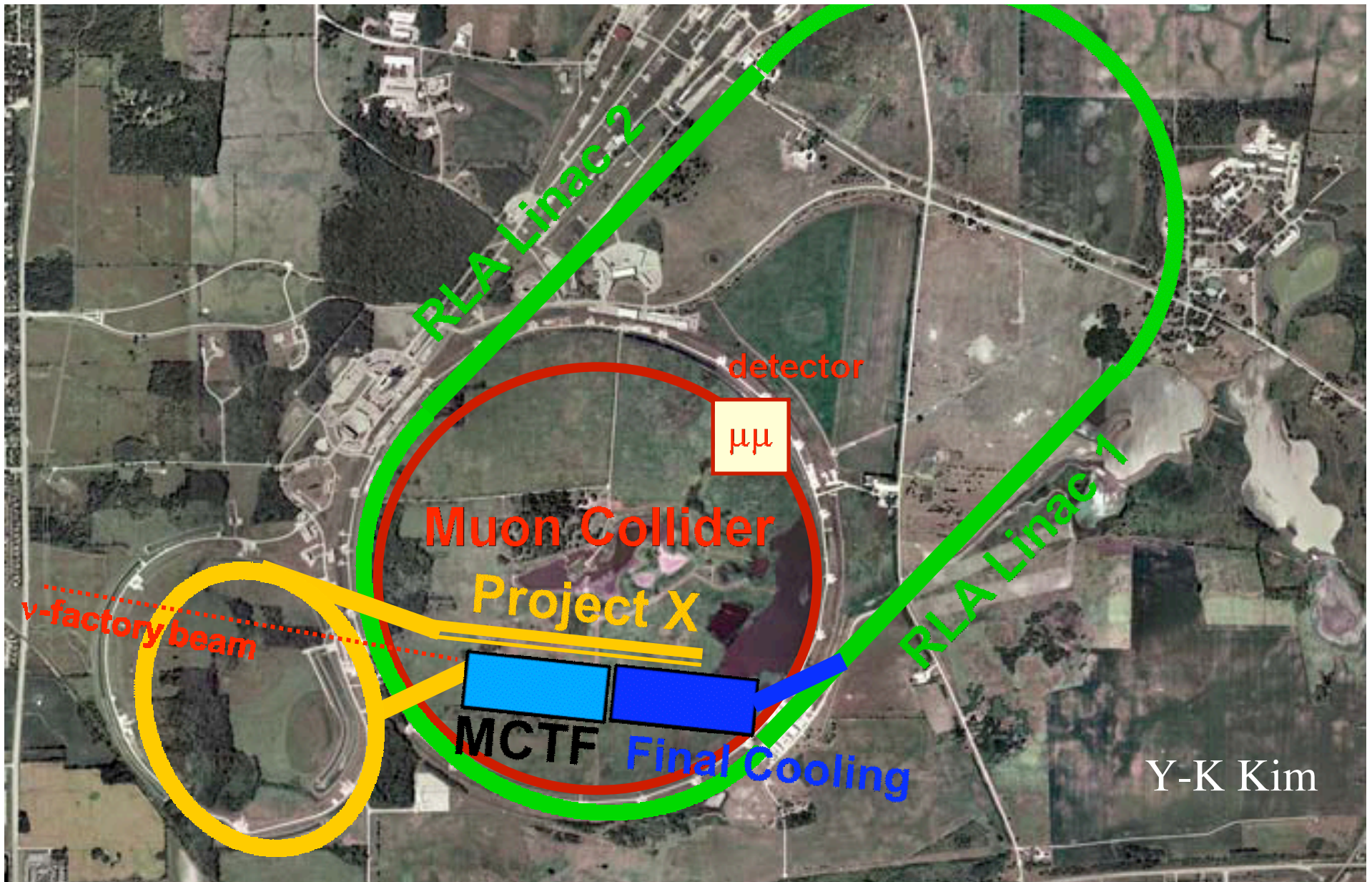
Project X
Beam Power (kW)



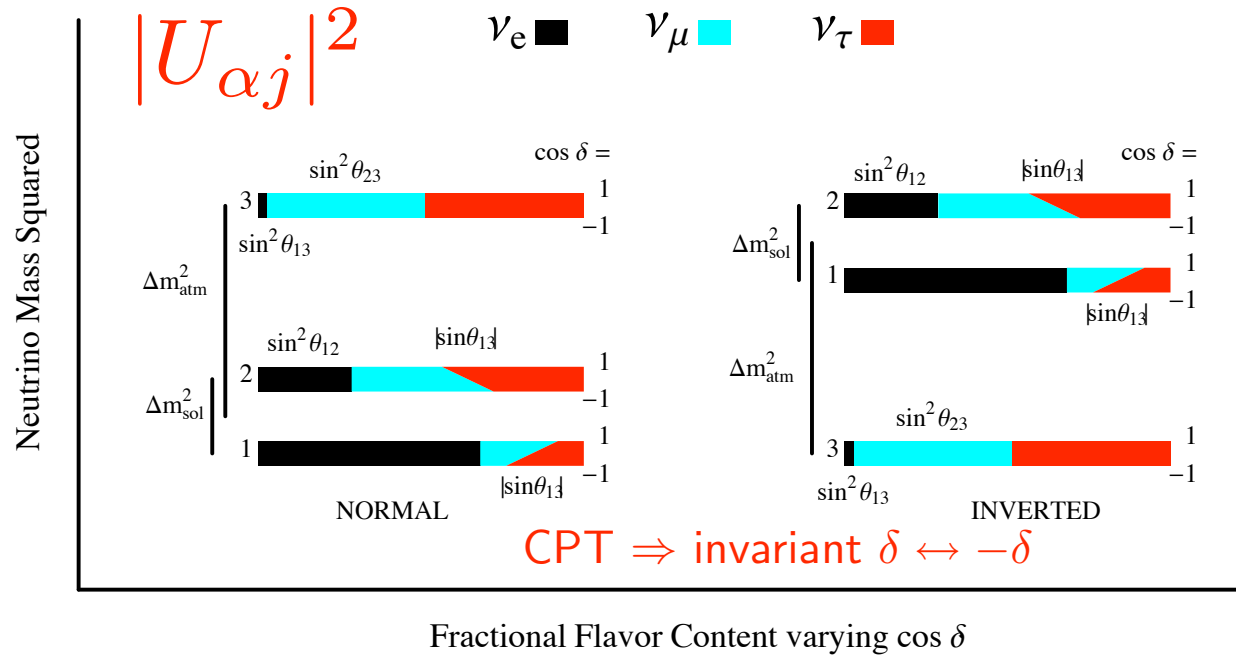
Toward “Proton Intensity Upgrade” Evolutionary Path to a Neutrino Factory



Evolutionary Path to a $\mu^+\mu^-$ Collider

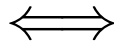


Summary:



CP

$$\nu_\mu \rightarrow \nu_e$$



$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

T

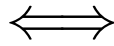


CPT across diagonals



T

$$\nu_e \rightarrow \nu_\mu$$



$$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$$

CP

- First Row: Superbeams where ν_e contamination $\sim 1\%$
- Second Row: ν -Factory or β -Beams, no beam contamination

● Size of $|U_{e3}|^2$

● Hierarchy ?

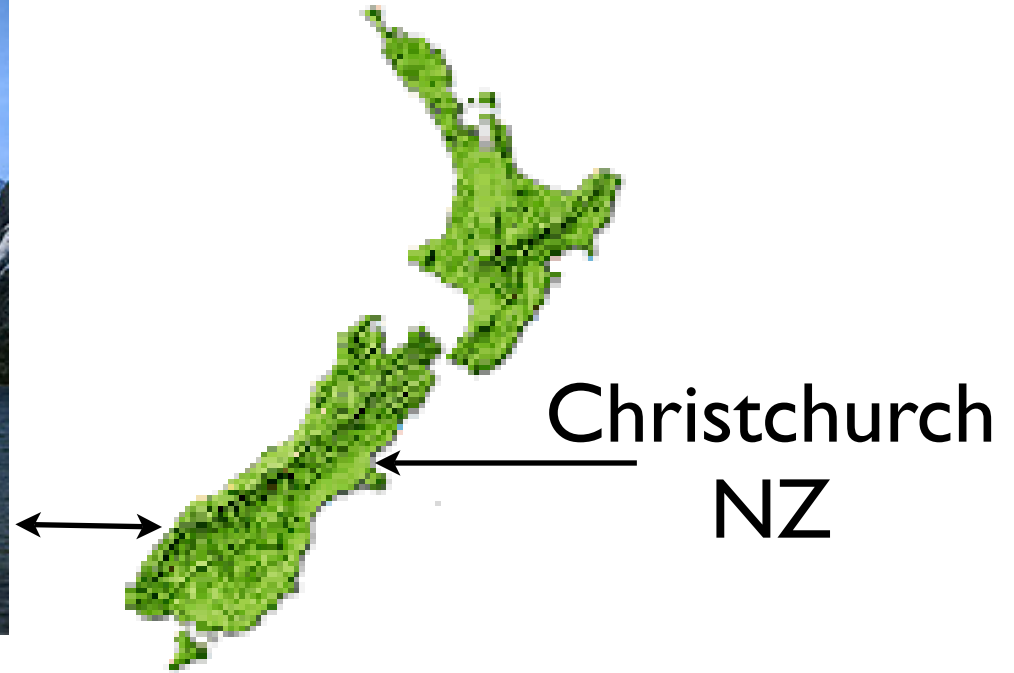
● CPV ?

● Maximal {23} Mixing ?

●

● New Interactions and Surprises !!!

Neutrino 2008 May 25-31



www.neutrino2008.co.nz