

# $D^0$ mixing & CPV from Belle & BaBar



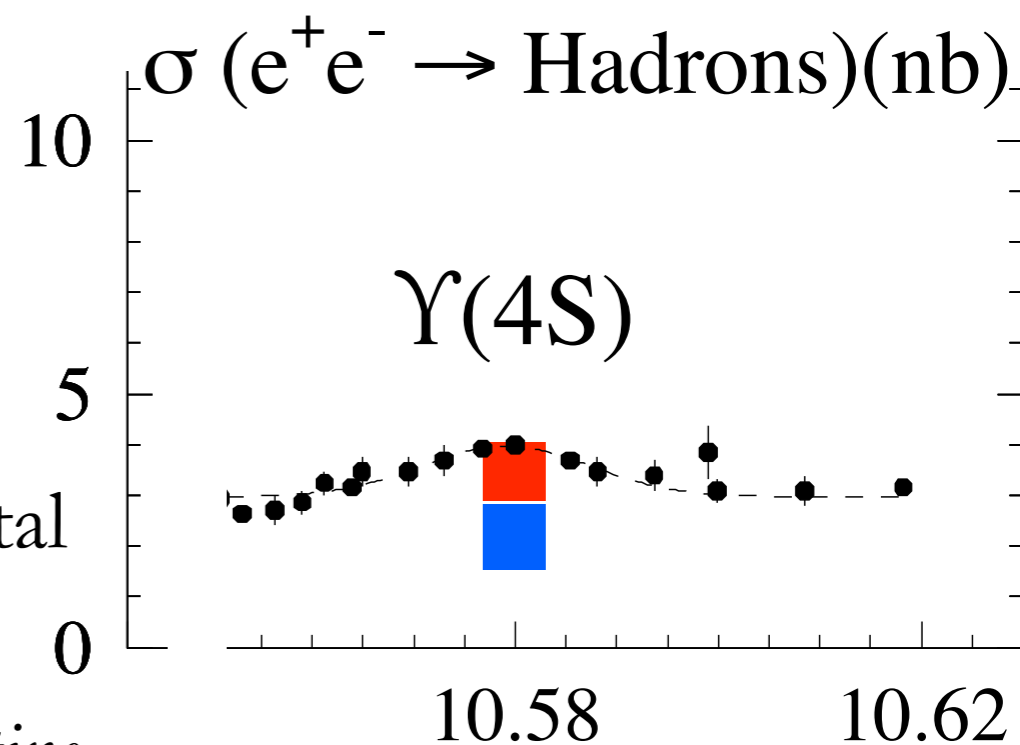
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There is an unimpeachable reason to visit the Sistine Chapel, namely to see Michelangelo's frescoes. ... Most of you who have been [there] will have forgotten ... there are wonderful frescoes by other famous masters, namely Botticelli...

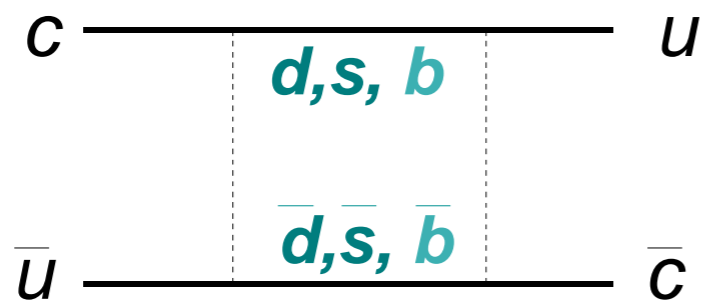
... I concede that the fascination of charm decays might not match that of beauty decays any more than Botticelli can match the power of Michelangelo. Of course, Botticelli is still Botticelli, i.e. a first-rate artist, but what about charm?

... I will argue that future charm studies can provide us with first rate lessons of fundamental dynamics...

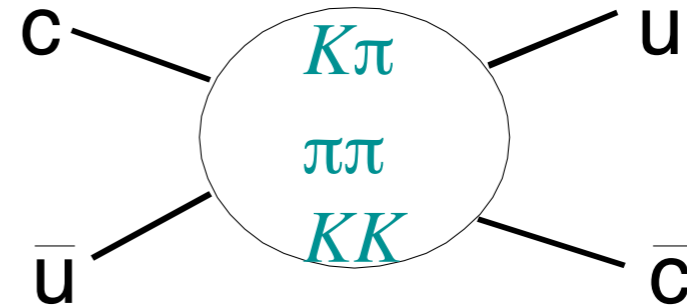
- I. Bigi, "*Charm Physics - Like Botticelli in the Sistine Chapel (2001)*"



# Neutral Meson Mixing



“box” diagram:  $\Delta m$



$D^0$  mixing is dominated by long-distance contributions (both  $\Delta m$  and  $\Delta \Gamma$ )

Meson	flavors	$\Delta m/\Gamma$	$\Delta \Gamma/2\Gamma$	observed?
$K^0$	$\bar{s}d$	0.474	0.997	1958
$B^0$	$\bar{b}d$	0.77	< 1%	1987
$B_s^0$	$\bar{b}s$	27	$0.15 \pm 0.07$	2006
$D^0$	$c\bar{u}$	< 0.029	$0.011 \pm 0.005$	March 2007

# $D^0$ mixing - the Formalism

$$i \frac{\partial}{\partial t} \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix} = \left( M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix}$$

$$|D_1(t)\rangle = |D_1\rangle e^{-(\Gamma_1/2 + im_1)t}$$

$$|D_2(t)\rangle = |D_2\rangle e^{-(\Gamma_2/2 + im_2)t}$$

$$|D^0\rangle = (|D_1\rangle + |D_2\rangle) / 2p$$

$$|\bar{D}^0\rangle = (|D_1\rangle - |D_2\rangle) / 2q$$

$$|D^0(t)\rangle = e^{-(\bar{\Gamma}/2 + i\bar{m})t} \left\{ \cosh [(\dots)t] |D^0\rangle + \frac{q}{p} \sinh [(\dots)t] |\bar{D}^0\rangle \right\}$$

$$|\bar{D}^0(t)\rangle = e^{-(\bar{\Gamma}/2 + i\bar{m})t} \left\{ \frac{p}{q} \sinh [(\dots)t] |D^0\rangle + \cosh [(\dots)t] |\bar{D}^0\rangle \right\}$$

$$\bar{m} \equiv (m_1 + m_2) / 2$$

$$\Delta m \equiv m_2 - m_1$$

$$\bar{\Gamma} \equiv (\Gamma_1 + \Gamma_2) / 2$$

$$\Delta\Gamma \equiv \Gamma_2 - \Gamma_1$$

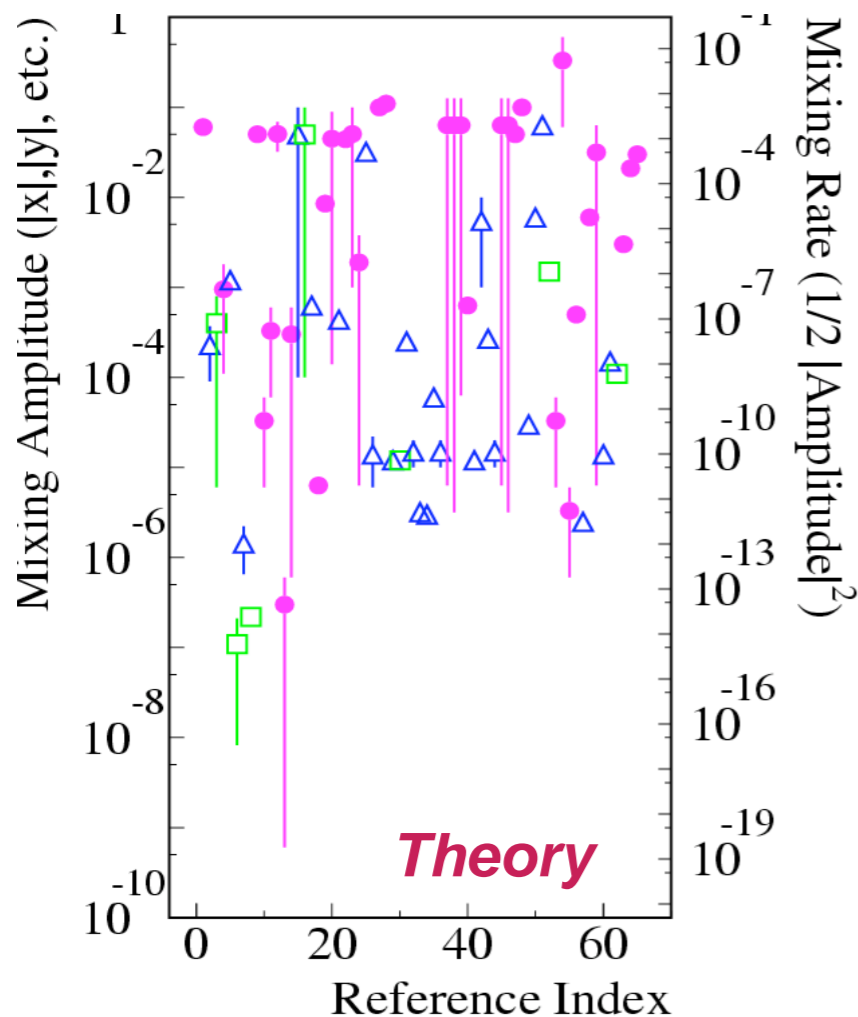
$$(\dots) = \frac{\Delta\Gamma}{4} + i \frac{\Delta m}{2}$$

# D<sup>0</sup> mixing - the Formalism

For  $\Delta m t \ll 1$  and  $\Delta\Gamma t \ll 1$

$$|\langle f | H | D^0(t) \rangle|^2 \propto e^{-\bar{\Gamma}t} \left\{ 1 + (y\mathcal{R}(\lambda) - x\mathcal{I}(\lambda)) \bar{\Gamma}t + |\lambda|^2 \frac{x^2 + y^2}{4} (\bar{\Gamma}t)^2 \right\}$$

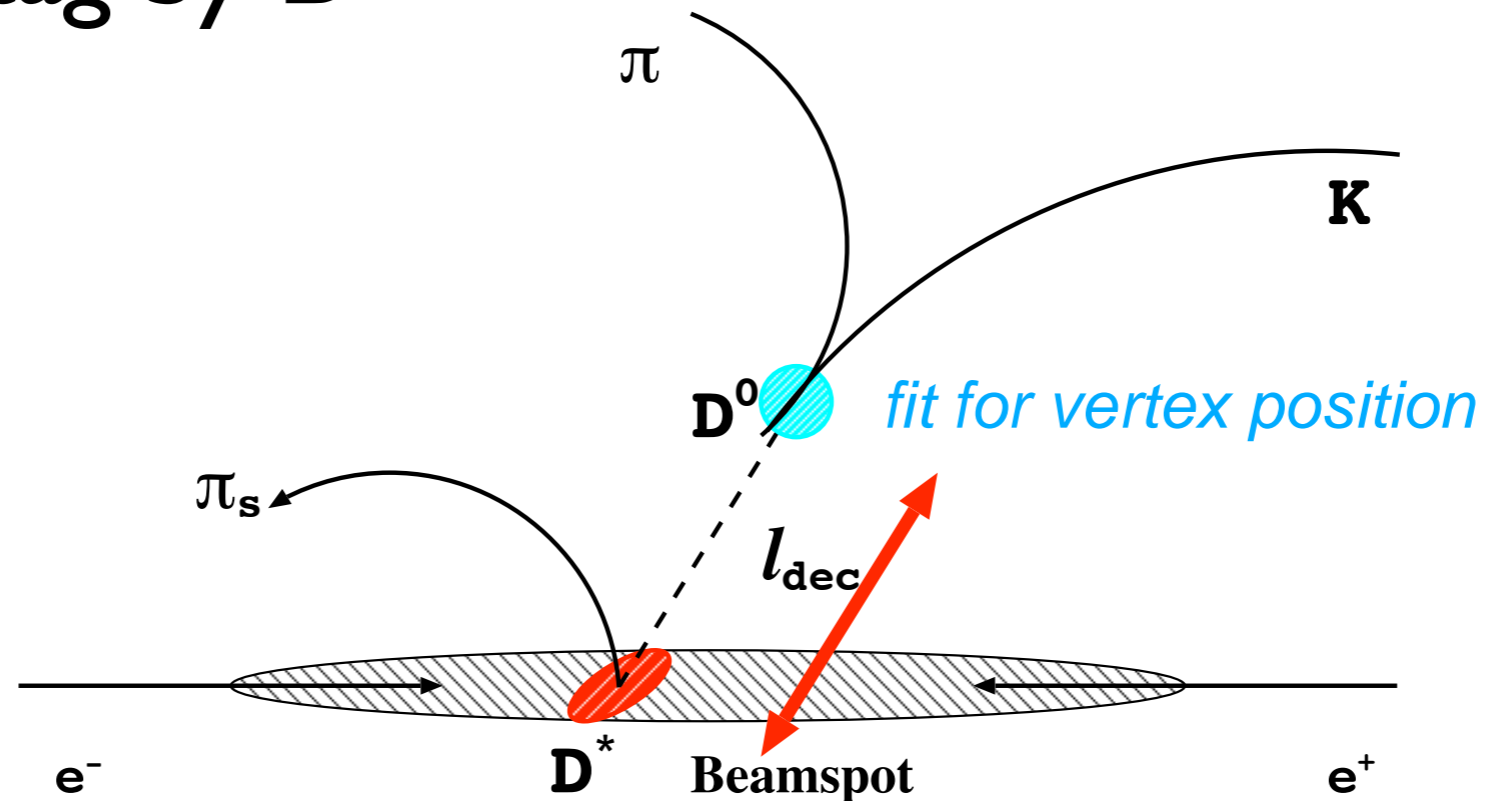
$$x \equiv \frac{\Delta m}{\bar{\Gamma}} \quad y \equiv \frac{\Delta\Gamma}{2\bar{\Gamma}} \quad \lambda \equiv \frac{q \mathcal{A}(\bar{D}^0 \rightarrow f)}{p \mathcal{A}(D^0 \rightarrow f)}$$



$x \lesssim y \sim$	$10^{-6} - 10^{-3}$	(short distance)
	$10^{-3} - 10^{-2}$	(long distance)

# $D^0$ mixing - key exp'tal features

📌 Flavor tag by  $D^*$



📌  $p(D^*) > \sim 2.5$  GeV to eliminate  $D^0$ 's from B decays

# $D^0$ mixing - exp'tal results

$\exists$  various measurements using

## Lifetime difference

- PRL 98, 211803 
- 0712.2249

## Hadronic $D^0$ decays

- PRL 99, 131803
- PRL 98, 211802 

## Semileptonic $D^0$ decays

- 0802.2952
- PRD 76, 014018



# $D^0$ mixing - by lifetime difference

- Study  $D^0$  mixing by apparent lifetime difference for  $D^0 \rightarrow K^+K^-$ ,  $\pi^+\pi^-$  and  $D^0 \rightarrow K^-\pi^+$

- Approximately, the effective lifetimes are:

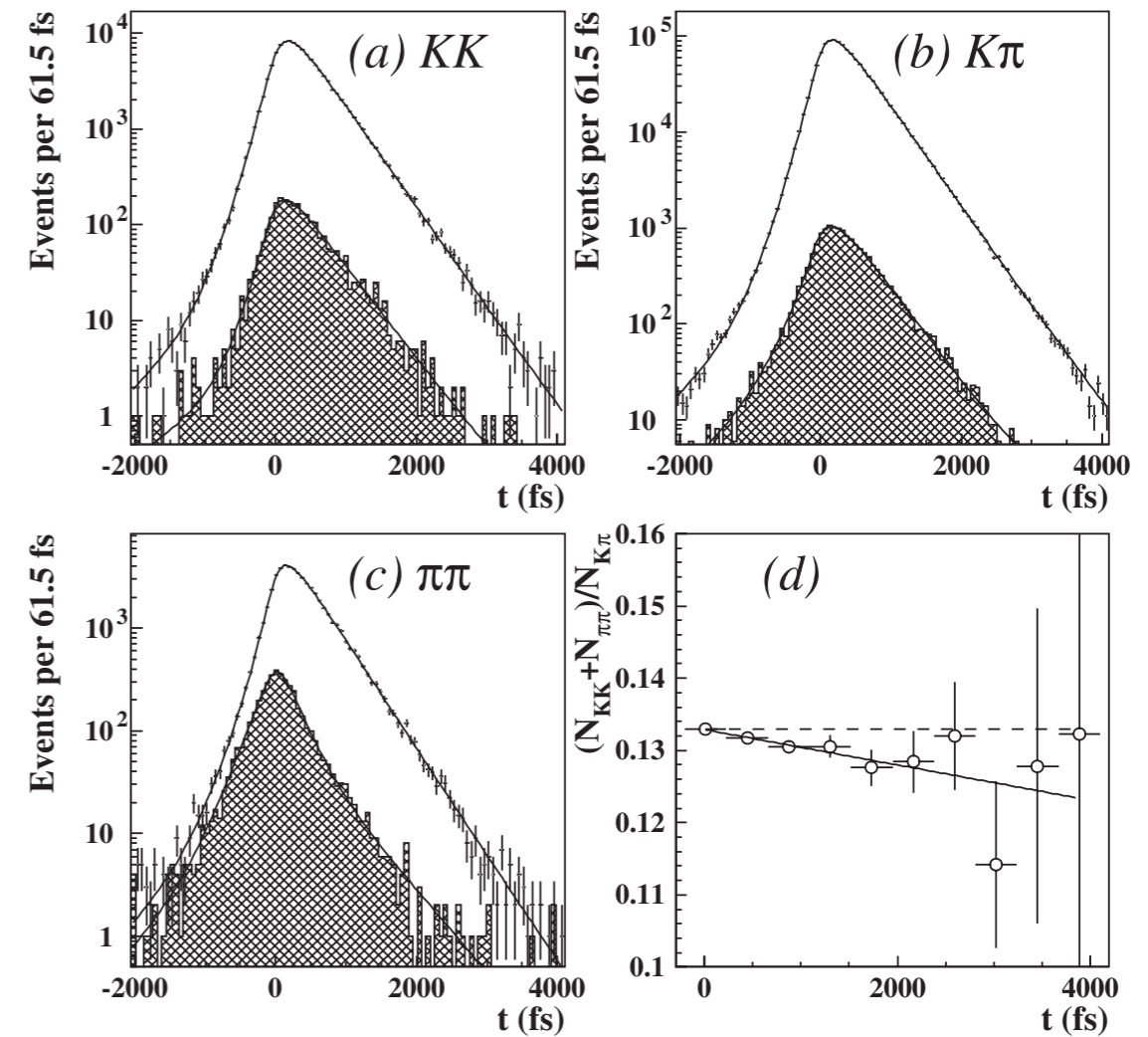
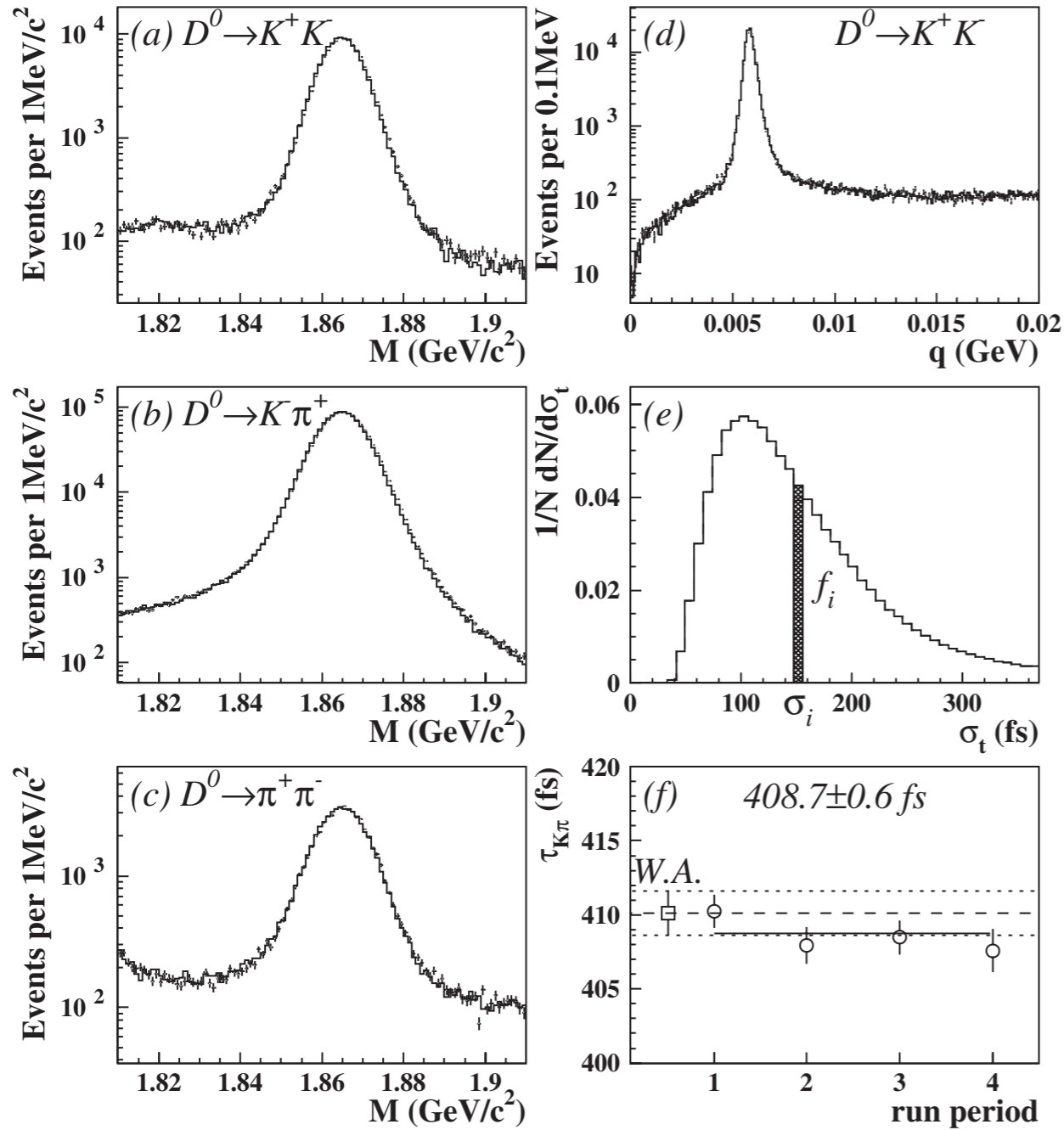
$$\begin{aligned} \tau_{hh}^+ &= \tau_{K\pi} / \left[ 1 + \left| \frac{q}{p} \right| (y \cos \varphi_f - x \sin \varphi_f) \right] \\ \tau_{hh}^- &= \tau_{K\pi} / \left[ 1 + \left| \frac{p}{q} \right| (y \cos \varphi_f + x \sin \varphi_f) \right] \end{aligned} \quad \varphi_f \equiv \arg(\lambda)$$

$$y_{CP} = \frac{\tau_{k^\pm \pi^\mp}}{\langle \tau_{h^+ h^-} \rangle} - 1 \quad \xrightarrow[\text{conserved}]{\text{CP}} \quad y_{CP} = y = \Delta\Gamma / 2\bar{\Gamma}$$

$$A_\Gamma = \frac{\tau_{hh}^+ - \tau_{hh}^-}{\tau_{hh}^+ + \tau_{hh}^-} \quad \Delta Y = \frac{\tau_{k^\pm \pi^\mp}}{\langle \tau_{h^+ h^-} \rangle} A_\Gamma \quad \xrightarrow[\text{conserved}]{\text{CP}} \quad 0$$



# $D^0$ mixing - by lifetime difference

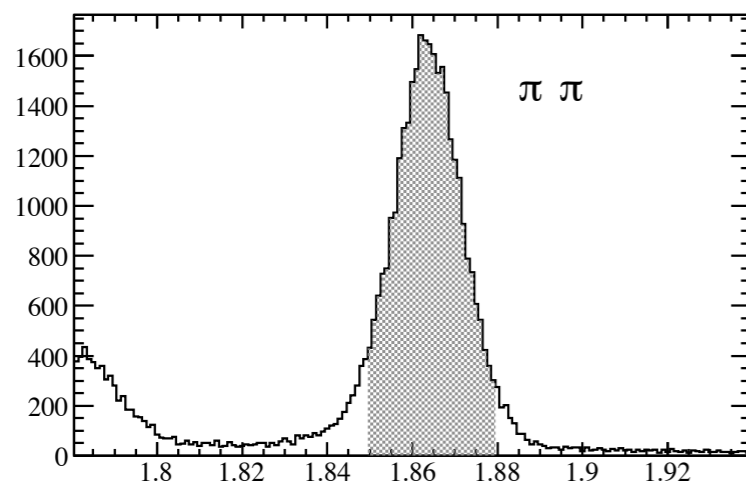
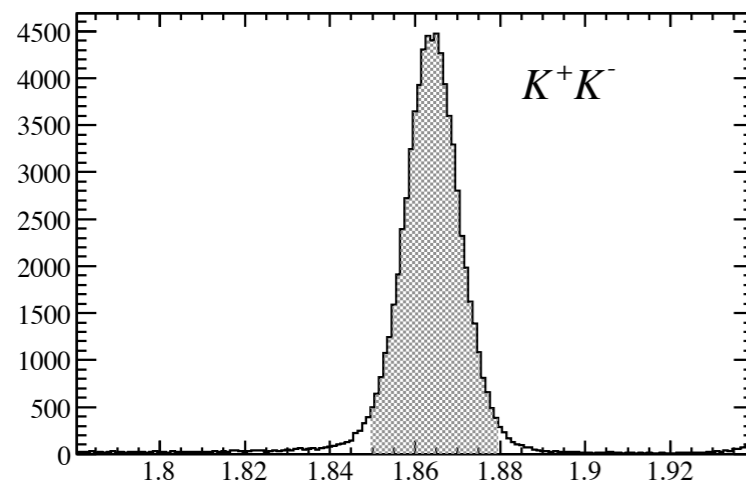
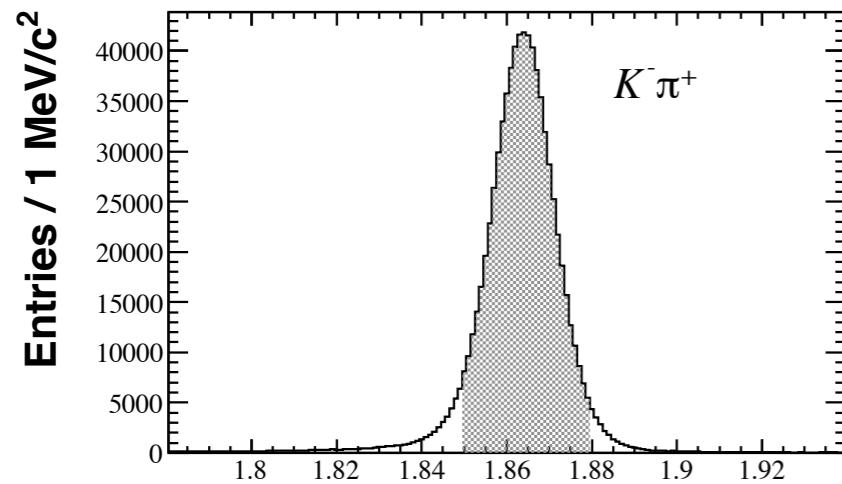


$$y_{CP} = (1.31 \pm 0.32 \pm 0.25)\%$$

$$A_{\Gamma} = (0.01 \pm 0.30 \pm 0.15)\%$$



# $D^0$ mixing - by lifetime difference



$M(\pi^+\pi^-)$  ( $\text{GeV}/c^2$ )

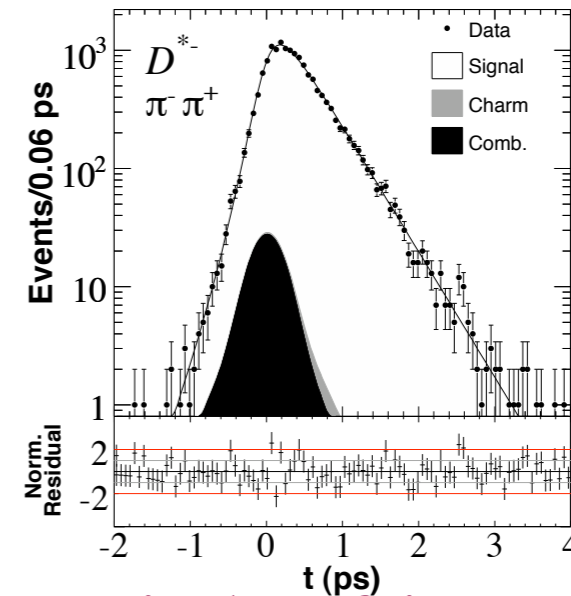
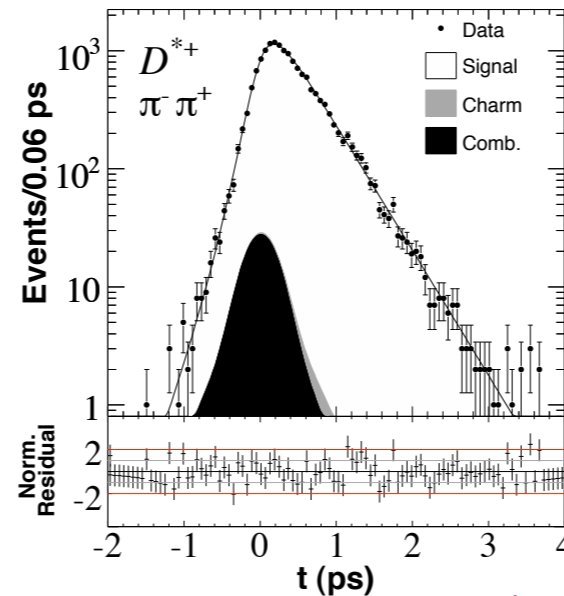
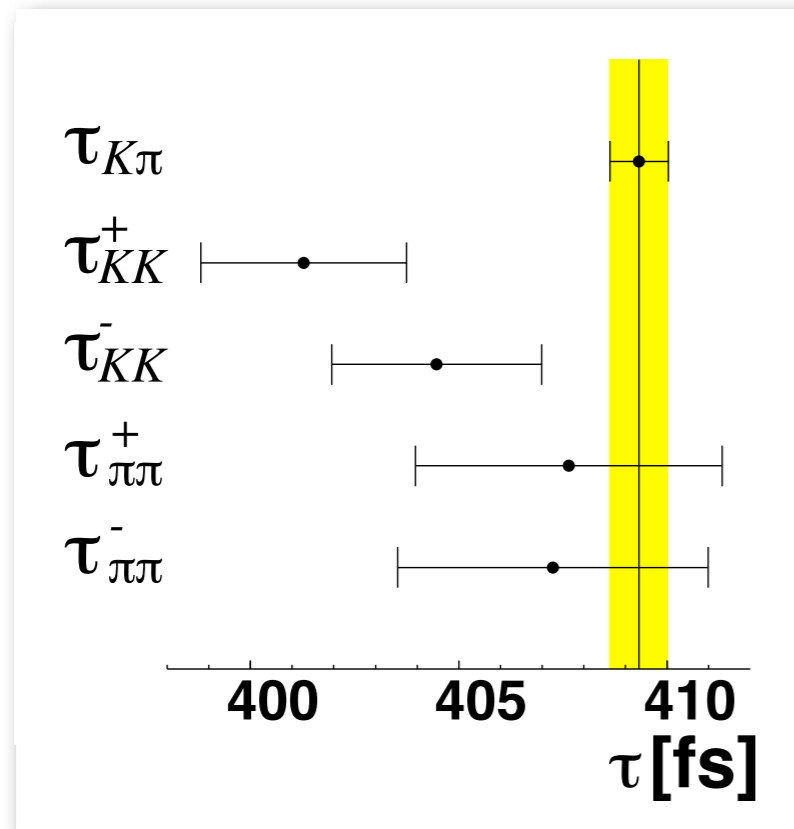
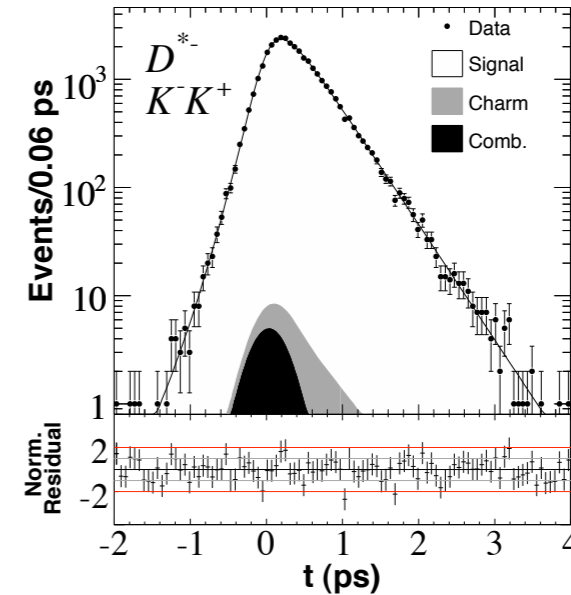
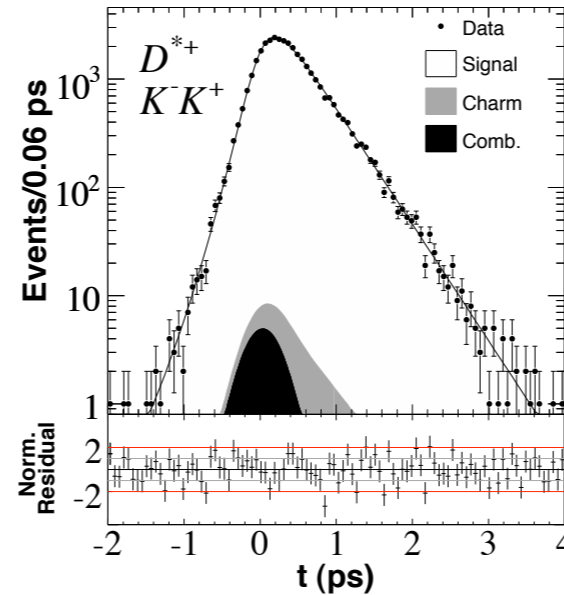
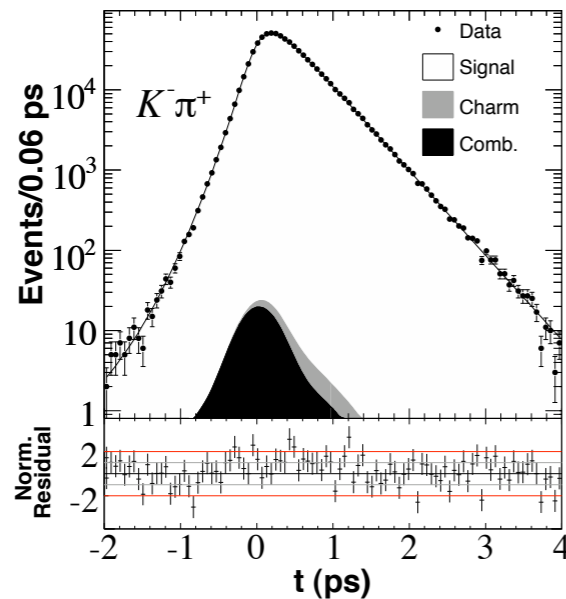
- Background events may contain effects differing in each mode
- Event selection is chosen for high purity
- e.g. require  $|\delta m - q_0| < 0.8 \text{ MeV}/c^2$

$q_0 = 145.4 \text{ MeV}/c^2$ : nominal value for  $D^{*+} - D^0$  mass difference ( $\delta m$ )

Sample	Size	Purity (%)
$K^- \pi^+$	730,880	99.9
$K^- K^+$	69,696	99.6
$\pi^- \pi^+$	30,679	98.0



# $D^0$ mixing - by lifetime difference



\* BaBar's  $A_{\Gamma}$  def. is opposite to Belle's

Sample	$y_{CP}$	$\Delta Y$
$K^- K^+$	$(1.60 \pm 0.46 \pm 0.17)\%$	$(-0.40 \pm 0.44 \pm 0.12)\%$
$\pi^- \pi^+$	$(0.46 \pm 0.65 \pm 0.25)\%$	$(0.05 \pm 0.64 \pm 0.32)\%$
Combined	$(1.24 \pm 0.39 \pm 0.13)\%$	$(-0.26 \pm 0.36 \pm 0.08)\%$



# D<sup>0</sup> mixing - by lifetime difference

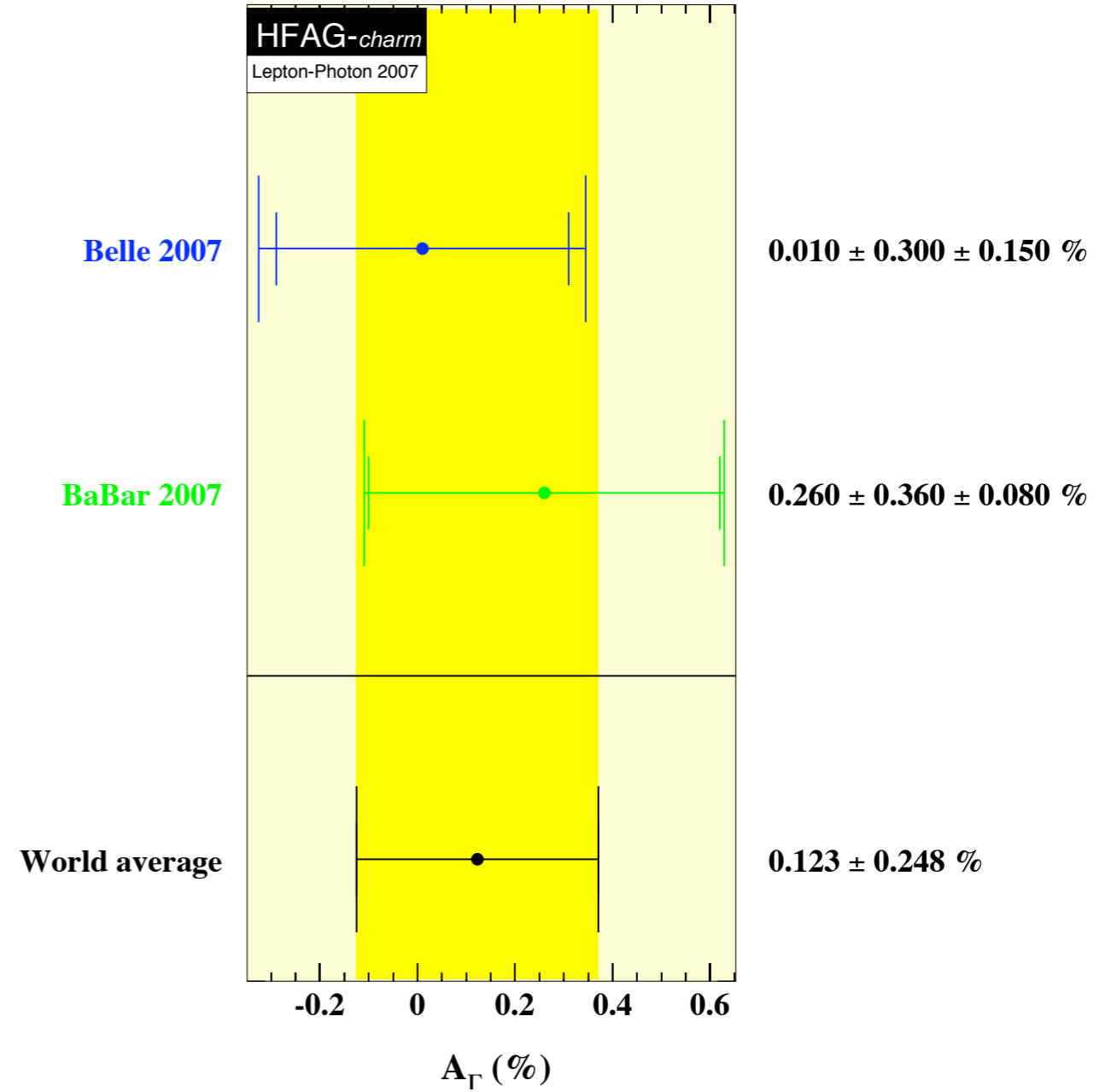
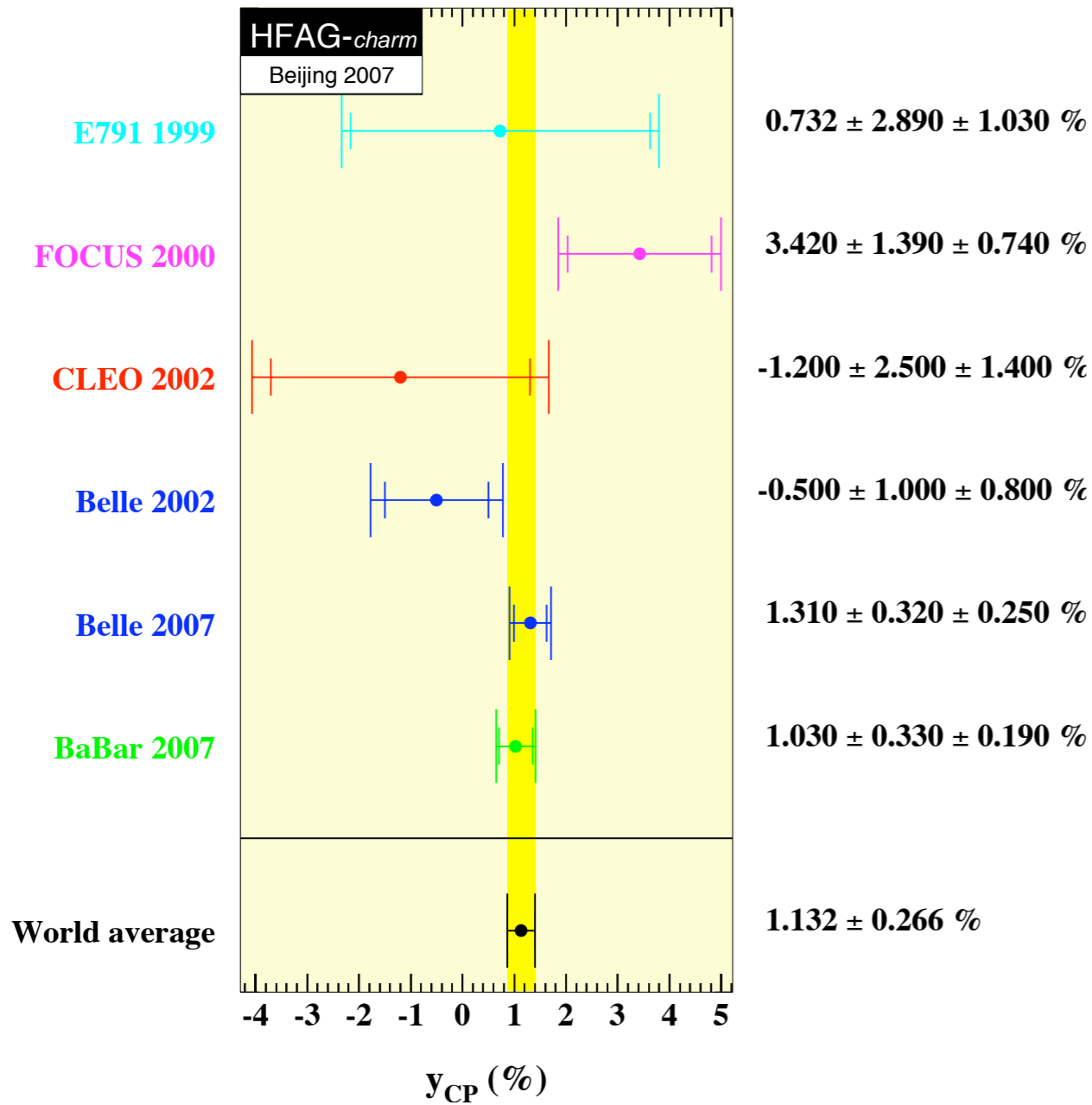
Systematic	$\sigma_{y_{CP}} (\%)$			$\sigma_{\Delta Y} (\%)$		
	$K^- K^+$	$\pi^- \pi^+$	Av.	$K^- K^+$	$\pi^- \pi^+$	Av.
Signal model	0.130	0.059	0.085	0.072	0.265	0.062
Charm bkg.	0.062	0.037	0.043	0.001	0.002	0.001
Combinatoric bkg.	0.019	0.142	0.045	0.001	0.005	0.002
Selection criteria	0.068	0.178	0.046	0.083	0.172	0.011
Detector model	0.064	0.080	0.064	0.054	0.040	0.054
Quadrature sum	0.172	0.251	0.132	0.122	0.318	0.083

- Syst. error on the average can be smaller than the individual ones because of anti-correlations.
- Combined with the previous analysis (of untagged sample,  $91 \text{ fb}^{-1}$ ), improve stat. error for  $y_{CP}$ :

$$y_{CP} = (1.03 \pm 0.33 \pm 0.19)\%$$

$$\text{cf. } y_{CP} = (1.24 \pm 0.39 \pm 0.13)\% \text{ (this analysis only)}$$

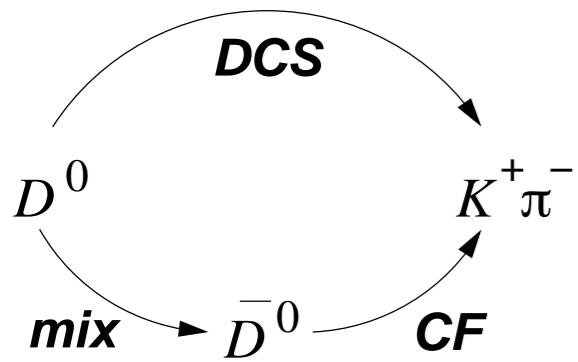
# D<sup>0</sup> mixing - by lifetime difference



# D<sup>0</sup> mixing - by $D^0(t) \rightarrow K^+ \pi^-$

## Master formula

$$|\langle f | H | D^0(t) \rangle|^2 \propto e^{-\bar{\Gamma}t} \left\{ 1 + (y\mathcal{R}(\lambda) - x\mathcal{I}(\lambda)) \bar{\Gamma}t + |\lambda|^2 \frac{x^2 + y^2}{4} (\bar{\Gamma}t)^2 \right\}$$



for  $f = K^+ \pi^-$  (wrong-sign),

$$\lambda = \frac{q \bar{\mathcal{A}}_f}{p \mathcal{A}_f} = \left| \frac{q}{p} \right| \sqrt{R_D} e^{i(\phi + \delta)}$$

$\delta$  : strong phase b/w DCS & CF

$$\propto e^{-\bar{\Gamma}t} \left\{ R_D + \left| \frac{q}{p} \right| \sqrt{R_D} [y \cos(\phi + \delta) - x \sin(\phi + \delta)] (\bar{\Gamma}t) + \left| \frac{q}{p} \right|^2 \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\}$$

$$= e^{-\bar{\Gamma}t} \left\{ R_D + \sqrt{R_D} (y \cos \delta - x \sin \delta) (\bar{\Gamma}t) + \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\} \quad \left( \begin{array}{l} |q/p| = 1 \\ \phi = 0 \end{array} \right)$$

no CPV

$$= e^{-\bar{\Gamma}t} \left\{ R_D + \sqrt{R_D} y' (\bar{\Gamma}t) + \frac{(x'^2 + y'^2)}{4} (\bar{\Gamma}t)^2 \right\}$$

$$x' \equiv x \cos \delta + y \sin \delta \quad y' \equiv y \cos \delta - x \sin \delta$$



# D<sup>0</sup> mixing - by $D^0(t) \rightarrow K^+ \pi^-$

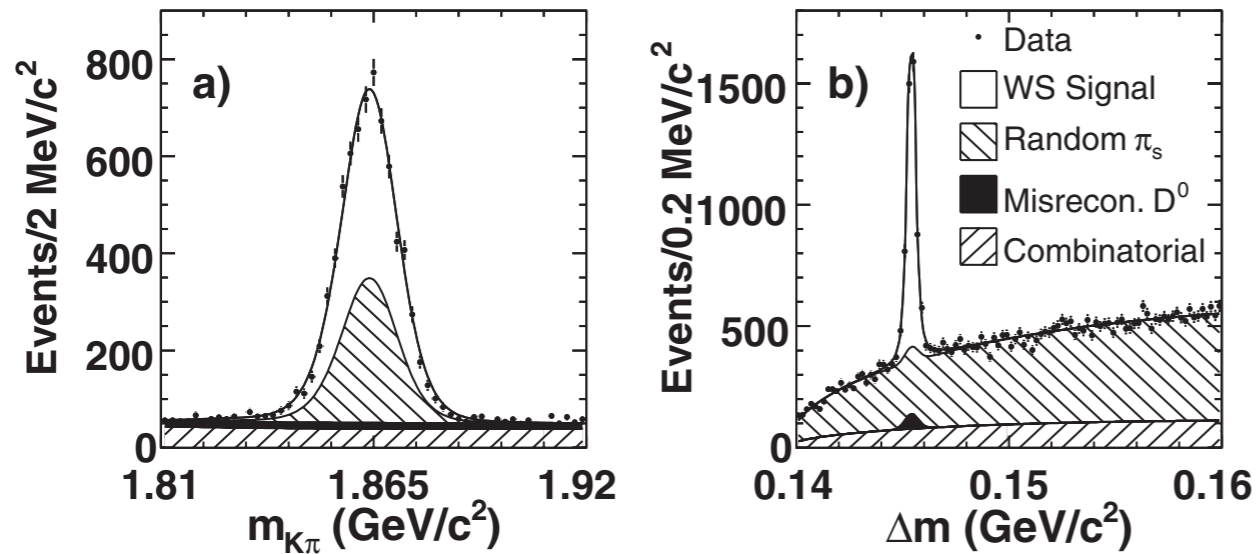
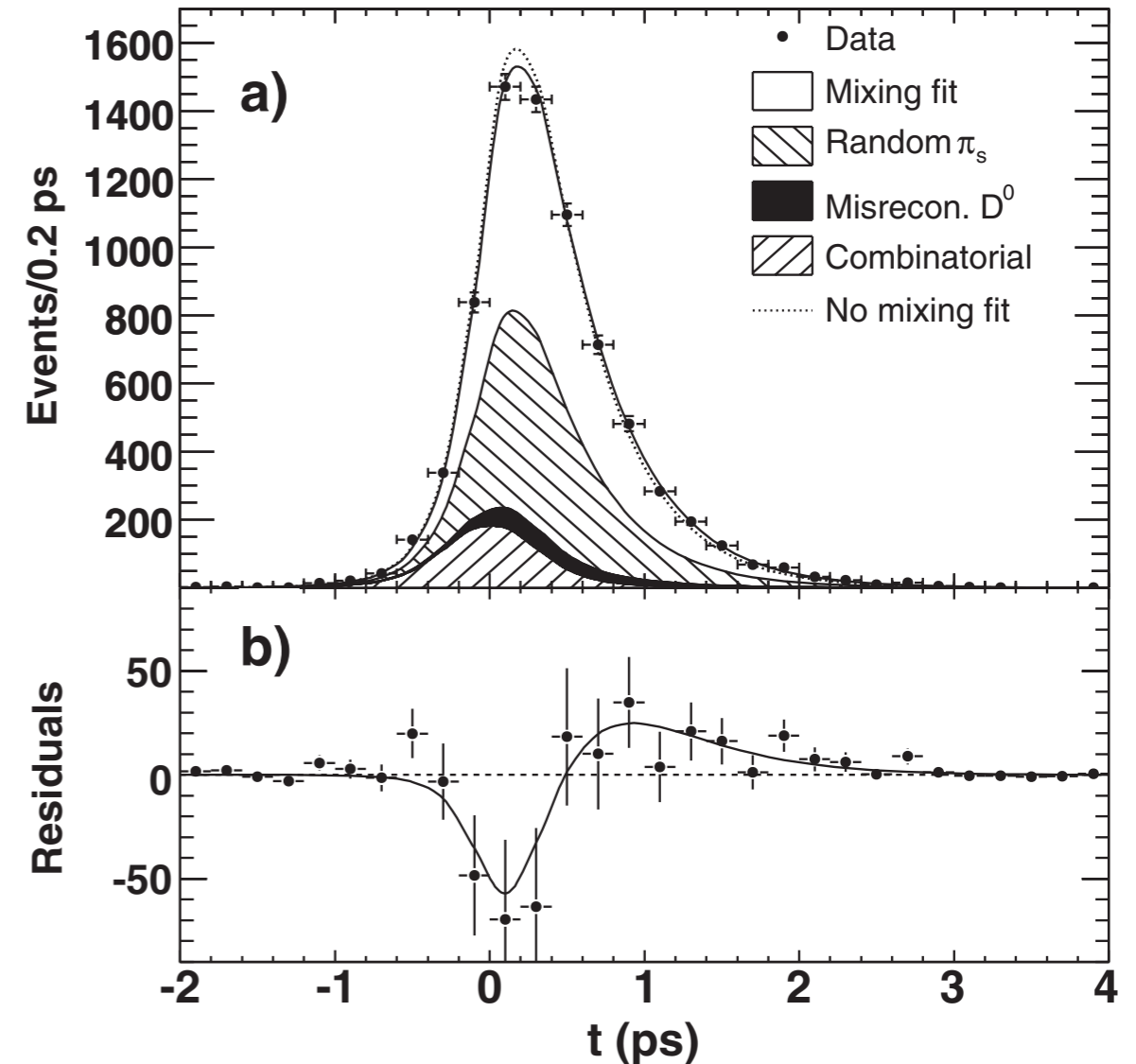


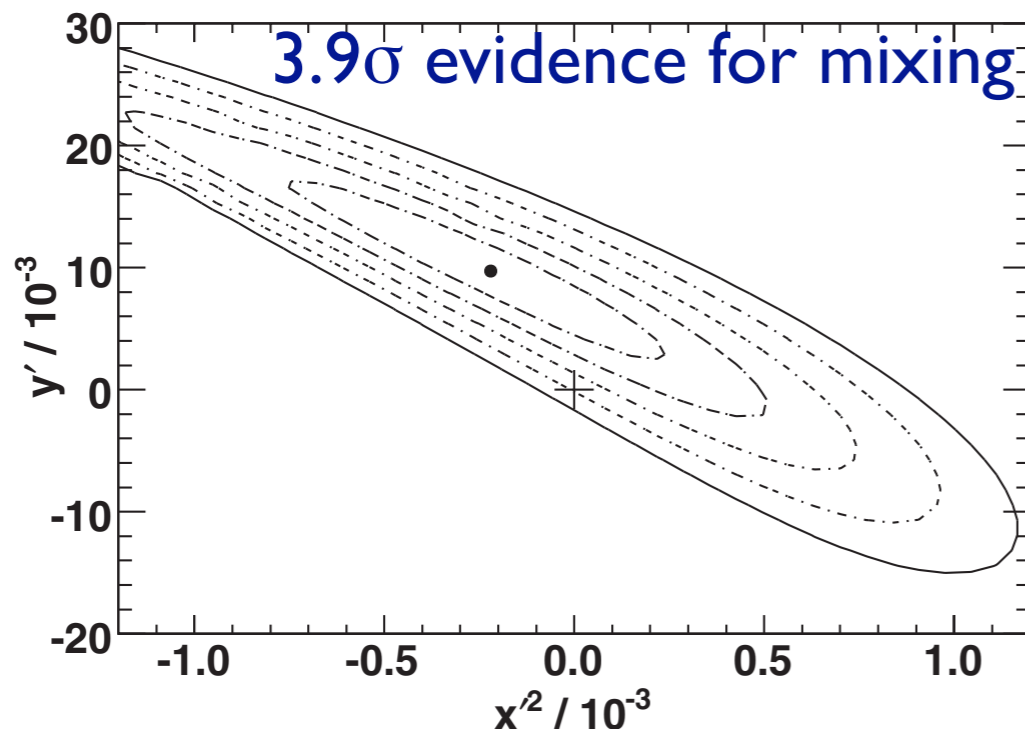
FIG. 1. (a)  $m_{K\pi}$  for WS candidates with  $0.1445 < \Delta m < 0.1465 \text{ GeV}/c^2$  and (b)  $\Delta m$  for WS candidates with  $1.843 < m_{K\pi} < 1.883 \text{ GeV}/c^2$ . The fitted PDFs are overlaid.



for combined WS candidates

$$y' = (0.97 \pm 0.44 \pm 0.31)\%$$

$$R_D = (0.303 \pm 0.016 \pm 0.010)\%$$



# $D^0$ mixing - by $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$

## Master formula

$$\begin{aligned}\langle K_S^0 \pi^+ \pi^- | H | D^0(t) \rangle &= \frac{1}{2p} (\langle K_S^0 \pi^+ \pi^- | H | D_1(t) \rangle + \langle K_S^0 \pi^+ \pi^- | H | D_2(t) \rangle) \\ &= A_1 e^{-(\Gamma_1/2 + im_1)t} + A_2 e^{-(\Gamma_2/2 + im_2)t}\end{aligned}$$

$$\begin{aligned}|\langle K_S^0 \pi^+ \pi^- | H | D^0(t) \rangle|^2 &= |A_1|^2 e^{-\bar{\Gamma}(1+y)t} + |A_2|^2 e^{-\bar{\Gamma}(1-y)t} \\ &\quad + 2e^{-\bar{\Gamma}t} [\mathcal{R}(A_1 A_2^*) \cos xt - \mathcal{I}(A_1 A_2^*) \sin xt]\end{aligned}$$

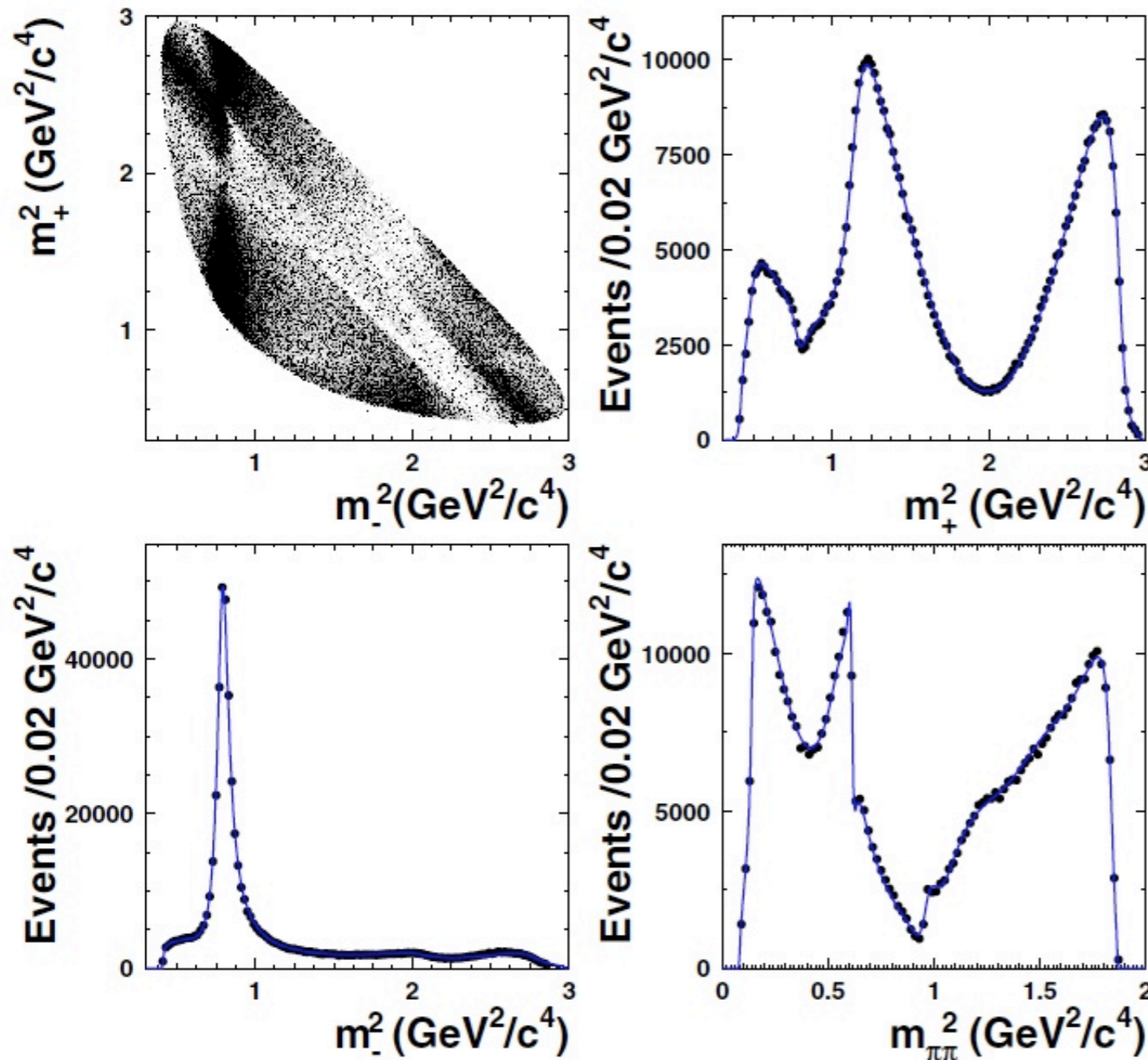
- The amplitudes  $A_j$  are functions of Dalitz plot (DP) variables  $m_+^2 = m^2(K_S^0 \pi^+)$  and  $m_-^2 = m^2(K_S^0 \pi^-)$  and account for intermediate states.
- The amplitude as a ftn. of  $m_+^2$  and  $m_-^2$  is expressed as a sum of quasi-2-body amplitudes and a const. non-res. term.
- The  $t$ -dependent decay amplitude is fitted over the DP and the mixing param's. are extracted.



# $D^0$ mixing - by $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$

$$\mathcal{A}(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) + a_{\text{NR}} e^{i\phi_{\text{NR}}}$$

$$\bar{\mathcal{A}}(m_-^2, m_+^2) = \sum_r \bar{a}_r e^{i\bar{\phi}_r} \mathcal{A}_r(m_+^2, m_-^2) + \bar{a}_{\text{NR}} e^{i\bar{\phi}_{\text{NR}}}$$



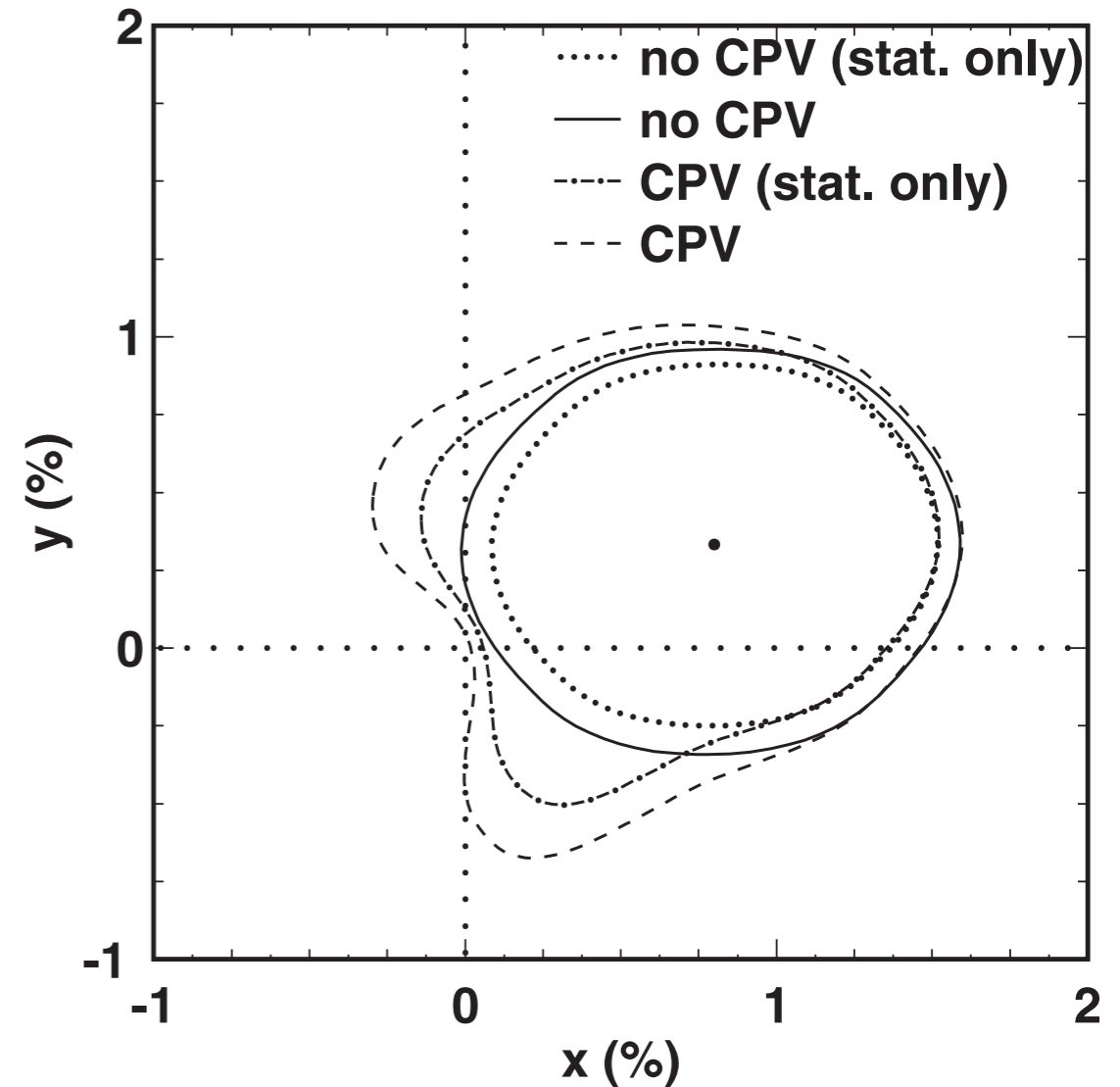
# $D^0$ mixing - by $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$

$$\mathcal{L} = \prod_{i=1}^{N_{D^0}} \sum_j f_j(m_{K_S^0 \pi \pi, i}, Q_i) \mathcal{P}_j(m_{-, i}^2, m_{+, i}^2, t_i)$$

Determine  $x, y$ , by maximizing  $\ln \mathcal{L} + \ln \bar{\mathcal{L}}$

Fit case	Parameter	Fit result	95% C.L. interval
No	$x(\%)$	$0.80 \pm 0.29^{+0.09+0.10}_{-0.07-0.14}$	(0.0, 1.6)
CPV	$y(\%)$	$0.33 \pm 0.24^{+0.08+0.06}_{-0.12-0.08}$	(-0.34, 0.96)
CPV	$x(\%)$	$0.81 \pm 0.30^{+0.10+0.09}_{-0.07-0.16}$	$ x  < 1.6$
	$y(\%)$	$0.37 \pm 0.25^{+0.07+0.07}_{-0.13-0.08}$	$ y  < 1.04$
	$ q/p $	$0.86^{+0.30+0.06}_{-0.29-0.03} \pm 0.08$	...
	$\arg(q/p)(^\circ)$	$-14^{+16+5+2}_{-18-3-4}$	...

**CL. for no mixing = 2.6%**



# $D^0$ mixing - by $D^0 \rightarrow K^{(*)} \ell^+ \nu$

- semileptonic decays, with no DCS contribution, gives direct access to mixing rate  $R_M$

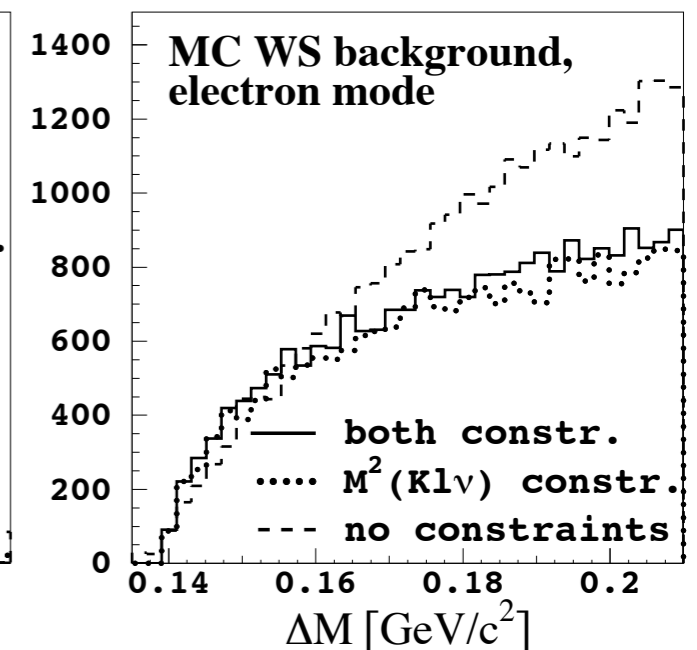
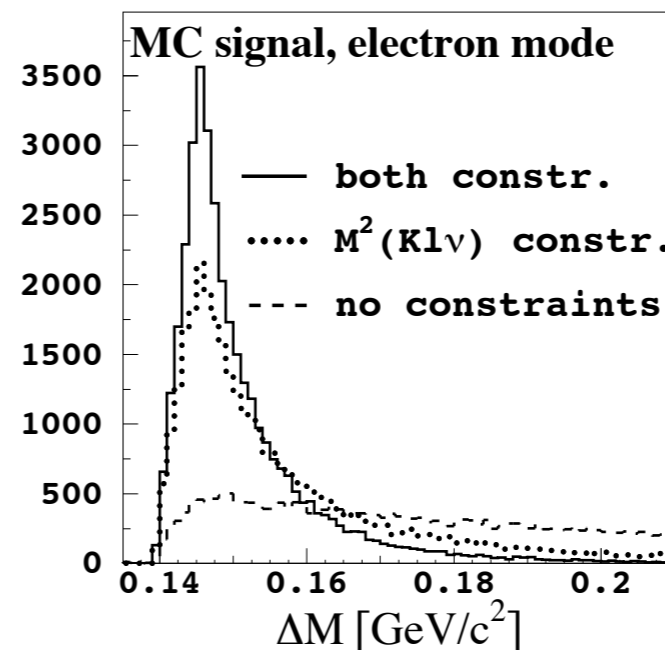
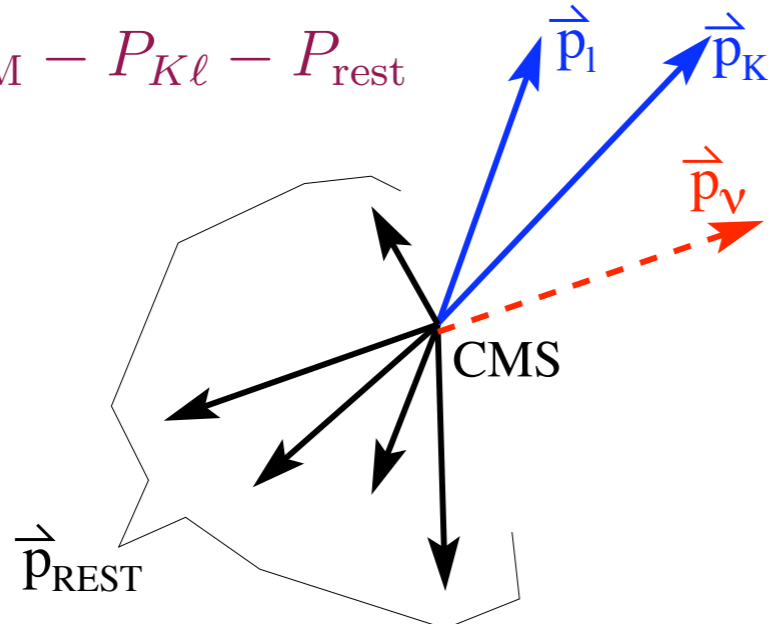
$$\mathcal{P}(D^0 \rightarrow \bar{D}^0 \rightarrow X^+ \ell^- \bar{\nu}_\ell) \propto R_M t^2 e^{-\Gamma t}$$

$$R_M = \frac{\int_0^\infty dt \mathcal{P}(D^0 \rightarrow \bar{D}^0 \rightarrow X^+ \ell^- \bar{\nu}_\ell)}{\int_0^\infty dt \mathcal{P}(D^0 \rightarrow X^- \ell^+ \nu_\ell)} \approx \frac{x^2 + y^2}{2}$$

- select  $D^0 \rightarrow K^- \ell^+ \nu$  ( $\ell = e, \mu$ ) from  $D^{*+} \rightarrow D^0 \pi^+$
- search for signals in  $\Delta M \equiv M(\pi_s K \ell \nu) - M(K \ell \nu)$

Require  $M_{K\ell\nu}^2 = m_{D^0}^2$  and  $(P_\nu^*)^2 = 0$

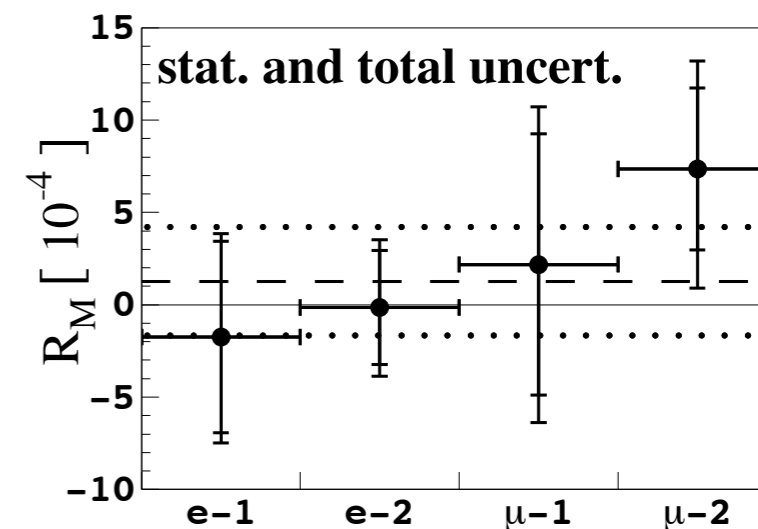
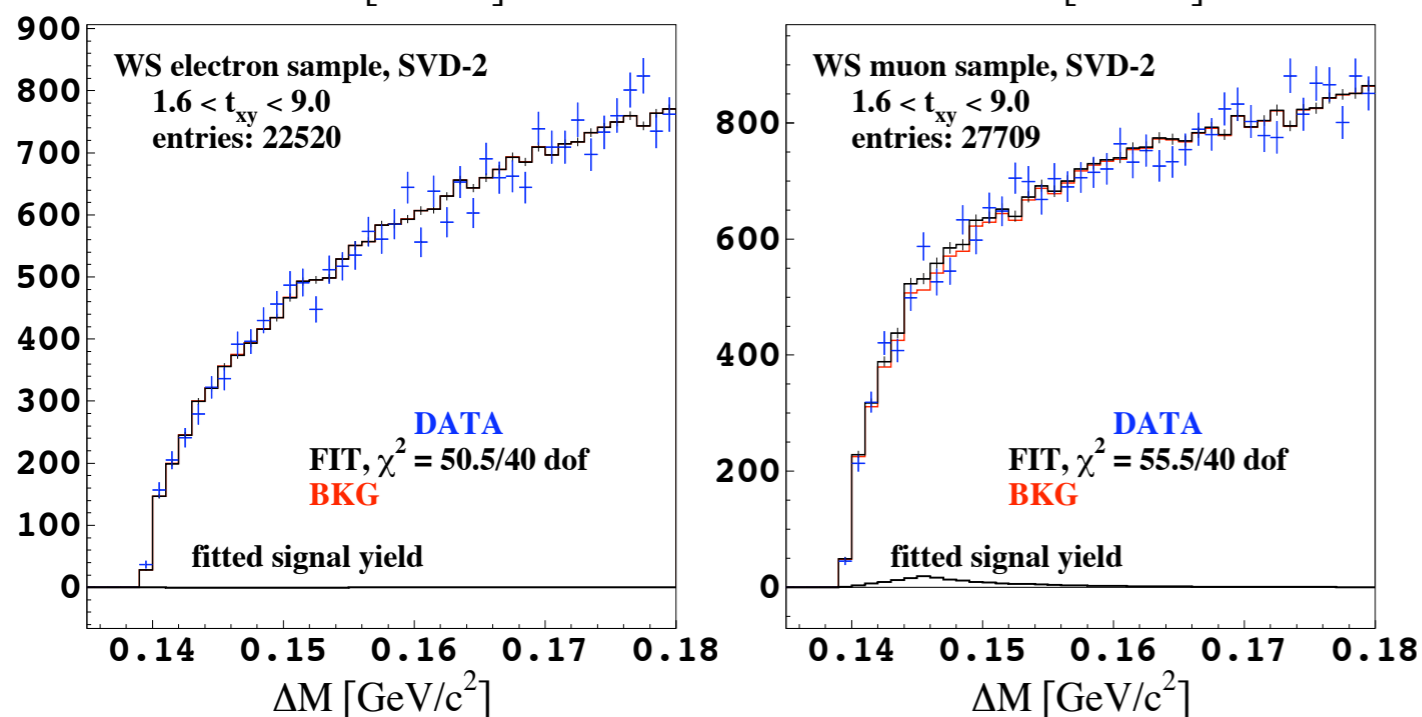
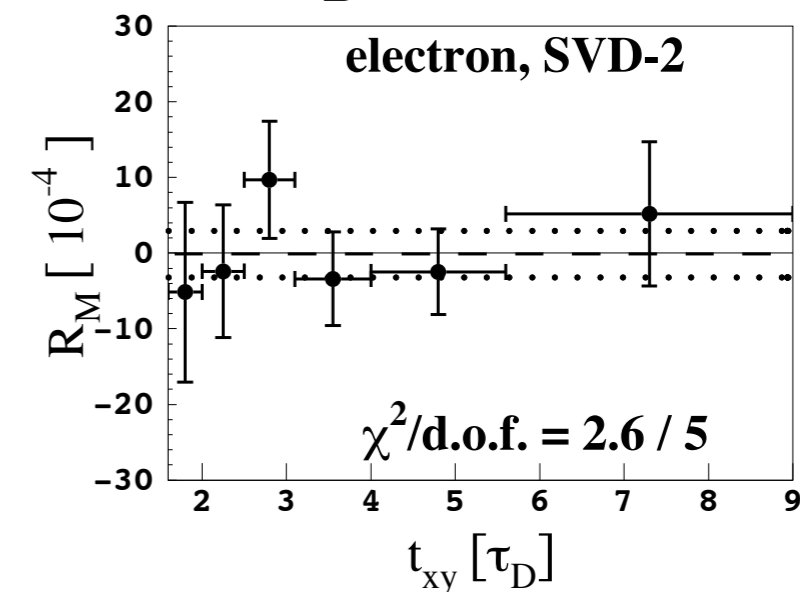
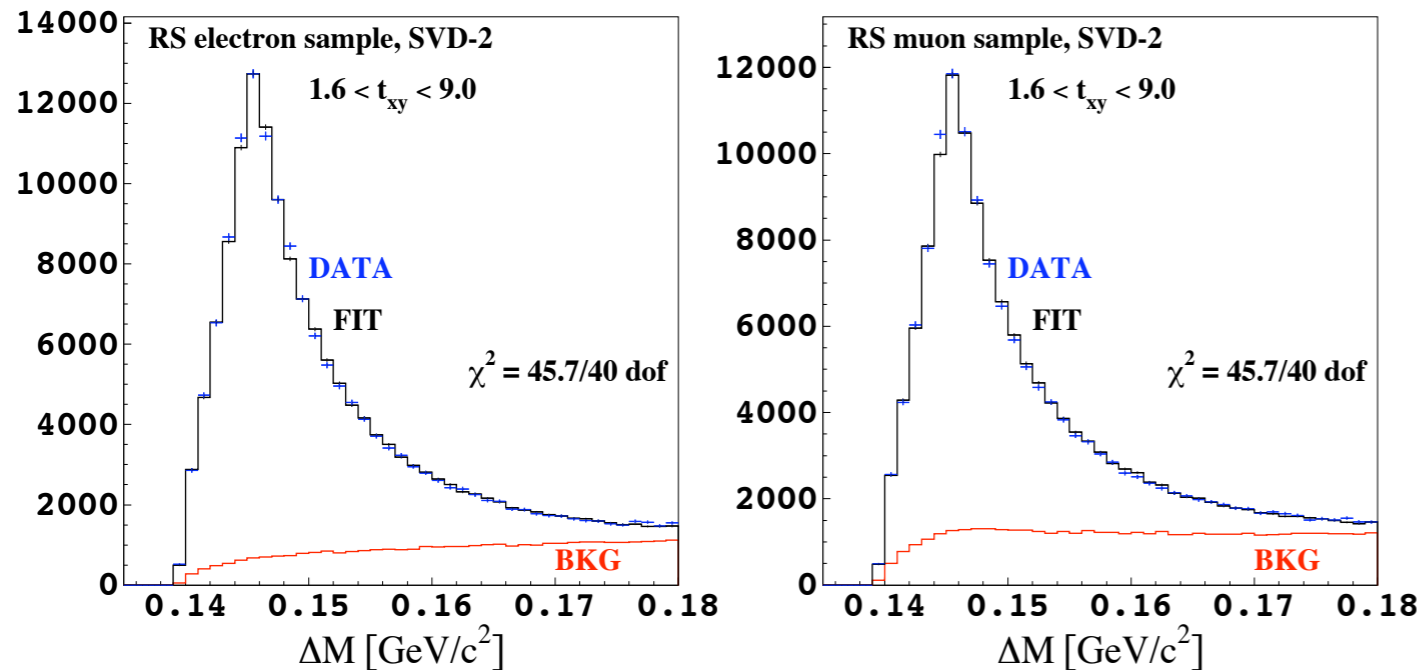
$$P_\nu = P_{\text{CM}} - P_{K\ell} - P_{\text{rest}}$$



# $D^0$ mixing - by $D^0 \rightarrow K^{(*)} \ell^+ \nu$

$$\Delta M \equiv M(\pi_s K \ell \nu) - M(K \ell \nu)$$

$t_{xy}$  : proper decay time in  $xy$  plane  
normalized to  $\tau_{D^0}$



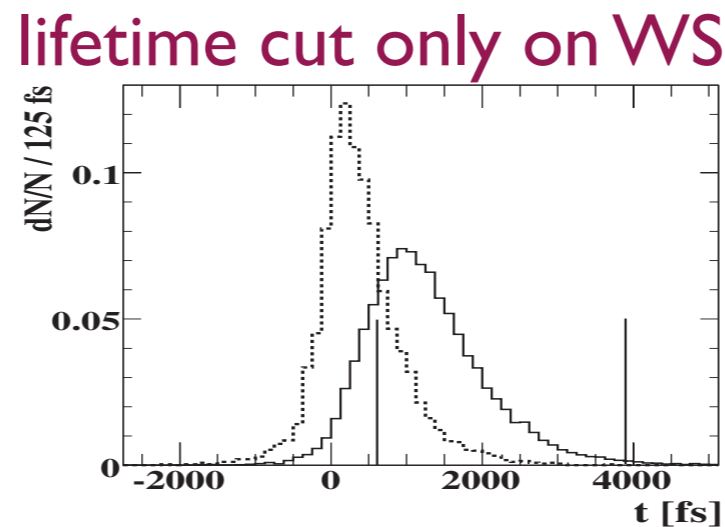
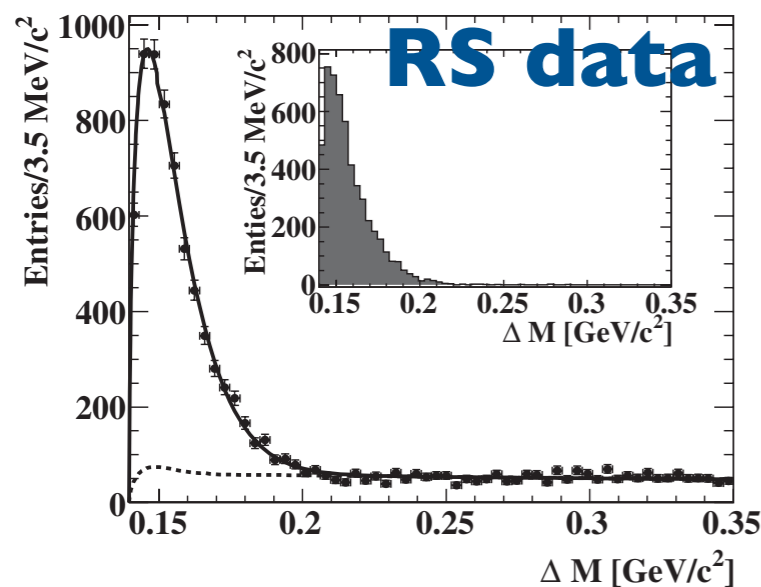
$$R_M = (1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$$

$$< 6.1 \times 10^{-4} \quad @ 90\% \text{ CL}$$



# D<sup>0</sup> mixing - by $D^0 \rightarrow K^{(*)} \ell^+ \nu$

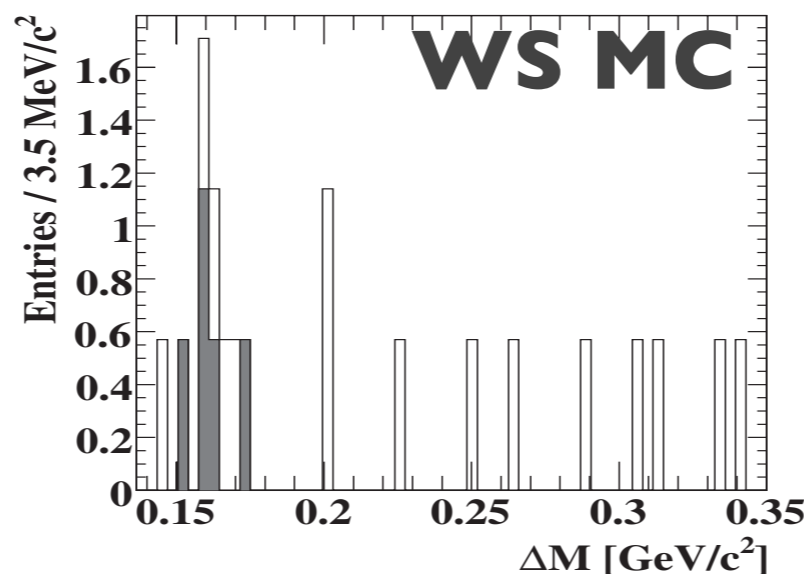
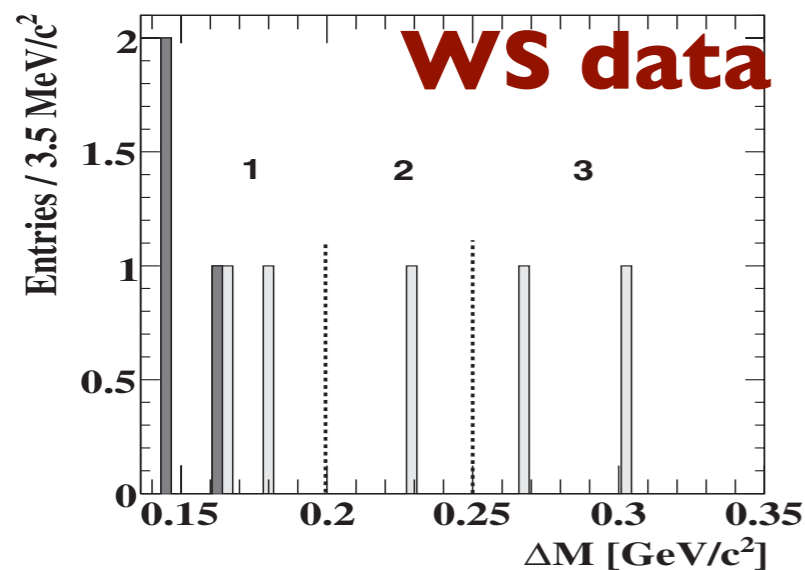
- full reconstruction of the opposite side (“double-tagging”)
- neural-network selection based on  $p_\pi$ ,  $p_{Ke}$ , thrust axis, opening angle
- “signal yield” by counting ; backg’d estimate comes from MC



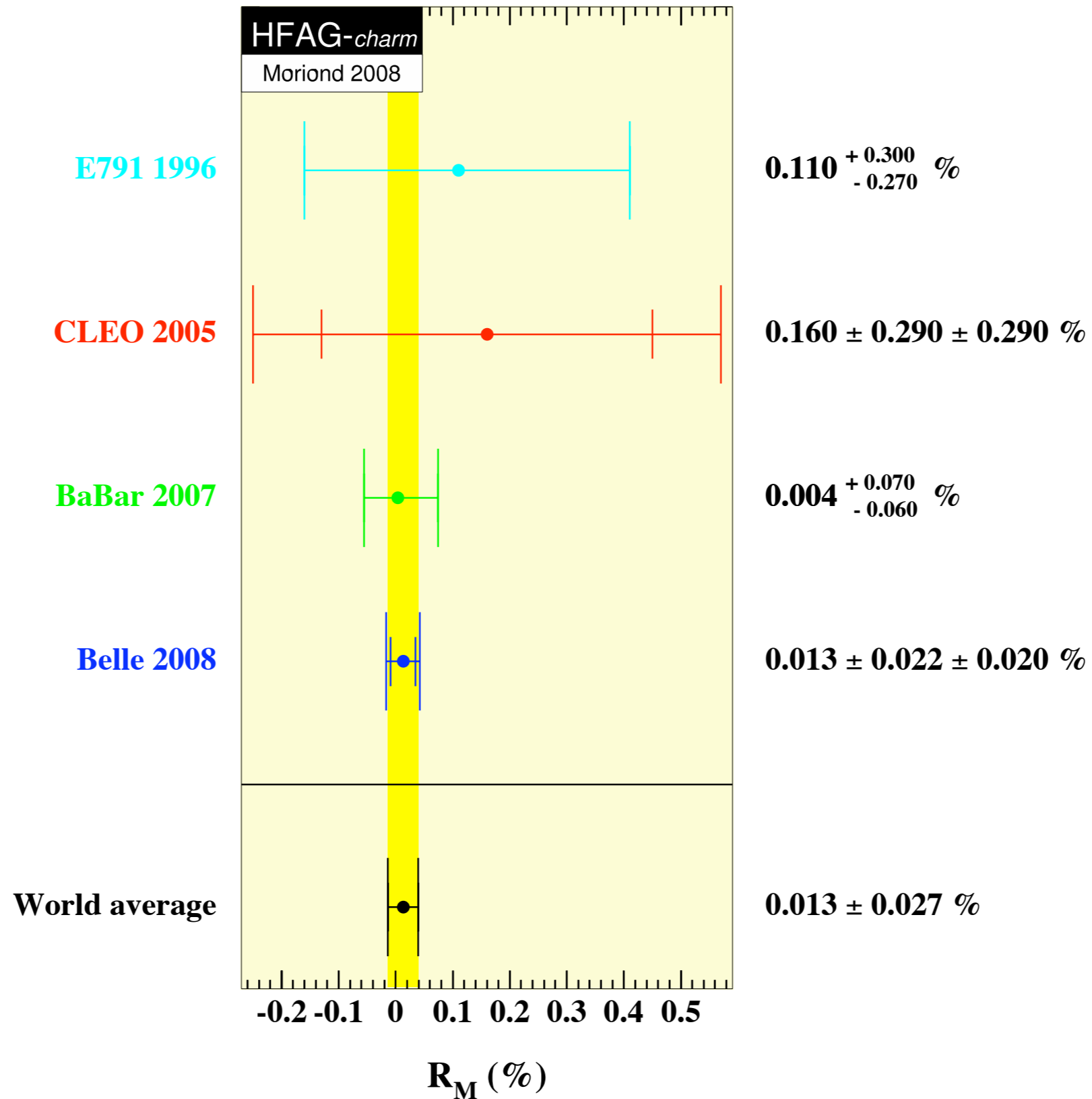
determine confidence interval by rise of Likelihood ftn.

$$R_M = (-13, 12) \times 10^{-4}$$

@ 90% CL



# $D^0$ mixing - by $D^0 \rightarrow K^{(*)} \ell^+ \nu$



# CP violation in $D^0$

- time-integrated asymmetry:  $A_{CP} = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$ 
  - in decays
  - in mixing
  - in interference b/w mixing & decays
- for  $f = K^- K^+, \pi^- \pi^+$ :  $A_{CP} \sim \mathcal{O}(10^{-5} - 10^{-4})$
- for  $f = \pi^- \pi^+ \pi^0$ :  $A_{CP} \sim \mathcal{O}(10^{-3})$
- Principle of measurements
  - $D^{*+} \rightarrow D^0 \pi_s^+$
  - $N_{D^0}^{\text{reco}} = N_{D^{*+}}^{\text{prod}} \cdot \mathcal{B}(D^{*+} \rightarrow D^0 \pi^+) \cdot \mathcal{B}(D^0 \rightarrow f) \cdot \epsilon_f \cdot \epsilon_{\pi_s}$
  - contributions to measured asymmetry:  
 $A^{\text{meas}} = A_{FB} + A_{CP} + A_\epsilon^\pi$

# $D^0$ CPV - exp'tal results

$\exists$  *several searches for CPV using*

 In singly Cabibbo-suppressed modes

- preliminary

- PRL 100, 061803

 In 3-body modes

- 0801.2439

- 0802.4035







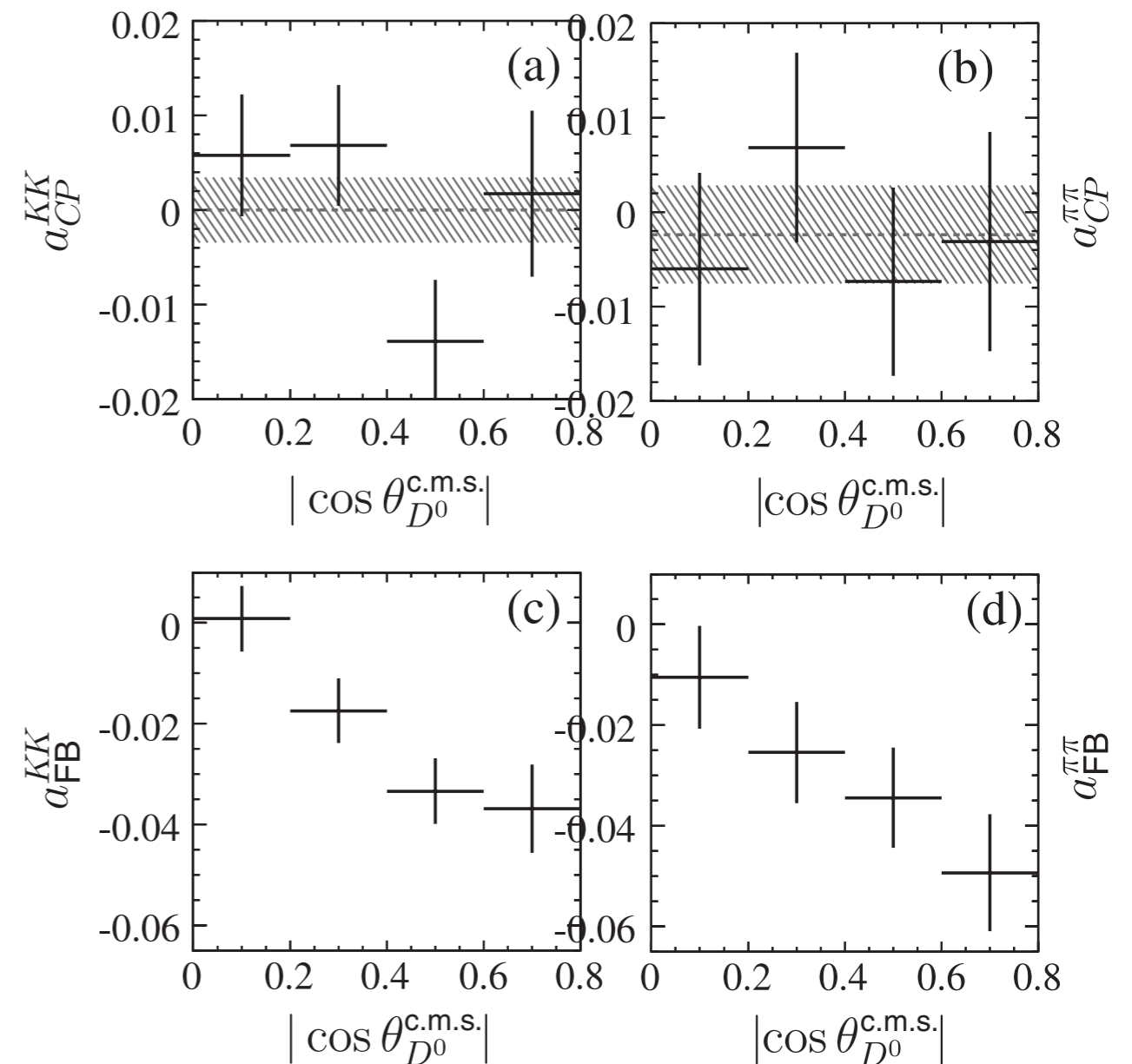
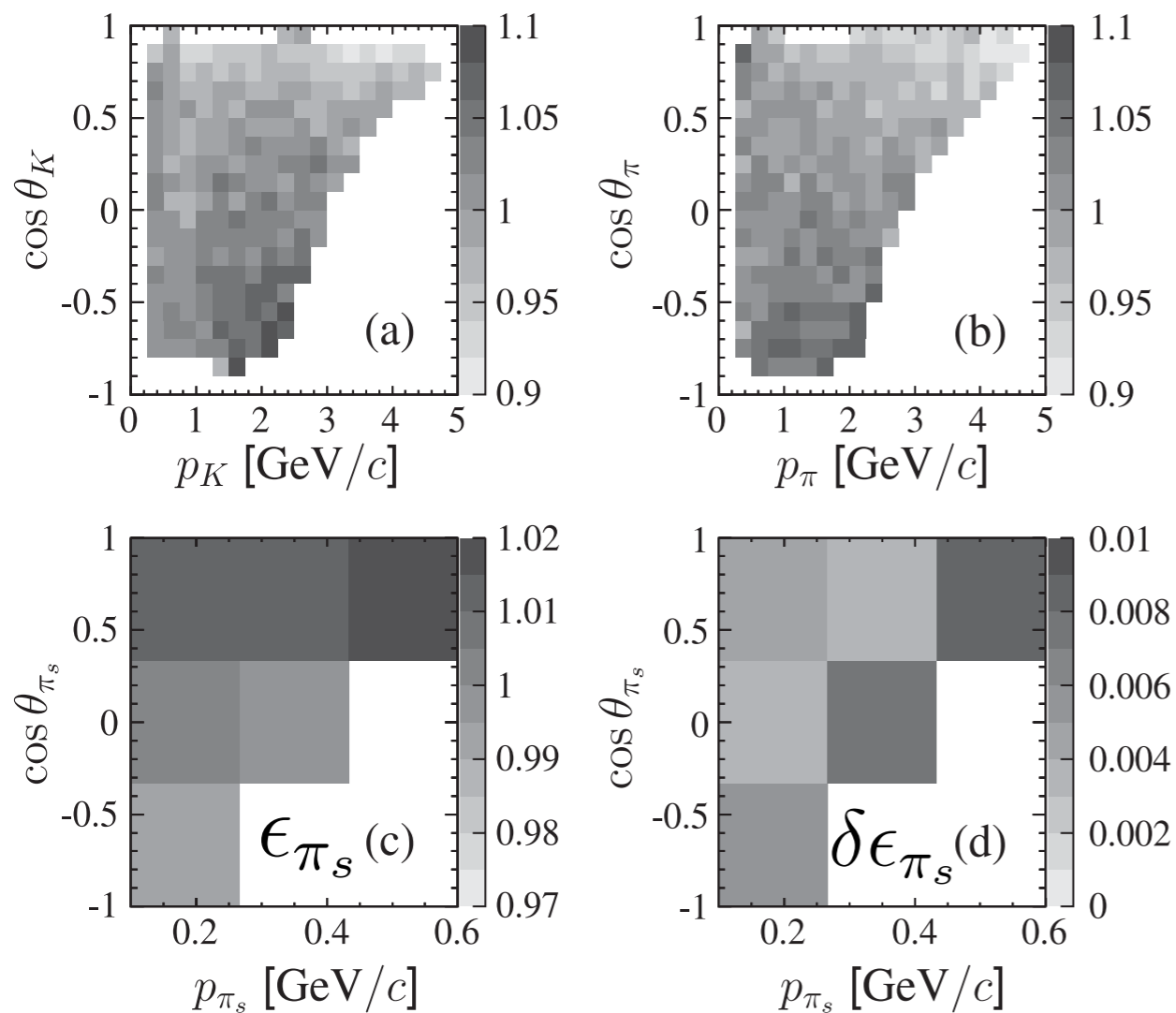
# CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$

$$A_{\text{corr}}^{\text{rec}}(\cos \theta^*) = A_{FB}^{D^*} + A_{CP}^{h^+h^-}$$

$$A_{CP} = \frac{A_{\text{corr}}^{\text{rec}}(\cos \theta^*) + A_{\text{corr}}^{\text{rec}}(-\cos \theta^*)}{2}$$

$$A_{FB} = \frac{A_{\text{corr}}^{\text{rec}}(\cos \theta^*) - A_{\text{corr}}^{\text{rec}}(-\cos \theta^*)}{2}$$

*efficiency map*



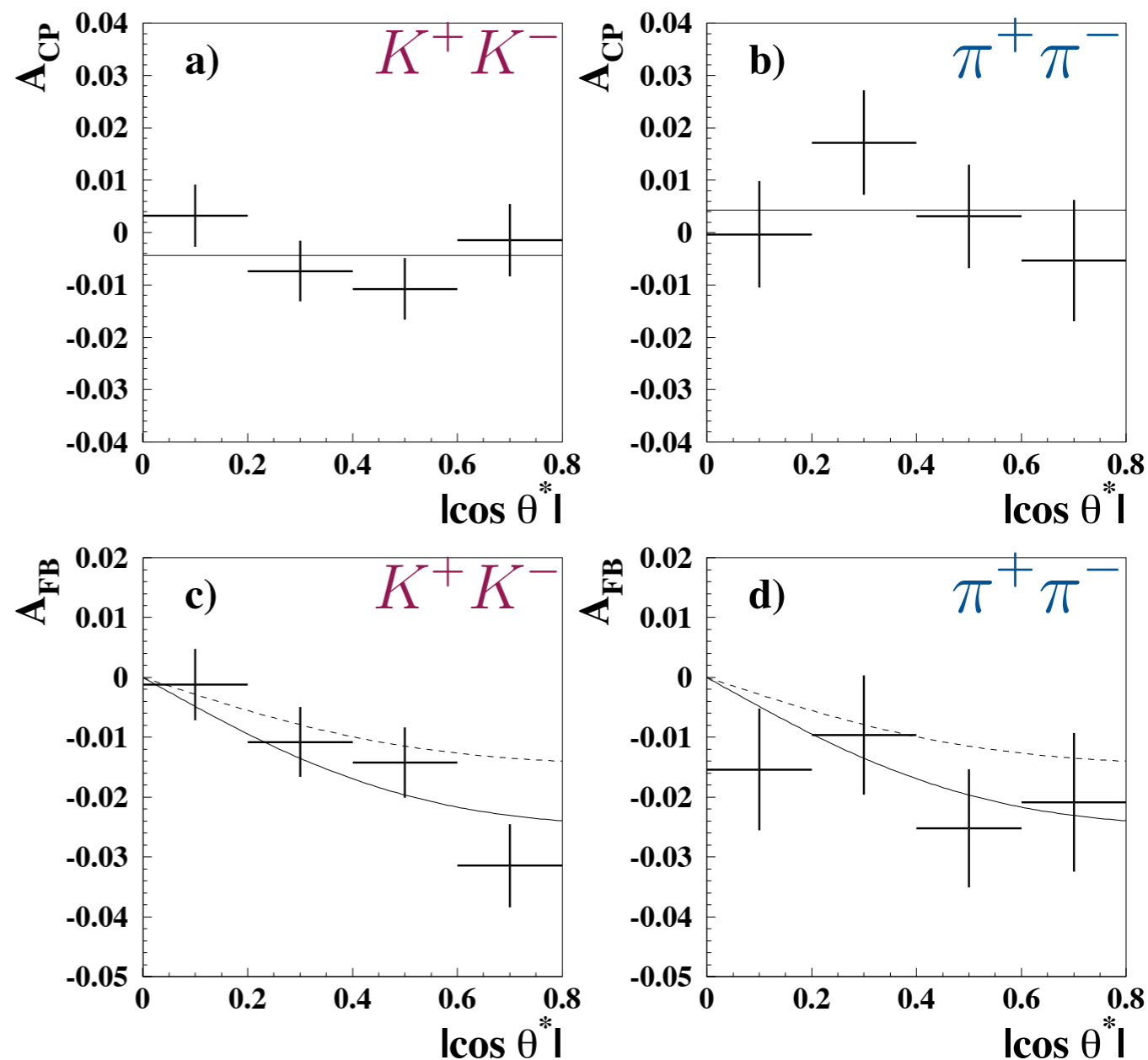
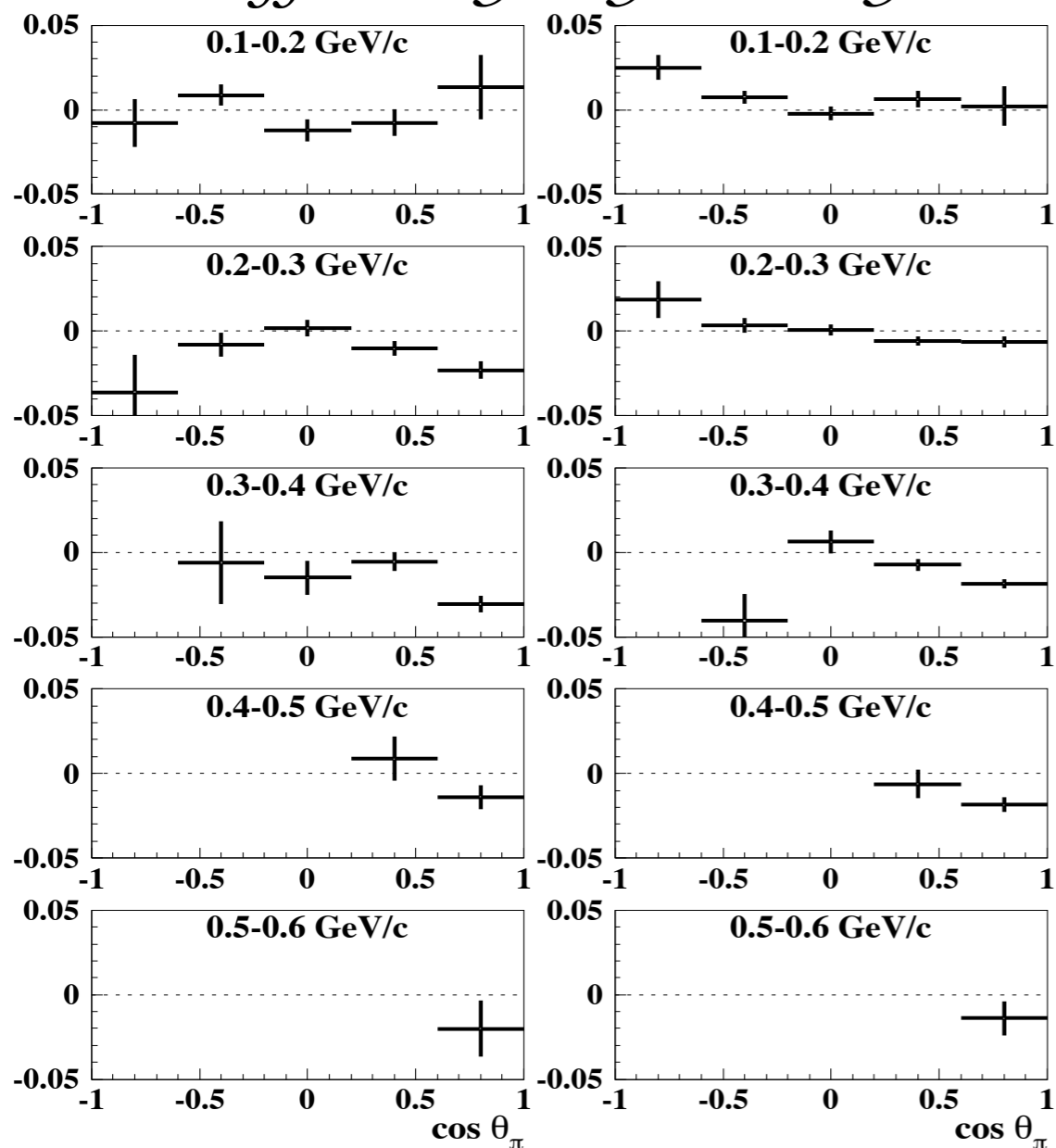
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## $\pi_s$ efficiency asymmetry



# CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$



$$A_{CP}^{KK} = (-0.41 \pm 0.30 \pm 0.11) \%$$

$$A_{CP}^{KK} = (0.00 \pm 0.34 \pm 0.13) \%$$

$$A_{CP}^{\pi\pi} = (+0.41 \pm 0.52 \pm 0.12) \%$$

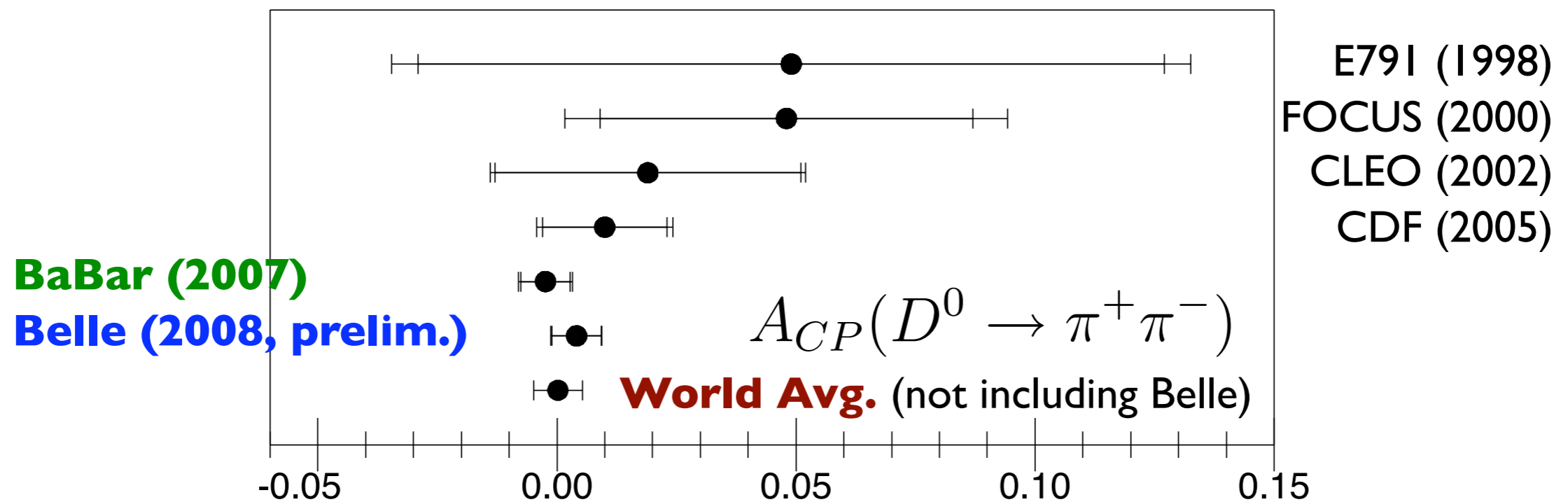
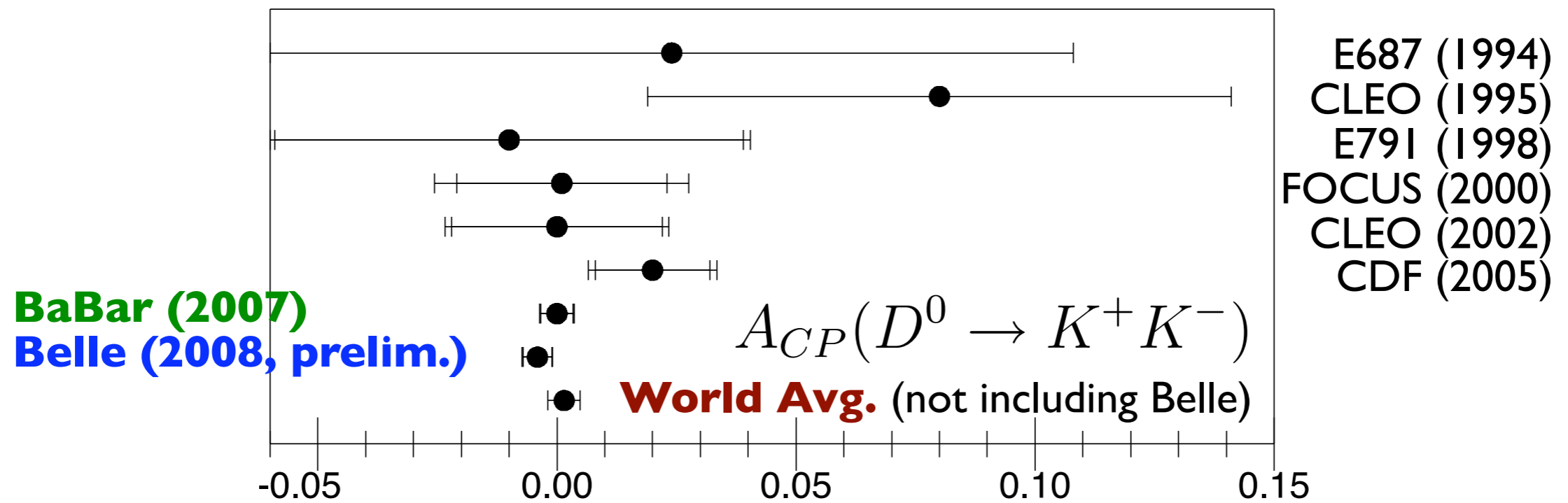
$$A_{CP}^{\pi\pi} = (-0.24 \pm 0.52 \pm 0.22) \%$$

Summary of systematic uncertainties of  $A_{CP}$ .

Source	$D^0 \rightarrow K^+K^-$	$D^0 \rightarrow \pi^+\pi^-$
Signal counting	0.04%	0.06%
Slow pion corrections	0.10%	0.10%
$A_{CP}$ extraction	0.03%	0.04%
Quadrature sum	0.11%	0.12%

Syst. err. will improve w/ more  $D^*$  sample

# CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$



# CPV in 3-body SCS $D^0$ decays

 In singly Cabibbo-suppressed 3-body  $D^0$  modes

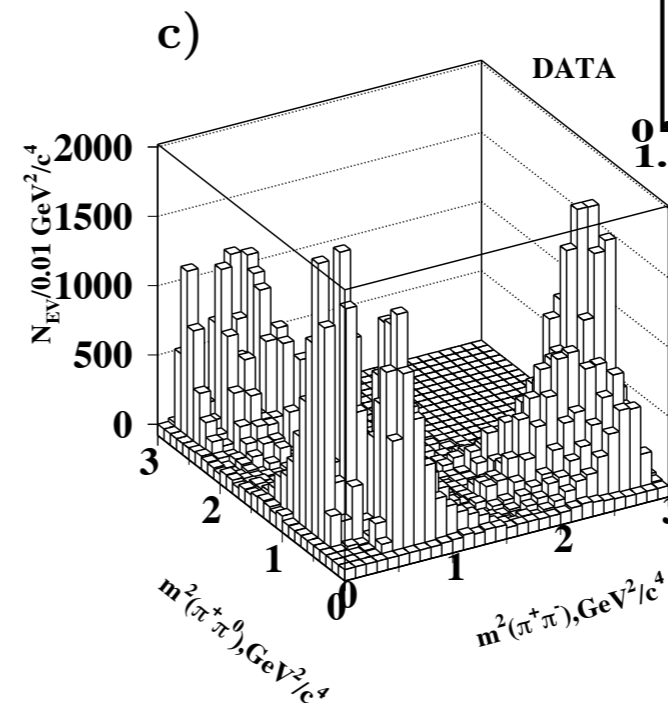
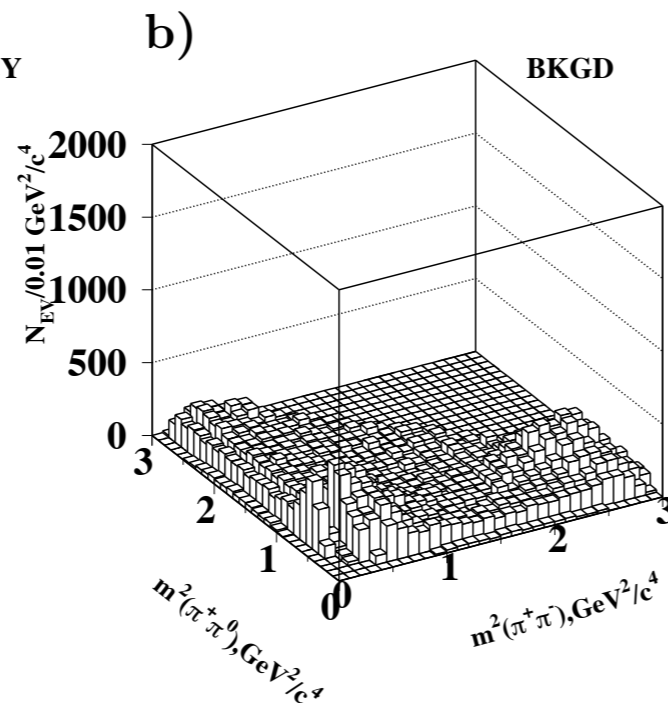
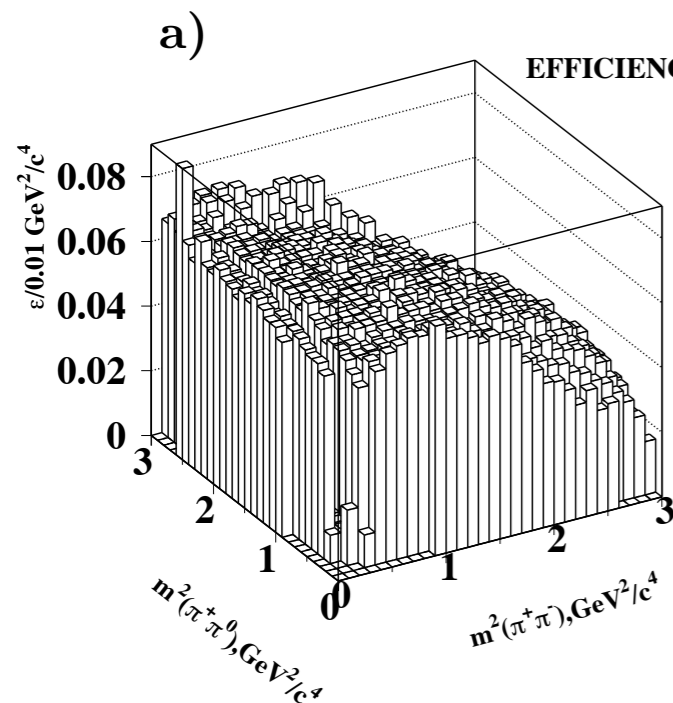
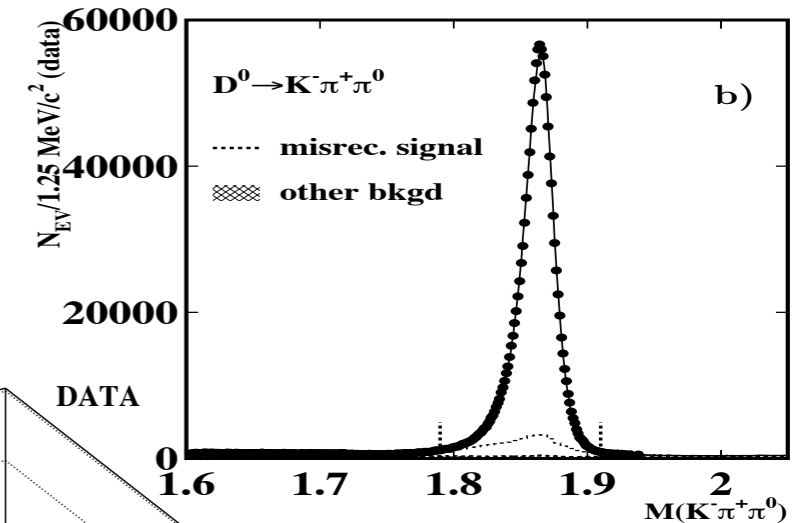
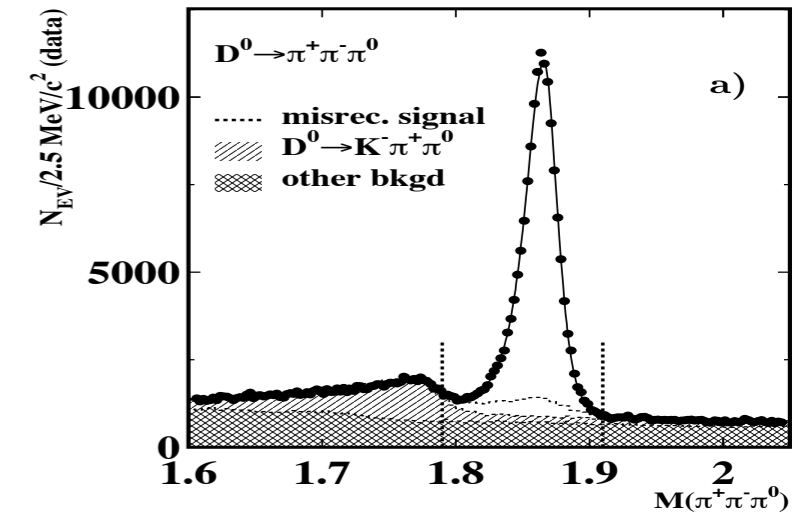
- $D^0 \rightarrow \pi^+ \pi^- \pi^0, K^+ K^- \pi^0$

 **What to look for**

- differences in  $D^0$  and  $\bar{D}^0$  Dalitz plots in 2-d.
- differences in angular moments
- Intermediate states (model-dep.)
- phase-space-integrated asymmetry

# CPV in 3-body SCS $D^0$ decays

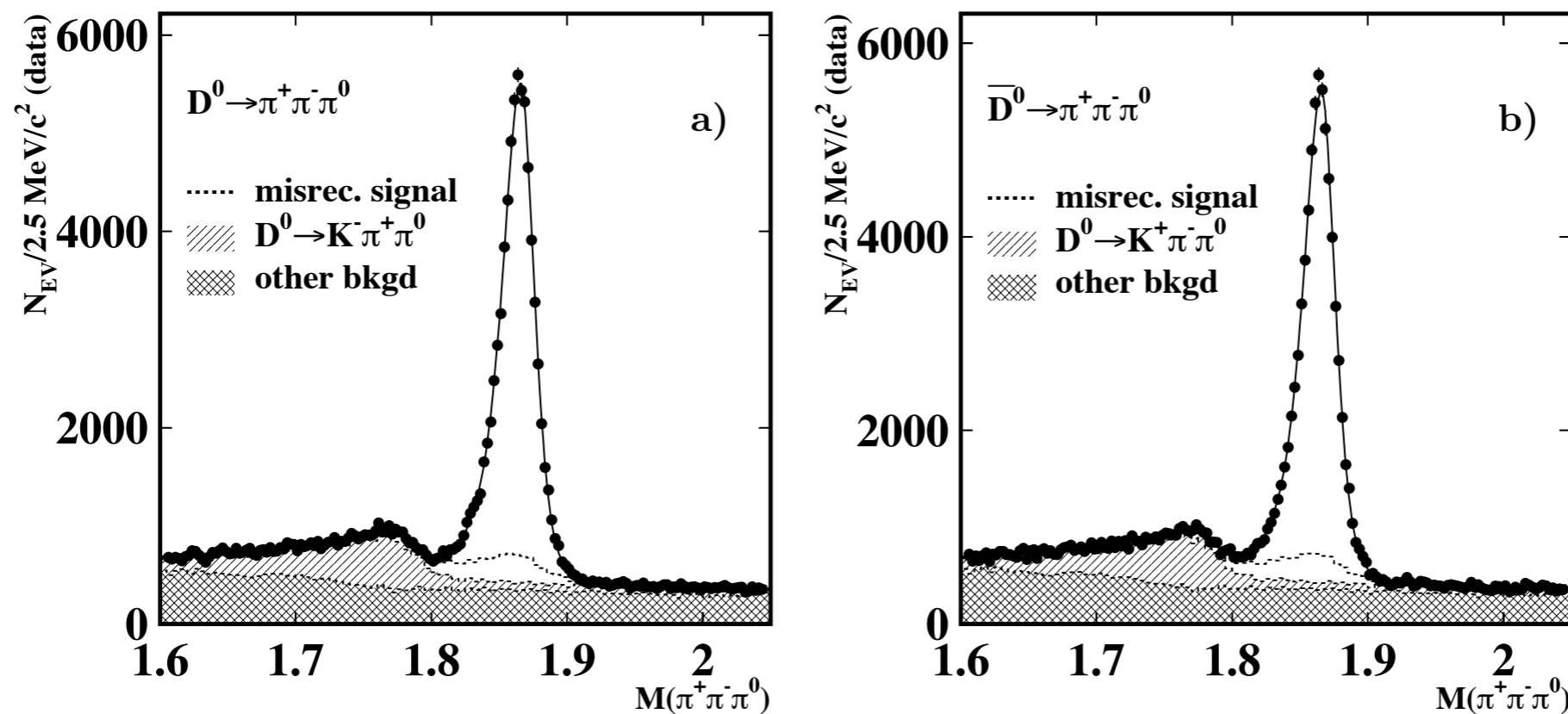
- Fit  $M(D^0)$  for signal & backg'd yield
- $D^{*+} \rightarrow D^0 \pi^+$  for flavor-tagging and backg'd suppression
- Fill separate Dalitz histograms
  - events from  $M(D^0)$  signal region for data
  - simulated backg'd w/ the normaliz'n fixed from the  $M(D^0)$  fit



$$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \pi^0) / \mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0) = (10.12 \pm 0.04(\text{stat}) \pm 0.18(\text{syst})) \times 10^{-2}$$

# CPV in 3-body SCS $D^0$ decays

- effi'cy-corrected signal yield separately for  $D^0$  and  $\bar{D}^0$
- detector-bias in tracking is the main source of syst. err.
- $A_{FB}$  effect is also studied with  $D^0 \rightarrow K^+ K^-$ ,  $\pi^+ \pi^-$  events



$$\begin{aligned}
 A_{CP} &= (S_{D^0} - S_{\bar{D}^0}) / (S_{D^0} + S_{\bar{D}^0}) = \\
 &= (0.43 \pm 0.41(\text{stat}) \pm 1.01(\text{track}) \pm 0.70(\text{other syst}))\%
 \end{aligned}$$



# CPV in 3-body SCS $D^0$ decays

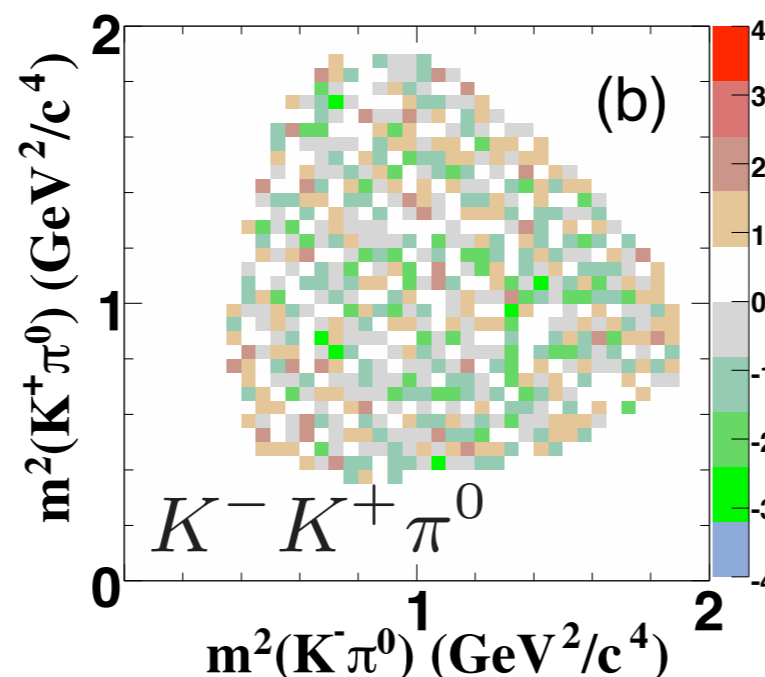
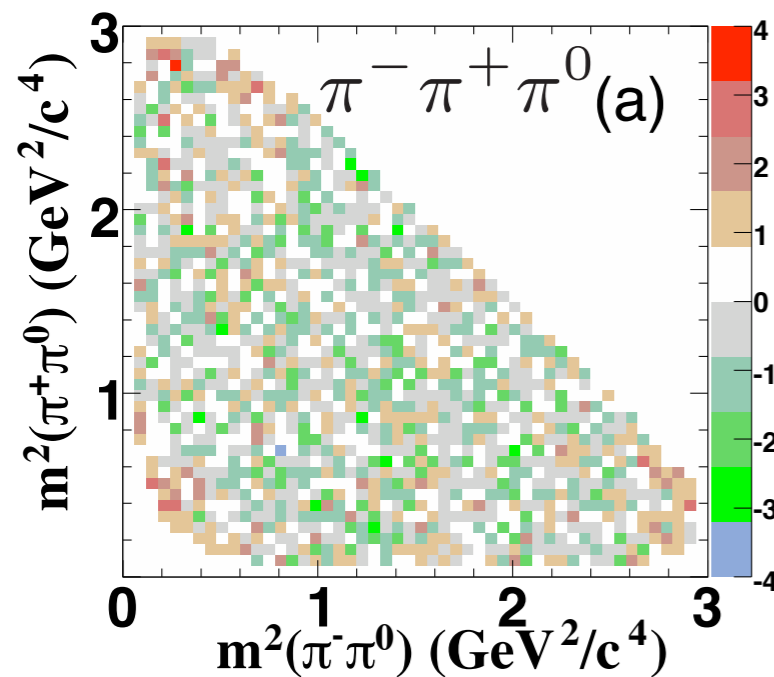
- a direct comparison of the effi'cy-corrected, backg'd-subtracted Dalitz plot for  $D^0$  and  $\bar{D}^0$

$$\Delta = (n_{\bar{D}^0} - R \cdot n_{D^0}) / \sqrt{\sigma_{n_{\bar{D}^0}}^2 + R^2 \cdot \sigma_{n_{D^0}}^2}$$

$$\chi^2/\nu = \frac{1}{\nu} \sum_{i=1}^{\nu} \Delta_i^2$$

$$R = 0.983 \pm 0.006$$

$$1.020 \pm 0.016$$



$\sim 1$  in the simulated ensemble

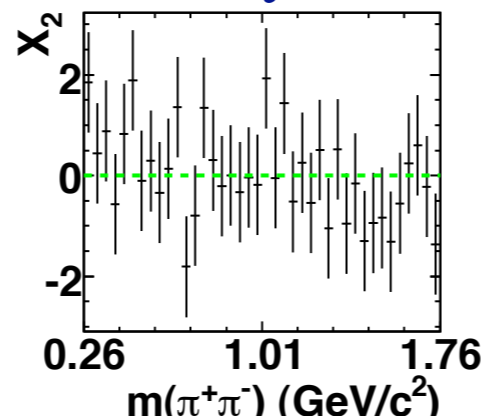
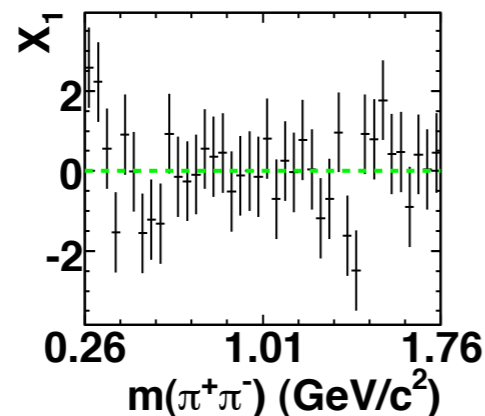
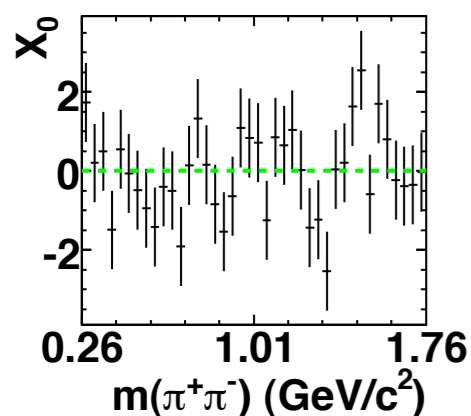
(Data)

1.020 ( $\pi\pi\pi$ ), 1.056 ( $KK\pi$ )

CL. for **No CPV**

0.328 ( $\pi\pi\pi$ ), 0.166 ( $KK\pi$ )

- asymmetry in moments of helicity angle  $\theta_H$



$$X_l = (\bar{P}_l - R \cdot P_l) / \sqrt{\sigma_{\bar{P}_l}^2 + R^2 \cdot \sigma_{P_l}^2}$$

CL. for **No CPV**

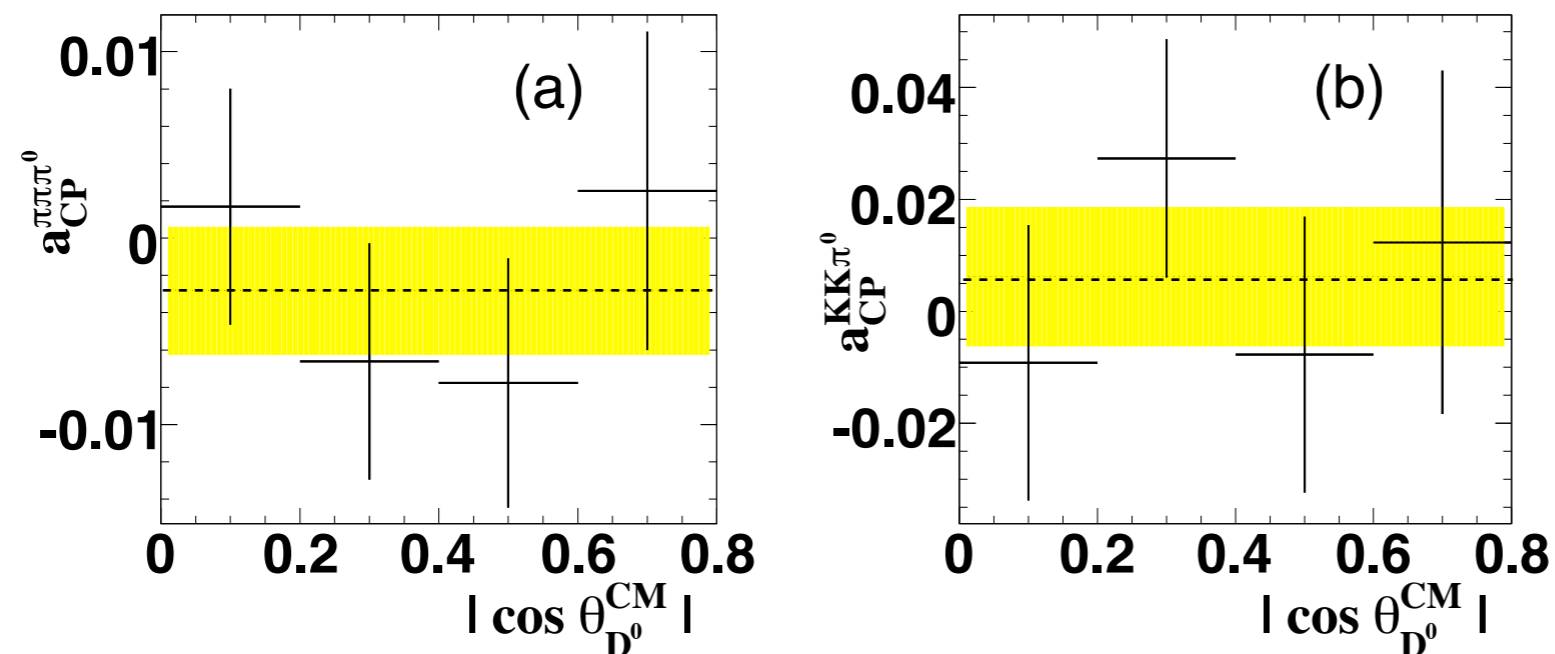
$\sim O(30\%)$





# CPV in 3-body SCS $D^0$ decays

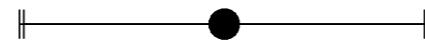
- model-dependent asymmetry in Dalitz plot amplitudes :  $\lesssim$  (a few)% and consistent with 0
- phase-space-integrated asymmetry



- any  $A_{FB}$  is cancelled in  $|\cos \theta_{D^0}^{CM}|$

$$A_{CP} = \begin{cases} (-0.28 \pm 0.34 \pm 0.19)\% & (\pi\pi\pi) \\ (0.62 \pm 1.24 \pm 0.28)\% & (KK\pi) \end{cases}$$

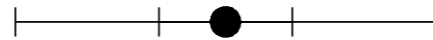
# CPV in 3-body SCS $D^0$ decays



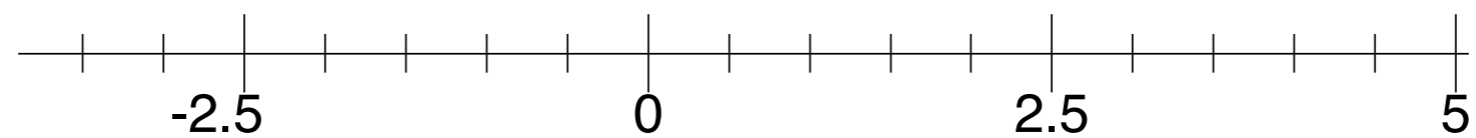
**BaBar ( $KK\pi$ )**



**BaBar ( $\pi\pi\pi$ )**

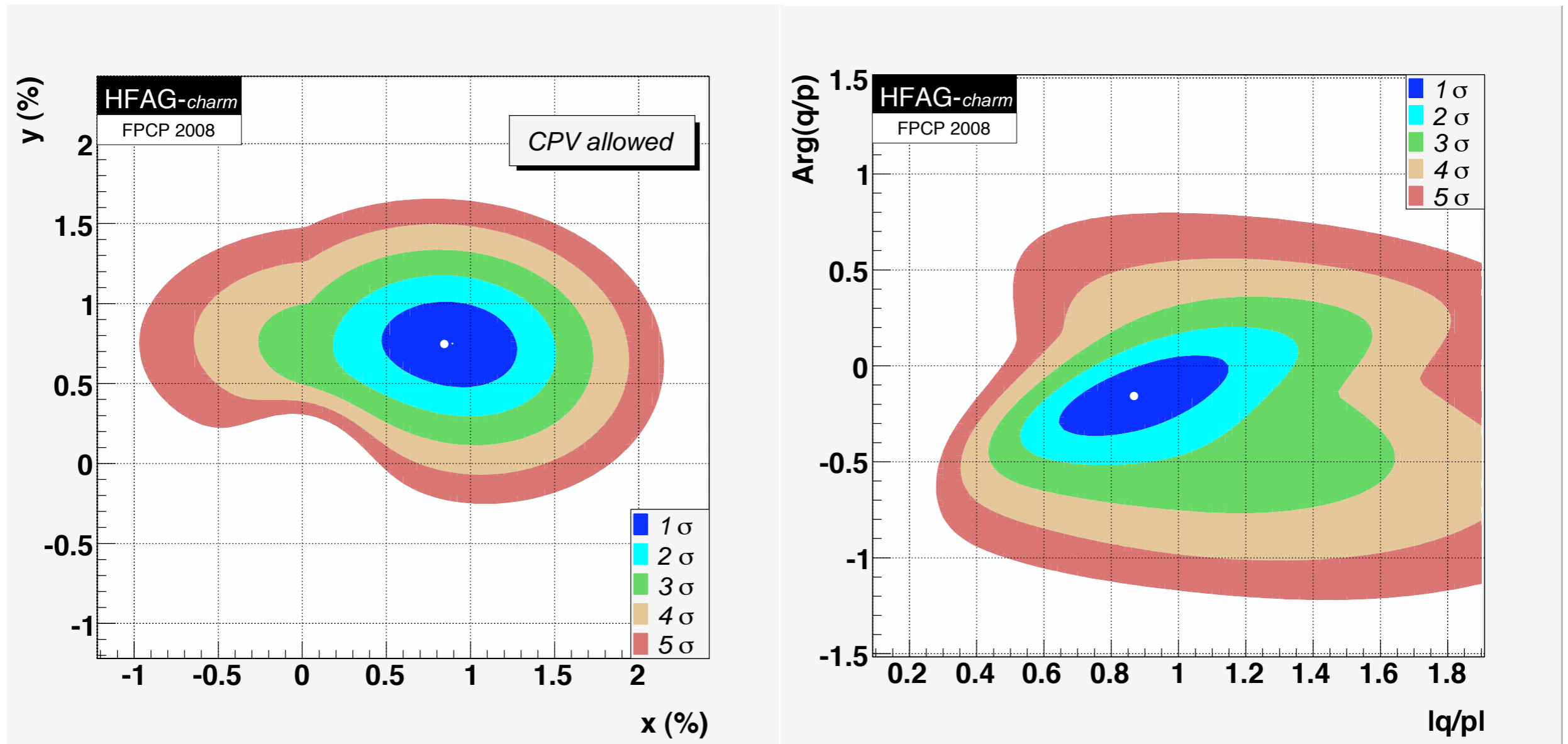


**Belle ( $\pi\pi\pi$ )**



$A_{CP}$  (%)

# Updated mixing/CPV parameters



# Summary

- 🎤 Firm and consistent evidences for  $D^0$  mixing
  - Systematic efforts are going on to measure  $D^0$  mixing parameters in various ways
- 🎤 No evidence for CPV in  $D^0$ 
  - Perhaps, not much bigger than  $O(1\%)$  level
  - Improving the syst. uncertainties shall be important