

2008

INTRODUCTION TO NUMERICAL ANALYSIS

Assignment 6

ASSIGNMENT 6-1

Generate the target distribution

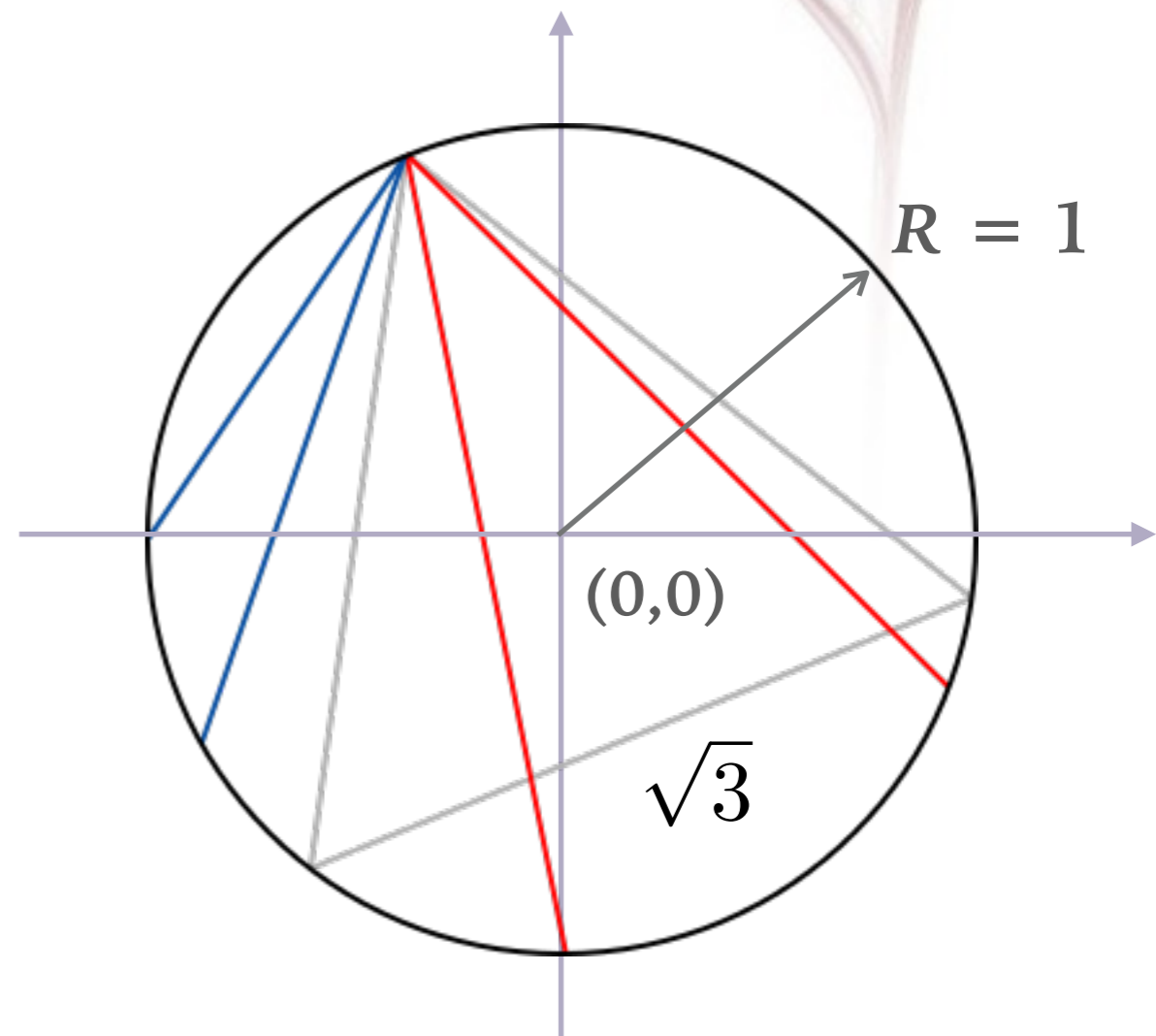
- Construct a function which takes the following two parameters as the arguments: N , a , b (where $a, b > 0$, and $b > a$). The function should return a NumPy array of shape $(N,)$ and filled with N random numbers x generated according to the following function within the boundary of $[a, b]$:

$$f(x) = \frac{1}{1+x}$$

ASSIGNMENT 6-2

Random chords

- Consider a circle, centered at $(0,0)$ with radius 1. Randomly choose two points on the circumference of the circle and calculate the distance between them. Construct a function which takes only an argument N , and it should return a NumPy array of shape $(N,)$ and filled with the length of the N chords constructed with the method above. Note $1/3$ of the chords should longer than 1.732!



ASSIGNMENT 6-3

“Smearred” Exponential

- Let’s produce a “smearred” exponential distribution with the following steps:

- Generate a random variable x according to the typical exponential distribution:

$$f(x) \propto \exp(-x/1.6)$$

- Generate another random variable y according to a Gaussian distribution:

$$f(y) \propto \exp\left[-0.5 \left(\frac{y-x}{0.2}\right)^2\right]$$

- Repeat the steps above.

- Construct a function which takes only an argument N , and it should return a NumPy array of shape $(N,)$ and filled with random number y generated with the method above.