

Neutral Pion-like Resonances at Photon Colliders



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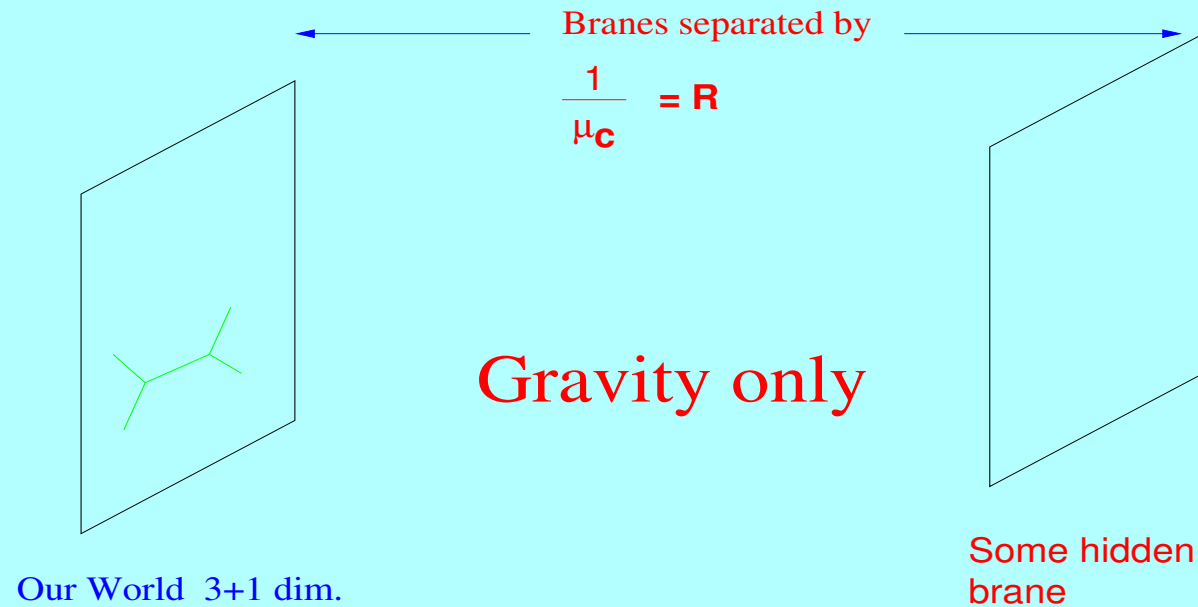
Outline

- What so unique about $\gamma\gamma$ collisions in probing new physics
- Highlights from large extra dimensions and Randall-Sundrum scenarios
- Techni-Pions of TC model

What so unique of $\gamma\gamma$ Collisions

- The SM $\gamma\gamma \rightarrow \gamma\gamma$ amplitude only goes through **box diagrams**, so **highly suppressed**.
- Any new physics that involves **tree-level exchanges** would be easily seen over the SM background.
- In particular, those with **anomaly-type couplings** to $\gamma\gamma$.
- Examples are low-scale gravity, the radion of RS model, techni-pions, ...

Low-scale gravity (ADD model)

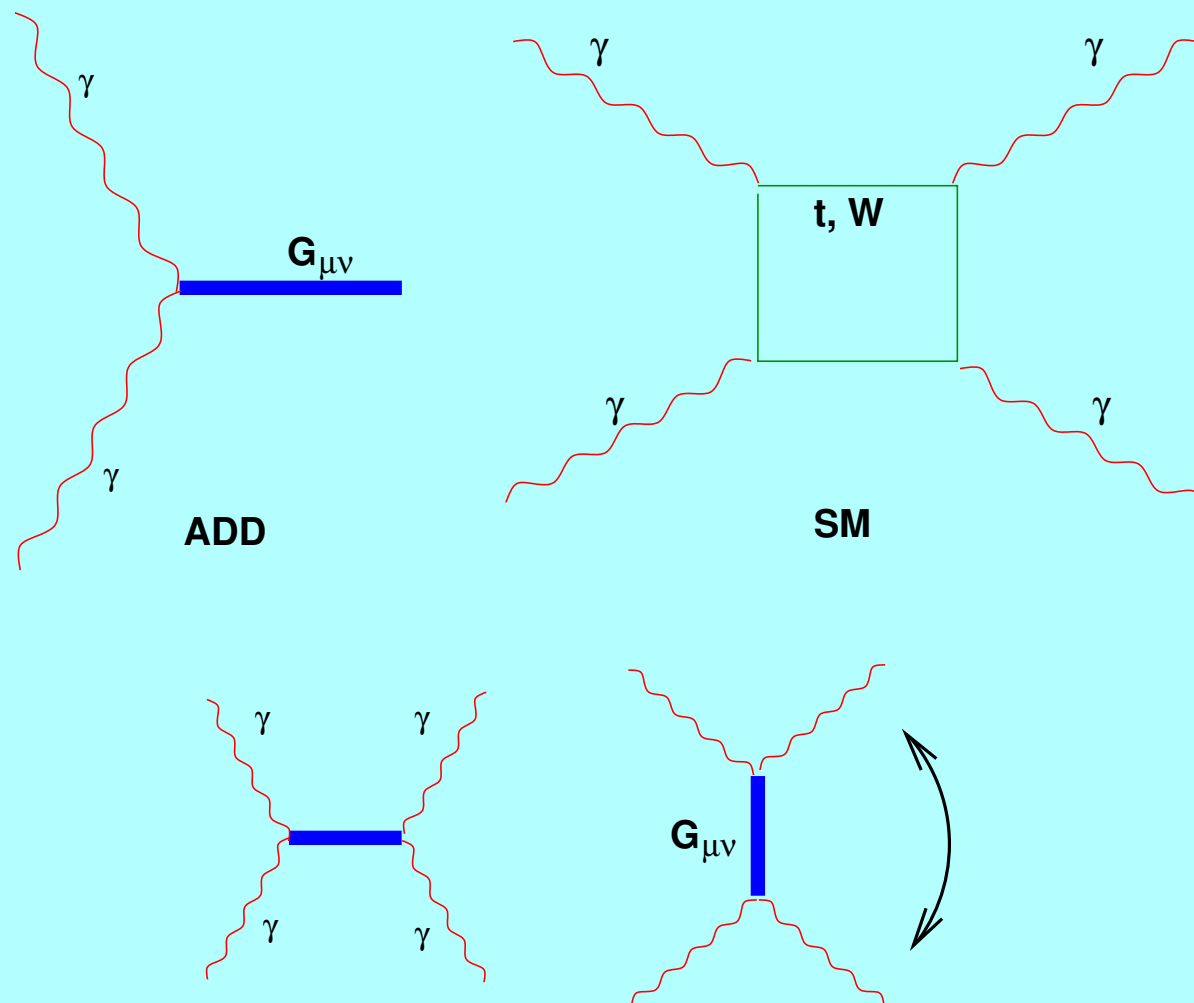


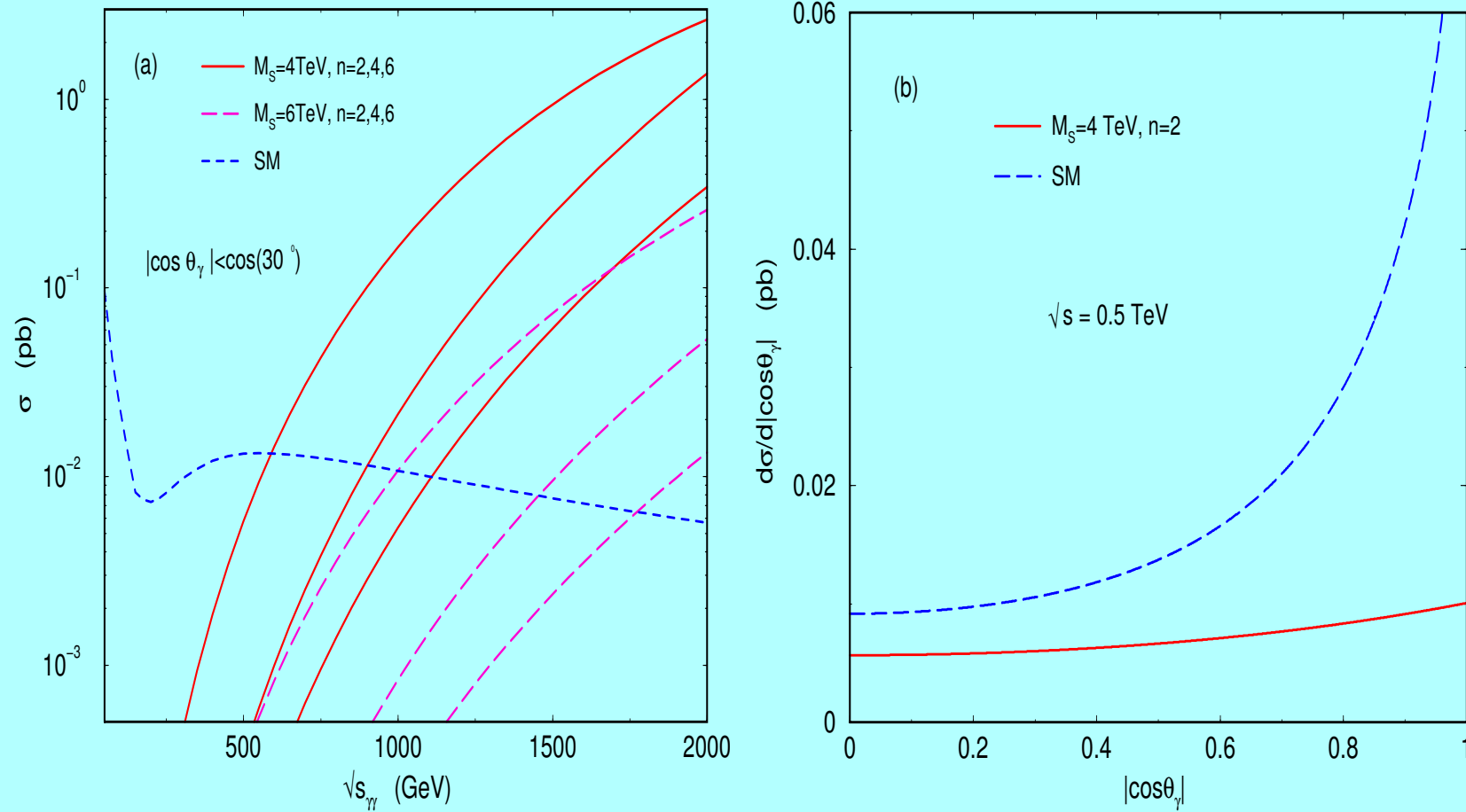
The size of the extra dimensions can be as large as $R \lesssim 1 \text{ mm}$.

$$\mu_c \equiv R^{-1} \gtrsim 10^{-4} \text{ eV} \ll M_{\text{EW}}$$

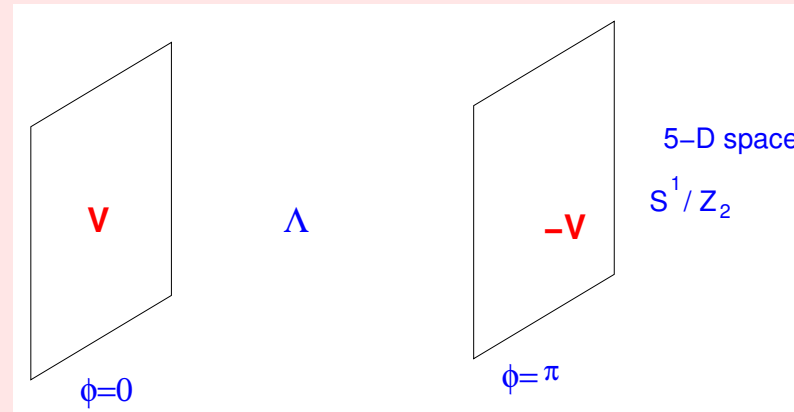
$$M_{\text{Pl}}^2 \sim M_D^{n+2} R^n \quad (\text{Gauss})$$

Light-by-light Scattering



$\gamma\gamma \rightarrow \gamma\gamma$ 

Randall Sundrum Model: Radion



The RS model has a 4D massless scalar, radion, about the background metric

$$ds^2 = e^{-2k\phi T(x)} g_{\mu\nu}(x) dx^\mu dx^\nu - T^2(x) d\phi^2$$

$T(x)$ is the modulus field describing the distance between the two branes.

A stabilization mechanism (GW) using a bulk scalar field to generate a potential.

The radion acquires a $O(0.1 - 1\text{TeV})$ mass with a coupling strength $1/\text{TeV}$.

Interactions of the Radion:

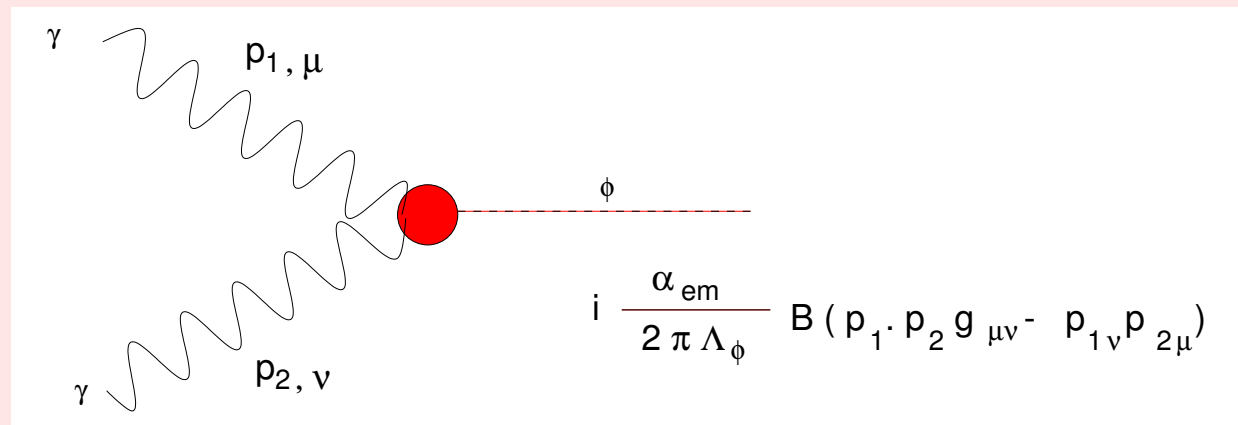
$$\mathcal{L}_{\text{int}} = \frac{\phi}{\Lambda_\phi} T_\mu^\mu(\text{SM}),$$

RS Radion

The radion coupling to a pair of gluons (photons) has a contribution from the trace anomaly.

$$T_{\mu}^{\mu}(\text{SM})^{\text{anom}} = \sum_a \frac{\beta_a(g_a)}{2g_a} F_{\mu\nu}^a F^{a\mu\nu} .$$

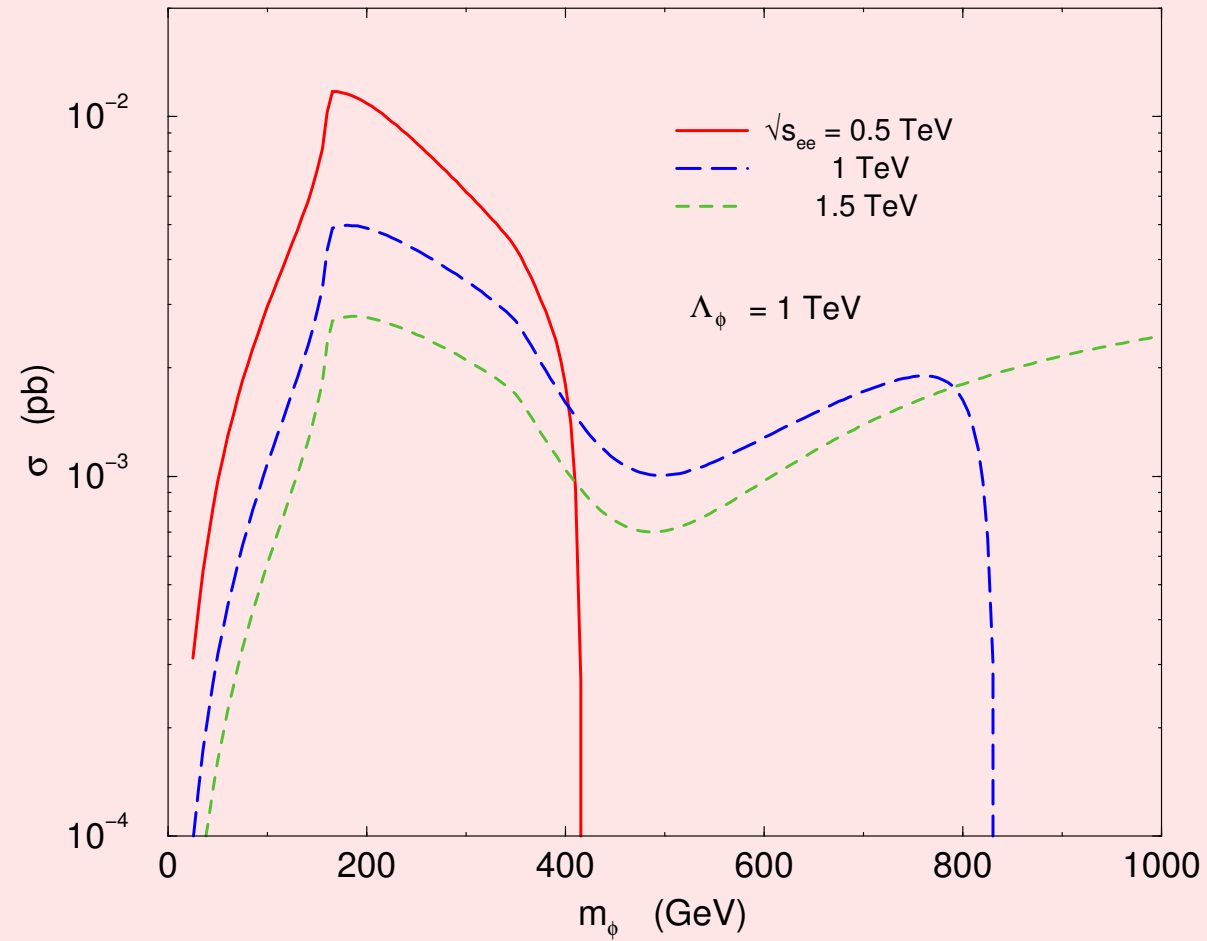
where $\beta_{\text{QCD}}/2g_s = -(\alpha_s/8\pi)b_{\text{QCD}}$ and $b_{\text{QCD}} = 11 - 2n_f/3$



where

$$B = b_2 + b_Y - (2 + 3y_W + 3y_W(2 - y_W)f(y_W)) + \frac{8}{3}y_t(1 + (1 - y_t)f(y_t)), \quad y_i = 4m_i^2/2p_1 \cdot p_2.$$

Randall Sundrum Radion



Higgs-Radion Mixing

Gauge and Poincare invariance do not forbid the mixing between the gravity scalar and the Higgs boson:

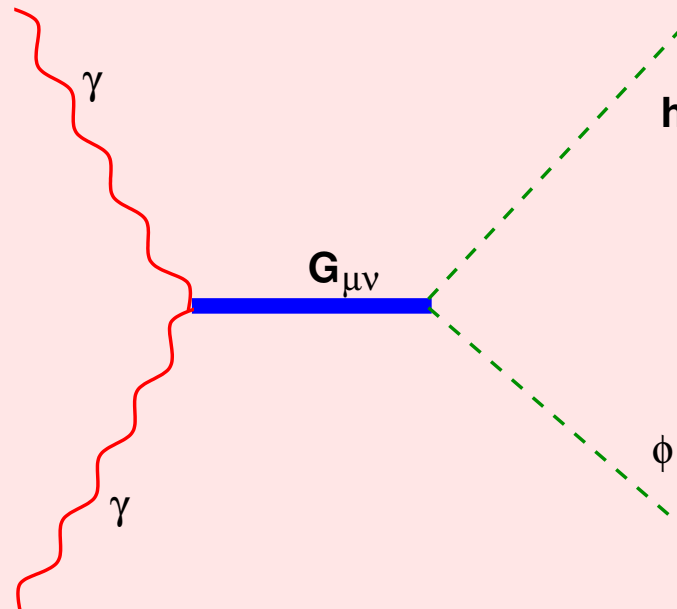
$$S_\xi = \xi \int d^4x \sqrt{g_{\text{vis}}} R(g_{\text{vis}}) \hat{H}^\dagger \hat{H},$$

where $R(g_{\text{vis}})$ is the Ricci scalar on the visible brane.

★ A nonzero ξ will induce some triple couplings

$$h - \phi - \phi, \quad h_{\mu\nu}^{(n)} - h - \phi, \quad \phi - \phi - \phi, \quad h_{\mu\nu}^{(n)} - \phi - \phi$$

$$\gamma\gamma \rightarrow G_{\mu\nu}^{(n)} \rightarrow h\phi$$



The corresponding analogs at e^+e^- and hadronic machines:

$$e^+e^- \rightarrow G_{\mu\nu}^{(n)} \rightarrow h\phi, \quad pp \rightarrow G_{\mu\nu}^{(n)} \rightarrow h\phi$$

have been performed (Cheung, Kim, Song PRD03, PRD04)

Neutral Techni-Pions

Because of the anomaly type coupling (like π^0 - γ - γ), we can use $\gamma\gamma$ collision to probe neutral-pion-like resonances.

Technicolor Straw Man model (TCSM, Lane 99):

- techni-isospin is a good symmetry
- the lightest techni-mesons are constructed solely from the lightest techni-fermion doublet (T_U, T_D) . They form isotriplet, isosinglet:

pseudoscalar: $\pi_T^{0,\pm}$, $\pi_T^{\prime 0}$, vector: $\rho_T^{0,\pm}$, ω_T^0

Consider two models of technicolor

Rescaled QCD model:

- A simple rescaling by the v/f_{π^0} . π_T^0 couples to $\gamma\gamma$, γZ , ZZ only.

Low-scale technicolor model:

- It is a multi-scale technicolor models. Quark and lepton masses are generated by broken extended technicolor gauge interactions in the walking technicolor model.
- There are two types of techni-fermions. One set condense at high scale set by $v = 246$ GeV. One set condense at low scale set by $f_{\pi_T} = v/\sqrt{N_D}$.
- Techni-pions will couple to normal quarks and leptons through Yukawa-type couplings.

$$\pi_T^0 \rightarrow b\bar{b}, t\bar{t}$$

- π_T^0 couples to $\gamma\gamma$, γZ , ZZ , gg , $b\bar{b}$.

The Anomaly Vertex

The anomaly coupling to π_T^0 - G_1 - G_2 :

$$\mathcal{M} = N_{TC} \mathcal{A}_{G_1 G_2} \frac{g_1 g_2}{2\pi^2 f_{\pi_T}} \epsilon_\nu \epsilon_\lambda \epsilon^{\nu\lambda\alpha\beta} P_{1\alpha} P_{2\beta} ,$$

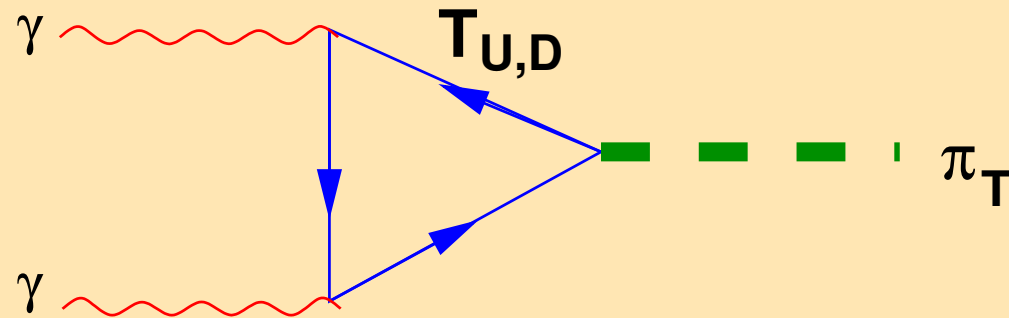
with

$$\mathcal{A}_{G_1 G_2} = \text{Tr}[T^a (\{T_1, T_2\}_L + \{T_1, T_2\}_R)]$$

T_i 's are the generators with the gauge boson G_i , and T^a is the axial current associated with the techni-pion

$$j^{\mu 5a} = \bar{\psi} \gamma^\mu \gamma^5 T^a \psi$$

$$\gamma\gamma \rightarrow \pi_T$$



$$\mathcal{A}_{\gamma\gamma} = \text{Tr}(T^a Q^2) \quad \text{with} \quad Q = \begin{pmatrix} Q_u & 0 \\ 0 & Q_d \end{pmatrix},$$

	Q_u	Q_d
rescaled	$2/3$	$-1/3$
low-scale	$4/3$	$1/3$

π_T^0 Production

$$\hat{\sigma}(\gamma\gamma \rightarrow \pi_T^0) = \frac{\pi m_{\pi_T}}{64} \left(N_{TC} \mathcal{A}_{\gamma\gamma} \frac{e^2}{\pi^2 f_{\pi_T}} \right)^2 \delta^{(0)}(\sqrt{\hat{s}} - m_{\pi_T})$$

Fold with photon luminosity function:

$$\sigma(\gamma\gamma \rightarrow \pi_T^0) = \frac{m_{\pi_T}^2}{2^5 s \pi^3} \left(\frac{N_{TC} \mathcal{A}_{\gamma\gamma} e^2}{f_{\pi_T}} \right)^2 \int_{x_{min}}^{x_{max}} \frac{1}{x} F_{\gamma/e}(x) F_{\gamma/e}\left(\frac{m_{\pi_T}^2}{sx}\right) dx$$

where

$$F_{\gamma/e}(x_i) = \frac{1}{D(\xi)} \left[1 - x_i + \frac{1}{1 - x_i} - \frac{4x_i}{\xi(1 - x_i)} + \frac{4x_i^2}{\xi^2(1 - x_i)^2} \right]$$

π_T^0 Decay

Rescaled model:

$$\Gamma_{total} = \frac{1}{2^4 \pi m_{\pi_T}} \left[\frac{c^2 m_{\pi_T}^4}{2^2} + \frac{c_1^2 (m_{\pi_T}^2 - m_Z^2)^3}{(m_{\pi_T}^2 + m_Z^2)} + c_2^2 (m_{\pi_T}^2 - 4m_Z^2)^2 \right]$$

$$B(\pi_T^0 \rightarrow \gamma\gamma) = \frac{\Gamma_{\gamma\gamma}}{\Gamma_{total}}$$

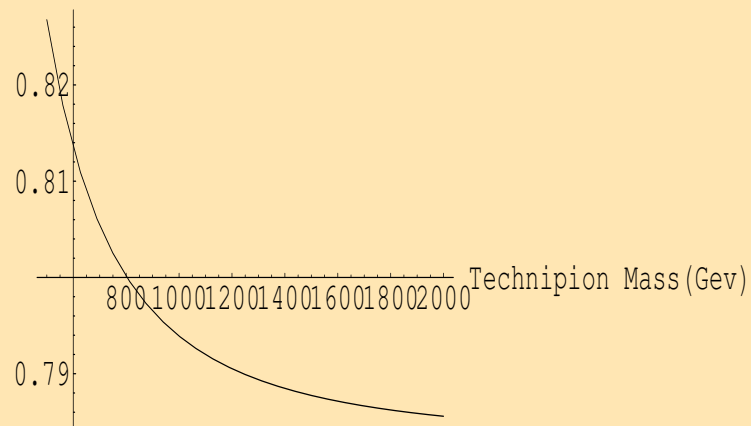
Low-scale model:

Additional contribution to the total width

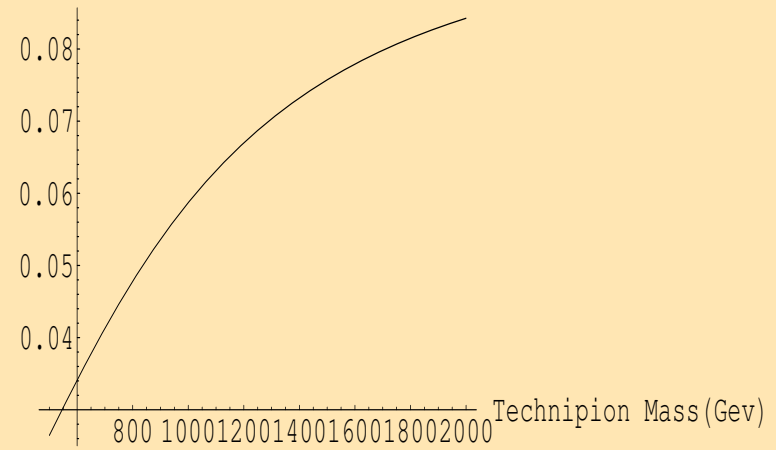
$$\Gamma(\pi_T^0 \rightarrow b\bar{b}) \Big|_{\text{low-scale}} = \frac{1}{16\pi f_{\pi_T}^2} N_b P_b C_{1b}^2 (m_b + m_{\bar{b}})^2$$

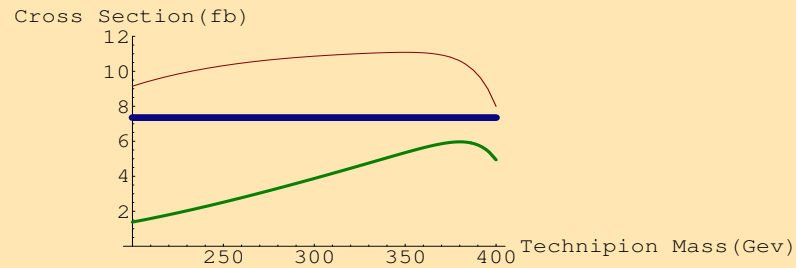
π_T^0 Decay: $B(\pi_T^0 \rightarrow \gamma\gamma)$

Branching Ratio

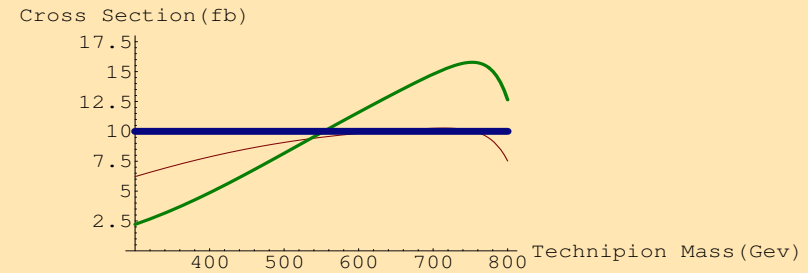
*Rescaled model*

Branching Ratio

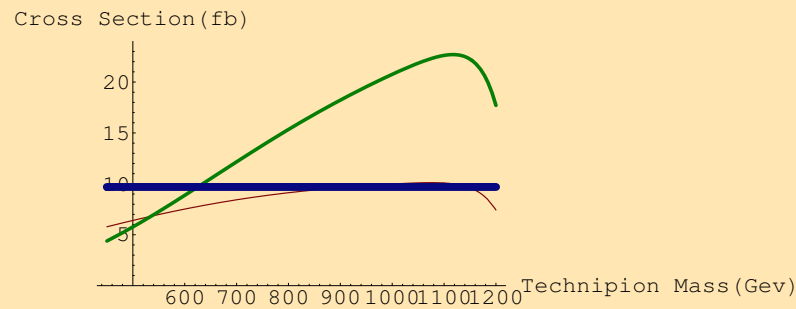
*low-scale model*

$$\gamma\gamma \rightarrow \pi_T^0 \rightarrow \gamma\gamma \text{ production}$$


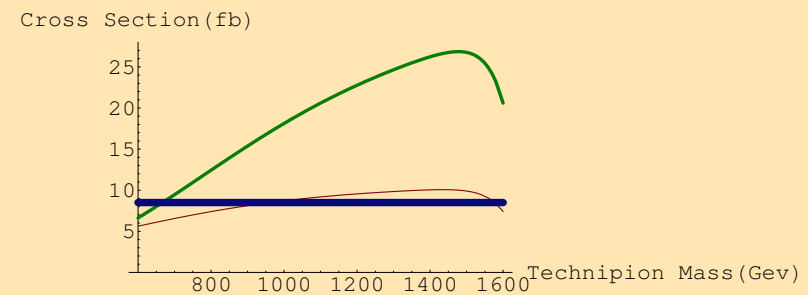
$$\sqrt{s_{ee}} = 0.5 \text{ TeV}$$



$$\sqrt{s_{ee}} = 1 \text{ TeV}$$



$$\sqrt{s_{ee}} = 1.5 \text{ TeV}$$



$$\sqrt{s_{ee}} = 2 \text{ TeV}$$

Summary

- Light-by-light scattering and $\gamma\gamma \rightarrow ZZ$ proceed via **box diagrams in the SM**.
- $\gamma\gamma \rightarrow \gamma\gamma$ is sensitive to the new physics that involves either tree-level couplings or anomaly-type couplings.
- Low scale gravity, RS radion are interesting examples.
- **Neutral techni-pions** of many technicolor models have anomalous couplings with photons. Photon colliders are unique in probing these kind of resonances.